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Edward Ransley  
School of Engineering, Computing and Mathematics

Shiqiang Yan

Scott Brown  
School of Engineering, Computing and Mathematics

Martyn Hann  
School of Engineering, Computing and Mathematics

David Graham

et al.  See next page for additional authors

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Authors

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A blind comparative study of focused wave interactions with floating structures
(CCP-WSI Blind Test Series 3)

Edward Ransley1, Shiqiang Yan2, Scott Brown1, Martyn Hann1, David Graham1, Christian Windi3, Pal Schmitt4, Josh Davidson5, John Ringwood5, Pierre-Henri Musiedlak1, Jinghua Wang2, Junxian Wang2, Qingwei Ma4, Zhihua Xie6, Ningbo Zhang7, Xing Zheng7, Giuseppe Giorgi8, Hao Chen6, Zaibin Lin9, Ling Qian9, Zhihua Ma5, Wei Bai9, Qiang Chen10, Jun Zang10, Haoyu Ding10, Lin Cheng11, Jinhai Zheng11, Hanbin Gu12, Xiwu Gong12, Zhenghao Liu13, Yuan Zhuang13, Decheng Wan13, Harry Bingham14, Deborah Greaves1

1: University of Plymouth, UK; 2: City, University of London, UK; 3: Maynooth University, Ireland; 4: Queen’s University Belfast, UK; 5: Budapest University of Technology and Economics, Hungary; 6: Cardiff University, UK; 7: Harbin Engineering University, China; 8: Politecnico di Torino, Italy; 9: Manchester Metropolitan University, UK; 10: University of Bath, UK; 11: Hohai University, China; 12: Zhejiang Ocean University, China; 13: Shanghai Jiao Tong University, China; 14: Technical University of Denmark

ABSTRACT

Results from the Collaborative Computational Project in Wave Structure Interaction (CCP-WSI) Blind Test Series 3 are presented. Participants, with numerical methods, ranging from low-fidelity linear models to high-fidelity Navier-Stokes (NS) solvers, simulate the interaction between focused waves and floating structures without prior access to the physical data. The waves are crest-focused NewWaves with various crest heights. Two structures are considered: a hemispherical-bottomed buoy and a truncated cylinder with a moon-pool; both are taut-moored with one linear spring mooring. To assess the predictive capability of each method, numerical results for heave, surge, pitch and mooring load are compared against corresponding physical data. In general, the NS solvers appear to predict the behaviour of the structures better than the linearised methods but there is considerable variation in the results (even between similar methods). Recommendations are made for future comparative studies and development of numerical modelling standards.

KEY WORDS: Code comparison; numerical validation; CFD; PIC; linear potential theory; nonlinear Froude-Krylov; hybrid codes; cylinder; moonpool; wave energy convertor; heave; surge; pitch; mooring load.

INTRODUCTION

Numerical predictions are being used more and more frequently in the design and development of offshore installations. Consequently, there exists an exhaustive range of numerical models, covering the entire spectrum of fluid phenomena (typically with considerable overlap in capability across large groups of existing codes). The usual compromise, between computational efficiency and level of the physics being solved, i.e. model ‘fidelity’, still strongly dictates the model used by end users. Despite this, there is no consensus on the required numerical model fidelity for any particular wave structure interaction (WSI) application and it is likely that in most cases either important physical phenomena are neglected or excessive computational resources are used. Consequently, if numerical models (particularly high-fidelity ones) are to be used effectively by the industry, a greater understanding of the boundaries of each models predictive capability is required (Ransley et al., 2016). Furthermore, as demonstrated in the CCP-WSI Blind Test Series 1 (which considered a fixed structure) (Ransley et al., 2019), judging the predictive capability of a model quantitatively is far from trivial; the ‘quality’ of the numerical result tends to be strongly affected by the implementation strategy, and experience, of the operator and what constitutes a ‘good’ result depends heavily on the application and the requirements of the end user.

The CCP-WSI Blind Test Workshops have been designed to tackle these issues and raise the necessary questions to maximise the value of future comparative studies. It is hoped this will accelerate the development of numerical modelling standards in WSI applications and increase the uptake of state-of-the-art numerical techniques by industry. These workshops bring together numerical modellers from the WSI community and assess the numerical codes currently in use by inviting participants to simulate a set of bespoke physical validation experiments, covering a range of relevant complexities, without prior access to the physical measurements. The ‘blind’ nature of the CCP-WSI Blind Test Workshops allows for assessment of numerical methods, without artificial manipulation of the results to match the physical measurements (which clearly represents a potential source of bias in traditional comparative studies). Furthermore, to enable contributions using all WSI modelling strategies, no constraints are applied to the computational implementation and participants are encouraged to use ‘best practice’ to generate their solutions. However, as was made clear in the CCP-WSI Blind Test Series 1 (Ransley et al., 2019), participants can have a very different idea of what ‘best’ practice is and this can result in distinct differences in the quality of the solution, even when comparing similar models. This does complicate the assessment but, is important in demonstrating the risk, to industry end users, posed by a lack of best practice guidelines (without which the appropriate constraints are unknown anyway). It is, therefore, critical that this effort continues and compliments other efforts (Wendt et al. 2019) to help standardise numerical modelling practices. Only then will we make progress towards understanding the true predictive capability of different models, converge towards a manageable suite of tools and extend the real benefits of this effort to industry.
CCP-WSI Blind Test Workshops - Series 3

The CCP-WSI Blind Test Series 3 is held in conjunction with the International Society of Offshore and Polar Engineers (ISOPE) conference, in collaboration with the International Hydrodynamics Committee (IHC) and builds on the Blind Test Series 1 (Ransley et al. 2019), in which participated numerical models are compared in terms of pressure and run-up on a fixed FPSO model in focused waves. The release of the Series 3 test cases was made in September 2018 and the showcase event was held over a series of special sessions at the 2019 ISOPE conference in Honolulu, Hawaii (16-21st June 2019). For more information on the CCP-WSI Blind Tests please visit the CCP-WSI website at http://www.ccpp-ysi.ac.uk/blind_test_workshops where supporting material is available including complementary references, photographs from the experiments and other related resources.

TEST CASES

The CCP-WSI Blind Test Series 3 test cases consist of three focused wave events, with a range of steepness, $kA = 0.13$–0.21, incident upon two separate, floating structures: a hemispherical-bottomed buoy (Geometry 1) and a truncated cylinder with a cylindrical moon-pool (Geometry 2). Here, $k$ is the wave number associated with the peak period, $T_p$, of the underlying energy spectrum of the wave and $A$ is the crest amplitude of the crest focused wave assuming linear superposition of the underlying wave components. All waves are non-breaking in isolation. The purpose of these particular test cases is to measure the predictive capability, of a wide range of numerical WSI codes, as a function of wave steepness and geometric complexity (Geometry 2 is considered to be more complex due to the ‘internal’ body of water within the moon-pool), and evaluate the required model fidelity when assessing critical design factors, such as the motion of floating structures and loads in a mooring system.

Both structures are axis-symmetric with their mooring attachment located level with the bottom of the structure on the axial line (in the case of Geometry 2 a frame of three 20 mm wide, 3 mm thick, steel bars are welded to the structure to enable the mooring attachment). The two buoys are designed to resemble simple, scale-model, wave energy converters (WECs) and are ballasted to have similar drafts and water-plane areas (in an attempt to isolate the effect of the moon-pool and relate this to the predictive capability of the numerical models). The dimensions and mass properties of the two structures are given in Figure 1 and Table 1 respectively, where $z_{CoM}$ is the axial (vertical) distance to the Centre of Mass (CoM), from the bottom of the buoy/mooring attachment, and $I_{zz}$ is the moment of inertia about the vertical ($z$) axis. The moments of inertia corresponding to the other two geometric axes, $I_{xx}$ and $I_{yy}$, are given relative to the CoM of each of the structures. Complimentary work involving Geometry 1 can be found in Hann et al. (2015) and Ransley et al. (2017).

![Fig. 1 Dimensions, including the positions of the centre of mass (CoM) and mooring attachment, for: (a) Geometry 1, and; (b) Geometry 2.](image1)

<table>
<thead>
<tr>
<th>Structure</th>
<th>Mass (kg)</th>
<th>$z_{CoM}$ (m)</th>
<th>$I_{xx}$ (kgm$^2$)</th>
<th>$I_{yy}$ (kgm$^2$)</th>
<th>$I_{zz}$ (kgm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>G1</td>
<td>43.674</td>
<td>0.191</td>
<td>1.620</td>
<td>1.620</td>
<td>1.143</td>
</tr>
<tr>
<td>G2</td>
<td>61.459</td>
<td>0.152</td>
<td>3.560</td>
<td>3.560</td>
<td>3.298</td>
</tr>
</tbody>
</table>

Table 1 Mass properties of Geometry 1 (G1) and Geometry 2 (G2).

In all cases, the structure is taut-moored using the same linear spring mooring with a stiffness of 67 N/m and a rest length of 2.199 m. Table 2 gives some key parameters when the structure is at rest ($z = 0$ corresponds to the still water level).

In each experiment, the six degrees of freedom (6DOF) motion of the structure is recorded using an optical motion capture system; the inline load in the mooring is recorded using a single-axis load cell attached to the basin floor via a universal joint, and; the surface elevation in the vicinity of the structures is recorded using an array of resistive wave gauges.

Experimental Set-up

Basin geometry

The experiments were performed in the Coastal, Ocean And Sediment Transport (COAST) Laboratory Ocean Basin (35 m long × 15.5 m wide) at the University of Plymouth, UK. The basin has 24 flap-type, force-feedback-controlled wavemakers (hinge depth of 2 m). The water depth at the wavemakers is 4 m and there is a linear slope to the working area where the water depth, $h$, was set to 3.0 m. At the far end of the basin there is a parabolic absorbing beach (Figure 2).

Structure position and wave gauge layout

13 wave gauge positions were used according to Figure 3. Position 5 corresponds to the rest position of the buoy(s) (with the structure in place gauge 5 was removed but the same number system maintained).

Test Program and Wave Parameters

For each test case, the incident waves were generated using paddle control software that is designed to reproduce the desired free-surface elevation by applying various corrections to account for the change in water depth in front of the wave paddles and the nonlinear propagation of the wave fronts. Each wave was created using linear superposition of 244 wave fronts with frequencies evenly spaced between 0.101563 Hz and 2 Hz. All waves in the CCP-WSI Blind Test Series 3 are unidirectional, non-breaking and crest-focused, i.e. each of the contributing wave components has a phase of 0 at a theoretical focus location, $x_0$. The amplitudes of the components are derived by applying the NewWave theory (Tromans et al., 1991) to a Pierson-Moskowitz spectrum with the three waves, in Series 3, differing only by crest height, i.e. the waves

![Fig. 2 Schematic of the COAST Laboratory Ocean Basin.](image2)
Released Data

As discussed in the CCP-WSI Blind Test Series 1 (Ransley et al., 2019), released until after all participants had submitted their final results and it maker signals are used. The remaining physical measurements were not the incident waves in cases including the structure, as the same wave-of the waves is good (2.5% maximum relative standard deviation, \( \sigma \)) random error associated with the wave generation, and; the repeatability non-breaking, compact focused wave groups help minimise sources of standing of the physical model set-up and experimental errors, leading active studies, and numerical validation activities, fail to provide conclu-

ical model validation. Furthermore, it must be recognised that, in order that bespoke experiments are conducted with the sole purpose of numer-

cient to reproduce the incident waves in cases including the structure, as the same wave-maker signals are used. The remaining physical measurements were not released until after all participants had submitted their final results and it is these ‘blind’ results that are reported in this paper.

Physical Measurement Errors and Experimental Limitations

As discussed in the CCP-WSI Blind Test Series 1 (Ransley et al., 2019), it is crucial that the errors/uncertainties in the physical validation experiments are understood well if a conclusive, quantitative assessment of predictive capability is to be made. As is the case here, it is recommended that bespoke experiments are conducted with the sole purpose of numerical model validation. Furthermore, it must be recognised that, in order to differentiate the capabilities of high-fidelity models, an equally ‘high-fidelity’ physical data set is required. It is too often the case that comparative studies, and numerical validation activities, fail to provide conclusive measures of predictive capability due to a less-than-thorough understanding of the physical model set-up and experimental errors, leading to prohibitive uncertainties in the validation data. As in Series 1, the non-breaking, compact focused wave groups help minimise sources of random error associated with the wave generation, and; the repeatability of the waves is good (2.5% maximum relative standard deviation, \( \sigma_{rel} \), in the crest height of the steepest wave, over 5 repeats, and much less for the less steep waves, \( \pm1\% \)). The repeatability of the body motion is also good with a \( \sigma_{rel} \) in the maximum heave, surge and pitch of 0.3%, 1.2% and 1.8% respectively. Systematic errors, particularly those present in the description of the structure and mooring system, are the biggest concern in these tests: the precise dimensions of the structures and mooring line may differ by less than 1% but there is greater uncertainty in the mass properties of the two structures and a series of assumptions have been made about the mooring line. The masses and moments of inertia of the two structures have been measured using a compound pendulum ‘swing’ test (Hinrichsen, 2014) and verified against outputs from a comprehensive computer-aided design (CAD) model. However, due to practical limitations over the optimal pendulum lengths, the precision of the swing test is uncertain and the accuracy questionable, particularly when measuring the moments of inertia. Consequently, the potentially erroneous description of the moments of inertia may lead to discrepancies between the physical and numerical results, particularly in the rotational behaviour, i.e. pitch. However, since all the participants use the same mass properties, convergence is, at least, expected between the numerical models. Lastly, neither the mass or drag properties of the mooring line are known: participants are advised to assume the mooring is massless and offers no resistance to the fluid. Furthermore, the universal joint on the basin floor is assumed to be idealised. Consequently, any dynamic behaviour/inertia effects or drag on the mooring, that were present in the physical experiments, will not be captured in the numerical models.

NUMERICAL METHODS

Participating Codes

The CCP-WSI Blind Test Series 3 involved 32 participants from 14 academic institutions. There were 10 submissions ranging from linear potential theory (LPT) to Navier-Stokes (NS) solvers; including hybrid (coupled) methods, particle methods, finite difference methods (FDM), finite element methods (FEM) and finite volume methods (FVM). No constraints on the implementations of the models were applied as part of the test. Each method is described below and summarised in Table 4.

Particle-In-Cell (PIC) method (in-house)

This model employs the hybrid Eulerian-Lagrangian PIC method to solve the incompressible NS equations for single-phase free-surface flows. Fluid-solid interaction is incorporated via a Cartesian cut-cell-based, two-way coupling algorithm (Chen et al., 2019a). Waves are generated using a piston-type wave paddle with the displacement, based on first-order wavemaker theory, derived iteratively by adjusting the theoretical focus location and amplitude. Wave absorption is via an improved relaxation approach (Chen et al., 2019b). The computational domain is 21 m long, 6 m wide and 4 m tall and consists of \( \sim \) 32 million cells (edge length 0.025 m) and \( \sim \) 189 million particles. Dynamic time-stepping is used (\( Co = 0.5 \)). Laminar flow is assumed, i.e. no turbulence modelling is employed. Computation was performed on 160 \( \times 2.6 \) GHz cores.

OpenFOAM using source-term

This method uses the open-source, FVM-based, OpenFOAM (v4.1) and solves the two-phase, incompressible, Reynolds-averaged NS (RANS) equations using volume of fluid (VOF) interface capturing (Rusche, 2002). Body motion is accommodated via dynamic mesh-deformation. Incident waves are generated using an impulse source method (Schmitt et al., 2018) with the required source term determined via an iterative calibration method. Wave absorption is achieved via a numerical beach implementation (Schmitt & Elsaesser, 2015). The computational domain is 28.75 m long, 7.825 m wide (utilising a symmetry-plane) and 6 m tall (3 m of air phase) and consists of \( \sim \) 1 million cells (edge lengths 1.9 m-0.015 m). A fixed time-step of 0.002 s is used. Laminar flow is assumed. Computation was performed on 23 \( \times 2.4 \) GHz cores (Windt et al., 2019).

![Fig. 3 Wave gauge layout; wave probe position 5 corresponds to the position of the structure’s CoM in cases with the structure included [all dimensions in mm] [Not to scale].](image-url)

<table>
<thead>
<tr>
<th>Table 3 Wave conditions used in the CCP-WSI Blind Test Series 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case</td>
</tr>
<tr>
<td>1BT3</td>
</tr>
<tr>
<td>2BT3</td>
</tr>
<tr>
<td>3BT3</td>
</tr>
</tbody>
</table>
Hybrid FNPT

LPT

ure 2) with a characteristic cell size of 0.075 m. The NS domain is 6 m
wavemakers. The FNPT domain mimics the physical wave basin (Fig-
ination and absorption is achieved (in FNPT domain) using self-adaptive
solver, using domain decomposition and a coupling boundary (Li et al.,
QALE-FEM (Ma and Yan, 2006 & 2009), with OpenFOAM's VOF, NS
∼
unknowns in total. Computation was performed using 4
The geometry is represented exactly using high-order B-splines with 54
the measured surface elevation signal at probe 5 in the empty tank test.
are assumed to be a linear superposition of the Fourier coe
coefficients from
linear spring (W AMIT, Inc., 2019; Bingham, 2019). The incident waves
2.4 GHz cores were used (Yan et al., 2020).

Hybrid FNPT/NS (in-house)

NS Solver (FVM)

in-house)

OpenFOAM

overset meshing

This method is based on OpenFOAM (v1706) and solves the RANS
ations for two, incompressible fluids using a VOF scheme. Overset
meshing functionality is applied to accommodate the moving boundary
patch (Chen et al., 2019a). The waves are generated and absorbed us-
ing IHFOAM (Higuera et al., 2013). The incident waves are generated
ased on the second order irregular wave theory where the components
are derived from the given theoretical spectrum. The computational do-
main is 25 m long, 6 m wide and 4 m tall (1 m of air phase) and consists
of 4.5 million cells (edge length 0.011875 m - 0.25 m). Dynamic time-
stepping is used (Co = 0.35). The k-ω SST turbulence model is applied.
Computation is performed using 64 × 1.7 GHz cores (Chen et al., 2019b).

Nonlinear Froude-Krylov

This numerical method implements nonlinear kinematics and nonlinear
Froude-Krylov force calculations in a linear potential theory-based
framework (Giorgi & Ringwood, 2018a). The waves are a linear super-
position of components, derived from the surface elevation at probe 5 in
the empty tank tests, propagated using linear dispersion and including
Wheeler-stretching (Giorgi & Ringwood, 2018b). A fixed time-step of
0.04 s is used. No viscous drag correction is included (as this was not
provided). The algorithm was run on one 3.5 GHz core (Giorgi, 2019).

OpenFOAM using waves2Foam

This method is based on OpenFOAM (v5.0) and solves the RANS
ations for two incompressible fluids using a VOF scheme (Rusche, 2002).
Body motion is accommodated via dynamic mesh-deformation. Inci-
dent waves are generated using an expression-based boundary condition,
formed from the linear superposition of wave components derived using
an FFT of the surface elevation at probe 1 in the empty tank test. Wave
absorption is achieved using the relaxation zone approach (Jacobson et
al., 2012). The computational domain is 25 m long, 15.5 m wide and 6 m
tall and consists of ≈11 million cells (edge lengths 0.5 m-0.255 m). Dy-
namic time-stepping is used (Co = 0.5). Laminar flow is assumed. Com-
putation was performed on 128 × 2.5 GHz cores (Brown et al., 2019).

NS Solver using FVM (in-house)

nao-FOAM-SJTU (in-house code based on OpenFOAM) solves the two-phase, incompressible RANS equations using FVM and a VOF in-
face capturing scheme (Wang et al., 2019). Body motion is accommo-
dated via dynamic mesh-deformation. Incident waves are generated us-
ing an expression-based, Dirichlet-type boundary condition derived from
the theoretical wave descriptions. Wave absorption is via an additional
source term in the governing equations (a sponge layer approach). The
computational domain is 27 m long, 8 m wide and 6 m tall (2 m of air)
and consists of ≈2.3 million cells (edge lengths 0.1 m-0.005 m). A fixed
time-step of 0.008 s is used. Laminar flow is assumed. Computation was
performed on 20 × 2.8 GHz cores (Liu et al., 2019).

Table 4 Summary of numerical methods used by participants

<table>
<thead>
<tr>
<th>Code ref.</th>
<th>Discret. scheme</th>
<th>Theory</th>
<th>Free-surface treatment</th>
<th>Turbulence treatment</th>
</tr>
</thead>
<tbody>
<tr>
<td>PIC</td>
<td>FDM + meshless</td>
<td>NS</td>
<td>MAC+ (1-phase)</td>
<td>laminar</td>
</tr>
<tr>
<td>OpenFOAM</td>
<td>FVM</td>
<td>NS</td>
<td>VOF</td>
<td>laminar</td>
</tr>
<tr>
<td>Hybrid FNPT/NS</td>
<td>FEM/ FVM</td>
<td>FNPT/ NS</td>
<td>1-phase/ VOF</td>
<td>inviscid/ laminar</td>
</tr>
<tr>
<td>LPT+WAMIT</td>
<td>BEM</td>
<td>LPT/ NS</td>
<td>linearised</td>
<td>inviscid</td>
</tr>
<tr>
<td>Hybrid FNPT/SPH</td>
<td>FEM/ SPH</td>
<td>FNPT</td>
<td>single-phase</td>
<td>inviscid</td>
</tr>
<tr>
<td>NS Solver (FDM)</td>
<td>FDM</td>
<td>NS</td>
<td>VOF</td>
<td>LES (SMA)</td>
</tr>
<tr>
<td>OpenFOAM (overset)</td>
<td>FVM</td>
<td>NS</td>
<td>VOF</td>
<td>RANS (SST)</td>
</tr>
<tr>
<td>Nonlinear Froude-Krylov</td>
<td>Analytical</td>
<td>LPT</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>OpenFOAM (waves2Foam)</td>
<td>FVM</td>
<td>NS</td>
<td>VOF</td>
<td>laminar</td>
</tr>
<tr>
<td>NS Solver (FVM)</td>
<td>FVM</td>
<td>NS</td>
<td>VOF</td>
<td>laminar</td>
</tr>
</tbody>
</table>

Hybrid FNPT/NS method (in-house)

The hybrid FNPT/NS solver, qaleFOAM, combines the FNPT model,
QALE-FEM (Ma and Yan, 2006 & 2009), with OpenFOAM’s VOF, NS
solver, using domain decomposition and a coupling boundary (Li et al.,
2018). Body motion (in NS domain) is via mesh-deformation. Wave gen-
eration and absorption is achieved in (FNPT domain) using self-adaptive
waversmakers. The FNPT domain mimics the physical wave basin (Fig-
ure 2) with a characteristic cell size of 0.075 m. The NS domain is 6 m
long, 3 m wide and 4.5 m tall and consists of 613k cells (edge lengths
0.02 m-0.1 m). Dynamic time-stepping is used (Co = 0.4). Laminar flow
is assumed. 16 × 2.4 GHz cores were used (Yan et al., 2020).

LPT + WAMIT method (in-house)

In this method, linear potential theory (LPT) is used to compute the
frequency-domain response of the body, including the mooring line as a
linear spring (WAMIT, Inc., 2019; Bingham, 2019). The incident waves
are assumed to be a linear superposition of the Fourier coefficients from
the measured surface elevation signal at probe 5 in the empty tank test.
The geometry is represented exactly using high-order B-splines with 54
unknowns in total. Computation was performed using 4 × 2.5 GHz cores.
Only cases involving Geometry 1 were simulated using the LPT method.

Hybrid FNPT/SPH method (in-house)

This method couples a fully Lagrangian, mesh-free, smooth particle hy-
drodynamics (SPH) solver (Zheng et al., 2014) with the FNPT solver,
QALE-FEM (Ma & Yan, 2006). The moving body boundary is sim-
ulated by using layers of dummy particles. Wave generation, and the
mesh in the FNPT domain, is as in the Hybrid FNPT/NS method. The
SPH domain is 10 m long and 1.2 m wide with ~1 million particles. Dy-
namic time-stepping is used (Co = 0.2). Laminar flow is assumed. Com-
putation was performed on 16 × 3.2 GHz cores. Only case 2BT3 (both
geometries) was simulated using this method (Zhang et al., 2019).

NEWTANK uses the FDM to solve the spatially averaged Navier-Stokes
(SANS) equations for two, incompressible fluids using a VOF scheme.
The interaction between the fluid and structure is simulated via a virtual
boundary force (VBF) method (Liu & Lin, 2009; Lin et al., 2016). Waves
are generated using an expression-based boundary condition based on
linear superposition of components derived from the theoretical wave
descriptions. Wave absorption is via an artificial damping scheme (Park
et al., 1999). The computational domain is 10 m long, 3 m wide and
4 m tall and consists of ~0.56 million cells (edge length 0.02 m-0.66 m).
Dynamic time-stepping is used (Co = 0.3). Laminar flow is assumed.
Computation was performed on 16 × 2.3 GHz cores (Cheng et al., 2019).
RESULTS & DISCUSSION

Time Series Analysis

Incident waves

In addition to time series of the heave, surge, pitch and mooring load, it was requested that participants also submit time series data for the surface elevation, at positions 1, 3, 5 and 8 (Figure 3), in an empty tank simulation of each wave case. The submissions for the intermediate steepness wave, 2BT3, at the focus position (probe 5) are shown, along with the experimental measurement, in Figure 4.

As the physical data was available for the empty tank tests, and the simulations are significantly simplified, it was anticipated that submissions (particularly those utilising similar methods) would be approximately equal in terms of their reproduction of the experimental result at the probe 5, i.e. the ‘target’ location (Figure 4). However, although there is a group that demonstrate very good reproduction, in general there is noticeably high variation in the quality of the reproduction across the submissions. Ignoring the linearised methods, which effectively have perfect reproduction at probe 5, the variation in the NS solvers clearly demonstrates a difference due to the wave generation/implementation strategy and, in some cases, there are significant discrepancies with respect to the experimental data. When viewed in frequency-space, the differences typically manifest themselves as an over-estimation of the energy density at the peak frequency (except in the case of the OpenFOAM (source-term) method which appears to under-estimate the peak, predicts a higher peak frequency and has some curious additional frequency content). At the other probe locations there is even more spread in the results (probably due to the iterative ‘tuning’ methods used by some participants concentrating only on the target, probe 5) and the LPT shows considerable discrepancies upstream, demonstrating that the propagation of the waves considered here cannot be described properly by linear theory. These observations (already) demonstrate a need for standardisation in numerical wave generation practices; it is reasonable to assume that the quality of the reproduction in the empty tank cases is strongly correlated to the reproduction in the cases with the structure present (at least for those methods that are required to simulate the propagation of the incident waves). This, also, makes judging the predictive capability of the models, in the cases with a structure, far more challenging compared to a scenario in which all models generate the incident waves to the same degree of accuracy. There is no obvious trend in the quality of the reproduction as a function of wave steepness.

Heave displacement

Figure 5 shows the heave displacement of Geometry 1’s CoM when subject to the mid-steepness wave, 2BT3. As anticipated (other than some curious exceptions attributed to additional implementation issues), the quality of the heave displacement prediction, from the NS solvers, resembles closely that of the surface elevation reproduction in Figure 4, i.e. those methods that have reproduced the waves well also reproduce the heave motion well. The linearised models (including the nonlinear Froude-Krylov method) display some discrepancies in heave displacement and, when viewed in frequency-space, noticeable additional frequency content. However, in general, the prediction of heave displacement is reasonably good across all model fidelities. This is possibly because, in these cases, heave motion may be dominated by inertia and restoring forces (i.e. hydrostatic force, weight and mooring stiffness), and hence may not be sensitive to some errors in the hydrodynamic forces. In the case of heave displacement, there is no obvious difference in the accuracy with respect to geometry. Again, there is no obvious trend in the quality of the reproduction as a function of wave steepness.
Surge displacement

Figure 6 shows the surge displacement of Geometry 1’s CoM when subject to the intermediate steepness wave, 2BT3. There is noticeably more spread in the quality of the reproduction, particularly after the main wave crest has passed, i.e. during the mean/slow ‘drift’ motion attributed to mean drag and second-order sub-harmonics (Yan and Ma, 2007; Ma and Yan, 2009). For NS methods, which included these nonlinearities, those that have reproduced the incident wave well have, in general, reproduced the surge motion well. As expected, the LPT model does not predict any drift motion as no nonlinear effects are included; the Nonlinear Froude-Krylov includes the necessary coefficients to predict the drift motion but, in these cases, tends to over-estimate this considerably (possibly due to exclusion of viscous drag corrections or assumed linear wave dispersion). One observation, with respect to the NS solvers, is that the method using overset meshing for the body motion (OpenFOAM (overset)) displays considerable discrepancies in the surge motion. As with heave, there is no obvious trend in the quality of the predictions when comparing the two geometries, however; it is possible that, when viewed in frequency-space, there is an improved capture of high-frequency surge components in the Geometry 2 case, which is unexpected. Again, there is no obvious trend in the quality of reproductions with respect to wave steepness.

Pitch angle

Figure 7 shows the pitch angle of Geometry 1 when subject to wave 2BT3. Physical measurements are plotted as a black dotted line; numerical submissions, from all participants, are shown using coloured lines. The experimentally measured data is apparently under-estimated. As noted earlier, possible inaccuracies in the specified mass properties of the structures may explain differences between the numerical predictions and the physical measurements, particularly for pitch motion. However, there is no clear convergence of the pitch natural frequency despite all numerical models specifying the same mass properties. The LPT method clearly struggles with pitch here, with the structure being excited in pitch much earlier than expected. It is suspected that this is due to the inherent nonlinearity in the incident wave and the failing of linear superposition to predict the free-surface elevation spatially. The nonlinear Froude-Krylov method works well during the wave loading but greatly over-estimates the amplitude of the pitch motion after the wave passes, i.e. greatly under-estimates the pitch damping. The pitch results offered by the NS Solver (FDM) have been omitted to an apparent post-processing issue. Again, the OpenFOAM (overset) method displays some odd behaviour and pitch motion is excited noticeably earlier than it should be (for both geometries). However, at this point it is worth noting, that the three degrees of freedom considered (heave, surge and pitch) are likely to be strongly coupled with one another in reality and so observed discrepancies in one are likely to cause (and be a cause of) discrepancies in the other two and, so, should not be considered in isolation. Again, there is no obvious trend in the predictive capability of the models as a function of wave steepness. Compared to Geometry 1, Geometry 2 displays much greater pitch damping. This is perhaps to be expected due to the flat base of Geometry 2, and associated sharp edges, but also the potential for ‘sloshing’ in the moon-pool which has been linked consistently with similar motion-damping. Qualitative, there does appear to be a reduction in the quality of the predicted pitch motion, in the case of Geometry 2, which may be evidence that the additional geometric complexity, and associated ‘internal’ fluid volume, does represent a scenario that can be used to differentiate the required numerical fidelity.
Mooring load

Unsurprisingly, in these cases, the mooring load is dominated by the vertical motion, i.e. heave. Consequently, in general, the quality of the numerical reproductions mimics that of the heave response and, therefore, the surface elevation reproduction (with the exception of the nonlinear Froude-Kylov code which has significant issues related to it’s overestimation of the surge motion). Therefore, again, there is no obvious trend in the predictive capability of the codes as a function of either the wave steepness or the geometric complexity. One concern raised, however, is that there appear to be considerable issues with predicting the rest tension in the mooring, despite this being specified in the test description.

Quantitative Analysis

In an attempt to uncover any underlying trends and provide a quantitative estimate of predictive capability, the normalised root mean squared (RMS) error in the submitted data has been calculated. As discussed in Ransley et al. (2019), an RMS is a relatively basic analysis tool that reduces the time series data to a single-number representation of the quality of the prediction. Although convenient, this obscures large amounts of (potentially valuable) information about the reproduction and can lead to bias in favour of those solutions that have good phase agreement. Furthermore, the RMS is an ‘absolute’ value that is influenced strongly by the underlying signal and can also be highly sensitive to the window of time over which it is calculated. This makes comparing RMS values across different cases difficult without ‘normalisation’. The RMS values calculated here have been normalised by the standard deviation of corresponding physical data set. It is believed that this normalisation strategy is more appropriate, than one based on a discrete maximum, as the normalisation factor considers the behaviour over the entire analysis window and, provided the RMS and standard deviation are over the same analysis window (in this case 35.3 s - 50.3 s), this normalised RMS value should demonstrate some independence from the length of window used.

Figure 8 shows the normalised RMS (NRMS) in the heave displacement, surge displacement and pitch angle versus the NRMS in the surface elevation predicted at wave probe 5 in the empty tank tests. The data have been colour-coded according to the underlying theory/method, i.e. red symbolises NS solvers, green symbolises methods based on linear potential theory, cyan symbolises hybrid methods and magenta symbolises the PIC method; filled markers represent cases involving Geometry 1 and open markers represent those involving Geometry 2; the marker sizes have been scaled according to the wave steepness, $kA$.

As anticipated from the time series data above, Figure 8a shows a clear correlation between the NRMS in the heave displacement and the NRMS in the surface elevation at probe 5 (for the methods modelling the wave propagation). In fact, for most of the methods, the trend is near linear with a one-to-one relationship, i.e. an increase in the NRMS of the predicted free-surface elevation corresponds to the same increase in the NRMS of the heave displacement. Curiously, there is a group of methods with a slightly inferior trend, i.e. the NRMS in heave increases more rapidly with the NRMS in the surface elevation, and this group contains all of the hybrid method results. Figure 8a also shows that, there appears to be a clear intercept of the data at the y-axis suggesting that even with perfect reproduction of the surface elevation a finite NRMS (of $\sim 0.1$) in heave displacement will still be observed. Perhaps this suggests that, if all the methods (excluding those based on linear theory) reproduced the waves equally well, they would all return a NRMS in the heave displacement of $\sim 0.1$, i.e. they all have the same predictive capability for heave displacement (in the cases considered here) and the $\sim 0.1$ NRMS could represent either the present limitation of modern numerical modelling capabilities or a systematic error in the description of the physical experiment. It can also be seen that, for many of the methods, the NRMS

Fig. 8 Normalise RMS error (w.r.t. the experimental data) in the heave displacement (a), surge displacement (b) and pitch angle (c) vs. NRMS error in the surface elevation at wave probe 5 (during empty tank tests). Filled markers represent Geometry 1; open markers represent Geometry 2. Marker sized scaled by wave steepness, $kA$. 
in heave increases with the wave steepness suggesting that the predictive capability of the codes is a function of wave steepness. There is no obvious trend with respect to the two geometries.

From Figures 8b and 8c it can be seen that, as observed in the time series data, the NRMS in both surge displacement and pitch angle does not follow such a clear trend with respect to the NRMS in surface elevation. In general, greater NRMS in the incident wave does lead to greater NRMS in both the surge and pitch motion, however; the scatter in the results suggests there are distinct differences in the capabilities of the individual methods (most likely due to inconsistencies in the quality of the implementation). However, it is worth noting that the analysis method used here (normalised RMS) may be better suited to a comparison between surface elevation and heave motion, particularly if the heave is dominated by buoyancy, and; alternative quantitative measures of reproduction quality may expose similar trends for the other degrees of freedom. For example, one might expect the surge motion to be dominated by drag forces and so the reproduction might be more strongly linked to the reproduction of the wave velocities, rather than the wave amplitudes.

Figure 9 shows the normalised RMS in the heave displacement versus the CPU effort required to generated the solutions. Here, the CPU effort has been defined as the execution time of the numerical solver, multiplied by the number of cores used in the processing, divided by both the simulated time and the processor speed in GHz. It should be noted that participants were not asked to minimise the CPU effort as part of this study and any additional ‘calibration’ effort has not been included here (including the effort required to calculate the hydrodynamic coefficients in the linearised methods). Furthermore, the details of the specific hardware used have not been considered here and this should be remembered when interpreting the results. As is to be expected, the Navier Stokes solvers require many orders of magnitude more CPU resource compared to the linearised methods and, in many cases, there is no significant improvement in the prediction to warrant the additional computing cost (for the cases investigated here). The NS solvers with the lowest NRMS (including the PIC method) do also have the highest CPU effort. The NS solvers with the lowest CPU effort also have the widest range in NRMS values and either have a very low number of mesh cells (NS Solver (FDM)) or utilise a fixed timestep (OpenFOAM (source-term) and NS Solver (FVM)(in-house)). In contrast to Ransley et al. 2019, the hybrid methods do now demonstrate a potential improvement in the required CPU effort (when compared to the better NS solvers).

**Fig. 9** Normalise RMS error (w.r.t. the experimental data) in the heave displacement vs. CPU effort. Filled markers represent Geometry 1; open markers represent Geometry 2. Marker sized scaled by wave steepness, kA. For key please refer to Figure 8c.

**CONCLUSIONS**

The CCP-WSI Blind Test Series 3 consists of a series of test cases involving focused wave interactions with two separate floating structures - a hemispherical-bottomed buoy and a cylinder with moonpool; the incident waves are varied in steepness but remained unbroken; the structures are taut-moored with a single linear spring mooring. The aims of the study are to assess the numerical codes currently in use, provide a better understanding of the required model fidelity in WSI simulations, and help to inform the development of future numerical modelling standards, to encourage the practical application of these tools by industry.

Ten different codes are used in the test, including a range of underlying complexities from LPT to NS solvers, mesh-based and particle methods, hybrid/coupled methods, and both in-house and open-source codes. No fully nonlinear potential flow solutions are available so a gap exists in the model fidelities considered. In general, as may be expected, the prediction of heave displacement, which is commonly considered to be a linear response, is reasonably good across all models. There is, however, some evidence that NS solvers provide more accurate results for surge and pitch motion, suggesting these represent a level of complexity that is appropriate to differentiate the predictive capability of different fidelity codes, i.e. include nonlinear effects. In contrast to Ransley et al. (2019), there does appear to be a gradual reduction in the predictive capability as a function of wave steepness but it is still believed that test cases need to cover a step-change in physical phenomena, e.g. unbroken - broken wave cases, to make a clear distinction between the predictive capability of numerical models. In the cases considered here, including a moonpool does not appear to represent sufficient additional complexity to make a distinction, however, it should be noted that, the hydrodynamic behaviour of the internal water volume is likely to depend strongly on the incident wave frequency and other frequencies, closer to the internal resonance, may give different results. For the NS solvers, it is shown that the quality of the predicted motion of the structures depends strongly on the quality of the surface elevation reproduction in the empty tank case, and; in the context of heave, it appears that all methods are equally good at predicting the motion given the same quality of incident wave reproduction. The relationships in the other degrees of freedom are less obvious and are likely to be more sensitive to discrepancies in the hydrodynamic predictions, compared to heave motion. As discussed in Ransley et al. (2019), further work is required to establish more appropriate analysis strategies for these degrees of freedom but, in order to draw clear conclusions, it may be important to compare numerical solutions at the level of hydrodynamics forces, or the pressure, instead of ‘integrated quantities’ such as wave-induced motions.

Finally, a key observation is that, there is considerable scatter in the predictions made by ‘similar’ NS codes, largely attributed to inconsistencies in the model implementation, and this highlights a large risk to end-users and the need for standardised practice in numerical modelling (including the derivation of model uncertainties) for both industrial usage and future comparative studies.

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REFERENCES


