

2021-09-10

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Stashchuk, N

<http://hdl.handle.net/10026.1/17785>

10.3389/fmars.2021.735358

Frontiers in Marine Science

Frontiers Media SA

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Internal Wave Dynamics Over Isolated Seamount and Its Influence on Coral Larvae Dispersion

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Specialty section:

This article was submitted to
Physical Oceanography,
a section of the journal
Frontiers in Marine Science

Received: 02 July 2021

Accepted: 20 August 2021

Published: 10 September 2021

Citation:

Stashchuk N and Vlasenko V (2021)
Internal Wave Dynamics Over Isolated
Seamount and Its Influence on Coral
Larvae Dispersion.
Front. Mar. Sci. 8:735358.
doi: 10.3389/fmars.2021.735358

The internal wave dynamics over Rosemary Bank Seamount (RBS), North Atlantic, were investigated using the Massachusetts Institute of Technology general circulation model. The model was forced by M2-tidal body force. The model results are validated against the *in-situ* data collected during the 136th cruise of the RRS “James Cook” in June 2016. The observations and the modeling experiments have shown two-wave processes developed independently in the subsurface and bottom layers. Being super-critical topography for the semi-diurnal internal tides, RBS does not reveal any evidence of tidal beams. It was found that below 800-m depth, the tidal flow generates bottom trapped sub-inertial internal waves propagated around RBS. The tidal flow interacting with a cluster of volcanic origin tall bottom cones generates short-scale internal waves located in 100 m thick seasonal pycnocline. A weakly stratified layer separates the internal waves generated in two waveguides. Parameters of short-scale sub-surface internal waves are sensitive to the season stratification. It is unlikely they can be observed in the winter season from November to March when seasonal pycnocline is not formed. The deep-water coral larvae dispersion is mainly controlled by bottom trapped tidally generated internal waves in the winter season. A Lagrangian-type passive particle tracking model is used to reproduce the transport of generic deep-sea water invertebrate species.

Keywords: internal tides, internal lee waves, bottom trapped internal waves, numerical modeling, Rosemary Bank Seamount, deep water coral, larvae dispersion

1. INTRODUCTION

The life of deep-water corals, their nutrition, sustainability, and survival in the conditions of climate change is in the focus of many studies (e.g., de Mol et al., 2002; van Weering et al., 2003; Roberts et al., 2006). In a deep water environment below 500 m the ocean dynamics are usually not sensitive to the processes developing in the surface layer, e.g., wind-driven circulation or surface currents. Still, they can be affected by internal waves and tidally induced residual water transport (White and Dorschel, 2010). As it was reported by Henry et al. (2014) and Davison et al. (2019), the primary source for food and oxygen supply to these deep-water communities usually has a tidal origin.

The mechanism of water mixing and deep-water coral feeding is related to tidal activity. Tidal currents streamlining bumpy bottom topography provide vertical fluxes of nutrients required for the initial biological production. They generate internal waves in the vertically stratified ocean and produce water mixing, which facilitates the dispersion of chemicals (Henry et al., 2014). The importance of internal wave mixing and internal tides for the sustainability of cold-water

coral communities is well-recognized. It is underpinned by many observations and theoretical studies, specifically conducted for underwater banks. For instance, Mohn and White (2010) in their modeling paper has shown how the tidal activity over the oceanic bank can affect the sea environment, specifically the deep-water corals' communities. The principal conclusion formulated in this paper is that the tidal motions in the areas of underwater seamounts have not just local but far-field effects on the deep-water coral dispersion. The investigation of the tidal actions is the topic of the present paper as well, although we consider not an idealized symmetrical oceanic bank but the natural area in the North Atlantic, which includes Rosemary Bank Seamount (RBS).

One of the recent publications based on observations, Soetaert et al. (2016), sheds light on the way how the organic matter is supplied to the deep-water corals. This particular study concerns the Rockall Bank area, which is close to RBS considered in the present paper. In general, all local studies conducted in the North Atlantic and referred here help understand the link between deep-water coral communities, their nutrition, and surface water productivity. The latter is a generic problem for many areas of the Global Ocean. The authors appreciate the significant role of internal tides and internal wave mixing in organic matter supply to the deep-water corals.

Significant progress in understanding the cold-water coral occurrence and the role of tidally induced water activity in the North Atlantic was reported by van Harren et al. (2014). The study of Mohn et al. (2014) based on high-resolution numerical modeling using the ROMS model and highlighted many exciting effects introduced by tides generated over underwater banks, specifically the role of trapped internal waves, radiated internals, and internal jumps. The results reported in the present paper are based on a similar approach of a combination of the observational data set and high-resolution modeling applied to a different area, Rosemary Bank Seamount. Our findings are in line with the conclusions of the paper by Cyr et al. (2016) who acknowledged a strong influence of the baroclinic tidal hydrodynamics on the sustainability of the coral communities in the Rockall Bank area.

In the present paper, we make another attempt to look at the deep-water coral life based on the available *in-situ* collected data and the results of high-resolution modeling. The North Atlantic area considered here is Rosemary Bank Seamount, close to the Rockall Bank reported in the papers mentioned above. The observational data collected during the 136th cruise of the RRS "James Cook" (hereafter JC136) to the North-East Atlantic in May–June 2016. The coral samples were collected from the flanks of Anton Dohrn Seamount, Rockall Bank, George Bligh Seamount, Rosemary Bank Seamount, and slopes of the Wyville Thomson Ridge, **Figure 1A**, using the remotely operating vehicle (ROV) ISIS 5000.

The biological campaign was accompanied by oceanographic measurements that included a series of CTD (Conductivity, Temperature, Depth) stations and the deployment of two moorings in the area of Anton Dohrn Seamount. The analysis of the generation of internal waves by tides in areas of Anton Dohrn Seamount and the Wyville Thomson Ridge was reported

in Vlasenko et al. (2018), Stashchuk et al. (2018), and Vlasenko and Stashchuk (2018).

The focus of the present paper is on Rosemary Bank Seamount. The tidal activity in the area is studied based on *in-situ* data and numerical modeling considering the semidiurnal M_2 -tide (Egbert and Erofeeva, 2002) as the predominant tidal constituent (the discharge of the M_2 tidal constituent is seven times greater than any other tidal harmonics). Another objective of the modeling efforts was defining the role of tidally generated dynamical processes, developing in the area around RBS in the dispersion of larvae released by deep water corals.

The paper is organized as follows. The observational data set that motivated the study and helped formulate the hypothesis is discussed in section 2. The model parameters and their setting are described in section 3. Internal wave generation over RBS with the detailed discussion of two wave-guide dynamics is the objective of section 4. In section 5, the analysis of model-predicted larvae tracks forced by tidal currents is presented. The paper finishes with a discussion and main conclusions.

2. OBSERVATIONS AND HYPOTHESIS

The observational data set for RBS includes temperature, salinity, and density profiles recorded at six CTD stations, **Figure 1B**. The buoyancy frequency profile, $N^2(z) = -g/\rho(\partial\rho/\partial z)$ (g is the acceleration due to gravity, and ρ is the water density), **Figure 1C**, is based on the density data averaged at all stations. It reveals the presence of two pycnoclines: (i) a very sharp seasonal pycnocline in the surface layer with its maximum at a depth of 50 m, and (ii) a weaker main one at the 1,200-m depth, that stretched from 800 to 1500 m.

A Lowered Acoustic Doppler Current Profiler (LADCP) was mounted on a CTD frame for recording instantaneous horizontal velocities. The LADCP data were processed using the method described by Visbeck (2002). **Figure 2** shows that collected velocity profiles reveal an intensification of bottom currents below 800 m at all deep-water stations (except shallow water station 32). It was assumed that such an intensification of bottom currents could be caused by internal waves generated by tides at RBS: (i) tidal beam by internal waves and/or (ii) bottom trapped sub-inertial internal waves.

The condition for tidal beam generation is controlled by a relative steepness of the bottom topography γ :

$$\gamma = \frac{|\nabla[H(x, y)]|}{\alpha[H(x, y)]},$$

which is a ratio of the topography steepness $|\nabla[H(x, y)]|$ at a point (x, y) (x and y are horizontal coordinates and H is the water depth) to the inclination of tidal beam α at this point:

$$\alpha[H(x, y)] = \frac{\omega^2 - f^2}{N^2[H(x, y)] - \omega^2}. \quad (1)$$

Here f is the Coriolis parameter, ω is the tidal frequency, and N is the buoyancy frequency at the bottom point $H(x, y)$. The internal tidal velocity forms the tidal beams in areas where $\gamma \sim 1$ (critical

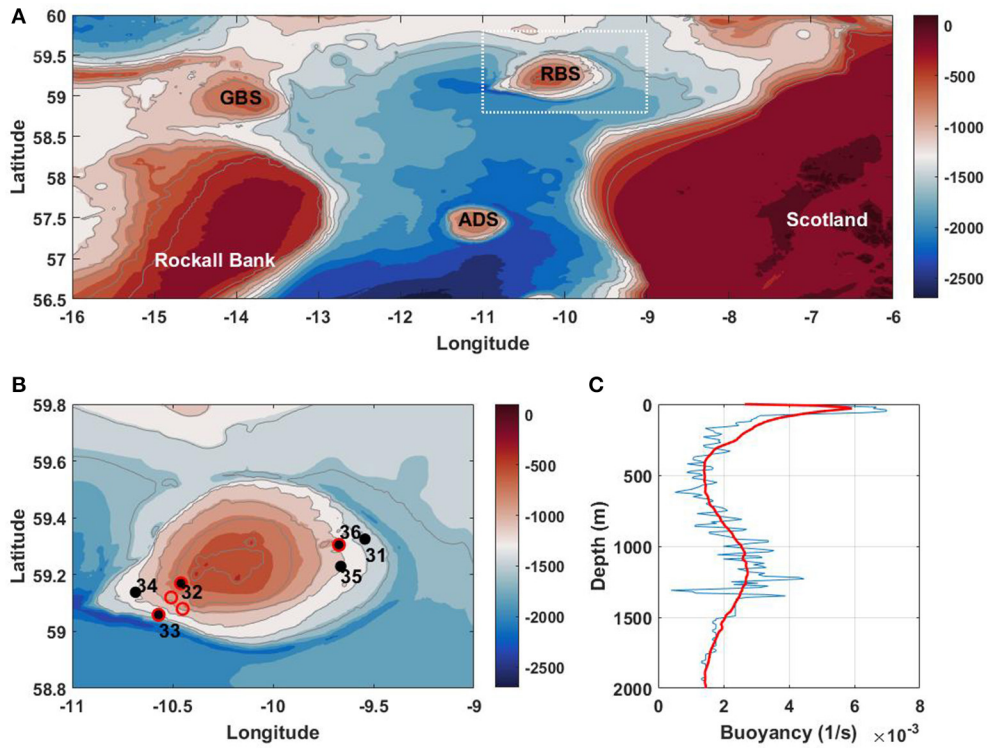


FIGURE 1 | (A) Overview map showing the main topographic features in the NE Atlantic: GBS, George Bligh Seamount; RBS, Rosemary Bank Seamount; ADS, Anton Dohrn Seamount. Zoom of the dashed rectangle is shown in panel (B) with the plan view of the JC136 CTD stations at Rosemary Bank Seamount (filled black circles) and ROV missions (red circles). (C) Buoyancy frequency averaged over the data collected at the CTD stations.

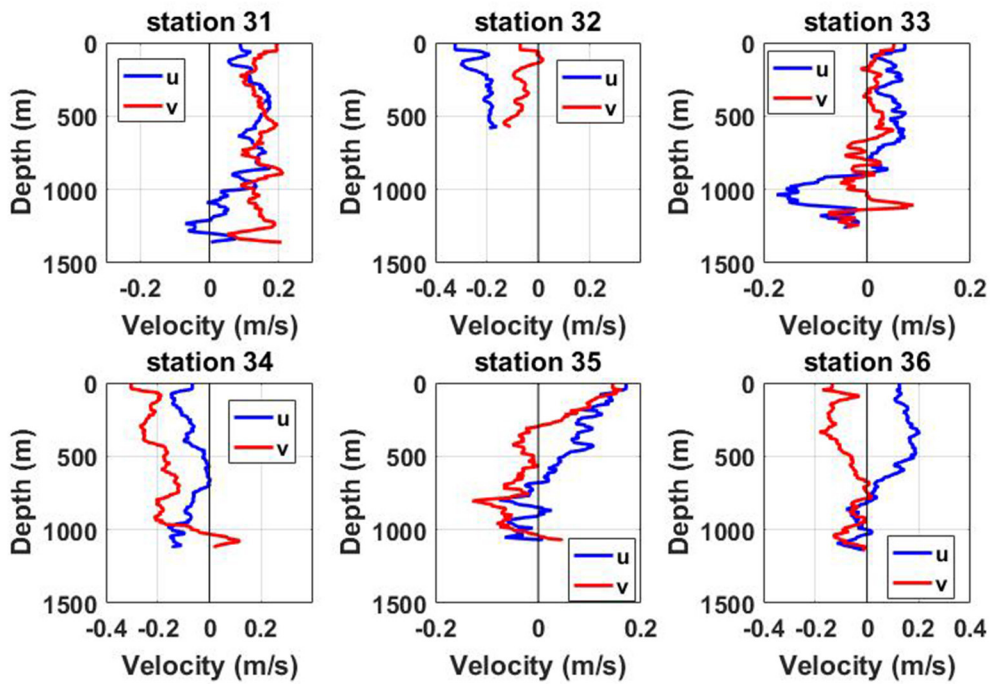


FIGURE 2 | Instant vertical profiles of eastward (*u*) and northward (*v*) velocities recorded by LADCP at CTD stations.

case) or $\gamma > 1$ (supercritical conditions). The beams present relatively narrow stripes with a considerable concentration of baroclinic energy (Bell, 1975).

Another possibility of bottom current intensification in the considered area could be sub-inertial bottom trapped internal waves. The theory of this type of motion was developed and discussed in many papers (e.g., Wang and Mooers, 1976; LeBlond and Mysak, 1978). Observational evidence and theoretical interpretation of such internal wave dynamics were reported recently by the authors for the Malin Shelf (Stashchuk and Vlasenko, 2017). The focus of the present paper is on the RBS area. The analysis is based on *in-situ* collected data set and model experiments that show a bottom current intensification below 1,000 m depth.

Our analysis relies on the results of previous studies that considered similar problems of bottom trapped internal waves generated by tides. The tidal flow interacting with seamounts generates internal waves radiated from the bottom obstruction in all directions. Linear theory predicts that internal waves are radiated from the topography when $\omega > f$ but are trapped in the place of the generation when $\omega < f$. Note that as Huthnance (1978) and Dale et al. (2001) found, the generation mechanism is not so sensitive to the Earth rotation as the linear theory predicts in the case when the tidal frequency ω is close to the Coriolis parameter (inertial frequency f). There is no sharp jump from near-inertial to sub-inertial regimes of internal tides generation. As was reported by Huthnance (1978) and Dale et al. (2001), the generated over two-dimensional slopes internal waves at the latitude close to the critical are “nearly trapped by topography.” They considered a slightly super-inertial ($\omega/f=0.9$), slightly sub-inertial ($\omega/f=1.1$), and strongly sub-inertial ($\omega/f=1.5$) cases. It was found that freely radiated internal waves can exist only when $\omega/f > 1$, although the bottom trapped waves propagated along the slope are allowed in all considered bands.

Note that RBS is located at 59°N latitude. According to Dale et al. (2001) classification, the RBS area falls into a slightly sub-inertial frequency band with the tidal frequency $\omega/f=1.1$. As predicted, the sub-inertial bottom trapped internal waves are quite possible there. Thus, the strong, deep-water currents recorded in the JC136th cruise can be associated with the generation of internal tidal beams (as it was in the case of Anton Dohrn Seamount, Vlasenko et al., 2018) or/and bottom trapped sub-inertial internal waves. Clarification of which of these mechanisms caused the observed bottom currents was the motivation of the present study.

3. THE MODEL

Modeling the tidal motions in the RBS area was conducted using the Massachusetts Institute of Technology general circulation model (MITgcm) (Marshall et al., 1997) in its fully nonlinear and nonhydrostatic three-dimensional version. We used the Cartesian coordinate system with x -axis directed to the east and y -axis directed to the north and vertical z axis ($z = 0$ at the free surface). The topography presented in **Figure 1B** was approximated by 815×698 model grid with a horizontal

resolution of 115.75 m in both zonal and meridional directions. Extra 128 grid steps were added to the northern, southern, western, and eastern boundaries, transforming it into a $1,071 \times 954$ grid. In these lateral areas, the grid resolution gradually changes from a 115.75 m spatial step in its central part to 2×10^8 m at the boundary. Such a telescopic increase of the horizontal steps toward the periphery eliminated the reflection of the waves from the model boundaries for at least 12 tidal cycles. In the vertical direction, the water depth was restricted by a 2,000-m isobath. The vertical model resolution was $\Delta z = 10$ m.

The M2-tide was activated in the model using a body force introduced into the right-hand side of the momentum balance equations. The details of the tidal body force method and its justification are described in Vlasenko and Stashchuk (2021). The tides were set in the model using the data from the inverse tidal model TPXO 8.1 (Egbert and Erofeeva, 2002).

The vertical turbulent closure for the coefficients of viscosity A^v and diffusivity K^v was provided by the Richardson number dependent parameterization, Pacanowski and Philander (1981), (PP81 scheme):

$$A^v = \frac{A_0^v}{(1 + a\text{Ri})^n} + A_b^v,$$

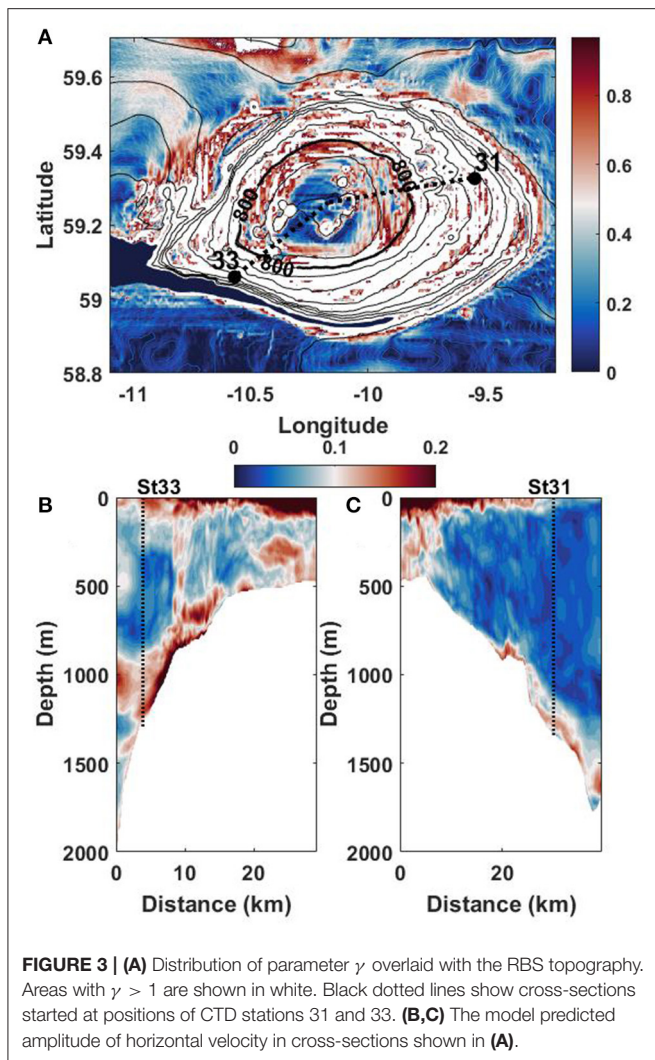
$$K^v = \frac{A^v}{(1 + a\text{Ri})} + K_b^v. \quad (2)$$

Here Ri is the Richardson number, $\text{Ri} = N^2(z)/(u_z^2 + v_z^2)$, and, u and v are the zonal and meridional components of horizontal velocity; $A_b^v = 10^{-5} \text{ m}^2 \text{ s}^{-1}$ and $K_b^v = 10^{-5} \text{ m}^2 \text{ s}^{-1}$ are the background viscosity/diffusion parameters, respectively, $A_0^v = 1.5 \cdot 10^{-2} \text{ m}^2 \text{ s}^{-1}$, $a=5$ and $n=1$ are the adjustable parameters. The PP81 scheme increases the coefficients A^v and K^v in the areas with the small Richardson numbers, which dumps shear instabilities and stabilizes inverse water stratification produced by breaking internal waves.

All model runs were conducted with constant horizontal viscosity A^h and diffusivity K^h coefficients at the level of $0.5 \text{ m}^2 \text{ s}^{-1}$. Technically, the model produced 1-h outputs for velocities and thermohaline data. In addition to that, the model delivered 1-min outputs of the vertical temperature and velocities sampling at the position of six CTD-LADCP stations, **Figure 1B**.

The great performance of the MITgcm on replication of internal tides was already checked and reported in many papers (e.g., Vlasenko et al., 2013, 2014, 2016, 2018; Stashchuk et al., 2014, 2017, 2018; Stashchuk and Vlasenko, 2017). These publications have shown the consistency of the observational data sets and the modeling outputs. On a quantitative level, the correlation coefficient between the MITgcm model predictions and observations was calculated and reported in Vlasenko et al. (2014). It was found that the correlation coefficient r between theoretical and observational velocity time series was at the level of 0.7, which is great for the model predictions (for the details, see the **Supplementary Material**).

Another quantitative measure of the consistency of the modeling results with the observational data sets is the index of agreement d introduced by Willmott (1981, 1982) (**Supplementary Material**). As we found in our modeling



experiments, the extent to which the model output is error-free is quite good. In general, the index of agreement d can vary from 0 (absolute disagreement) to 1 (perfect coincidence). The value of d estimated here was 0.7, which shows a good agreement between the observations and the model results.

4. TIDAL WAVE DYNAMICS

The internal wave dynamics in underwater seamount areas are sensitive to the intensity of tidal flow, water stratification, background mixing, and configuration of the bottom topography. The latter controls the spatial variability and spectral properties of the generated waves.

The summit of RBS above 800 m isobath (thick black line in **Figure 3A**) is relatively flat. Beneath this depth, the bottom is supercritical in terms of internal tide generation, i.e., the parameter $\gamma > 1$ (white color in **Figure 3A**). In this case, one of the expected scenarios would be a generation of internal wave beams at the RBS flanks, which radiate the tidal energy to the surface, Vlasenko et al. (2016, 2018). If this is the case, the beams

should dominate in the model-predicted baroclinic velocity output. They can be evident after removing the barotropic tidal signal. However, closer inspection of the amplitudes of horizontal velocities along the transects crossing the positions of stations 31 and 33, **Figure 3**, does not show any sign of strong tidal beams over the RBS periphery. The model-predicted velocity amplitudes reveal two areas of intense baroclinic tidal signal—in the surface 100 m layer, and below 800-m of depth. As modeling results show, these two wave structures, i.e., (i) surface located internal waves and (ii) bottom trapped waves, develop independently without any apparent influence on each other. Such a structure of wave fields developed independently can be explained in terms of two waveguides dynamics. **Figure 1C** shows the presence of two pycnoclines, a thin surface 100 m stratified layer (seasonal pycnocline), and thick, deep stratified layer located between 800 and 1,500 m depth. Weakly stratified intermediate water separates two stratified layers, surface seasonal pycnocline and deep main pycnocline. This type of stratification can create conditions for two waveguide internal wave dynamics.

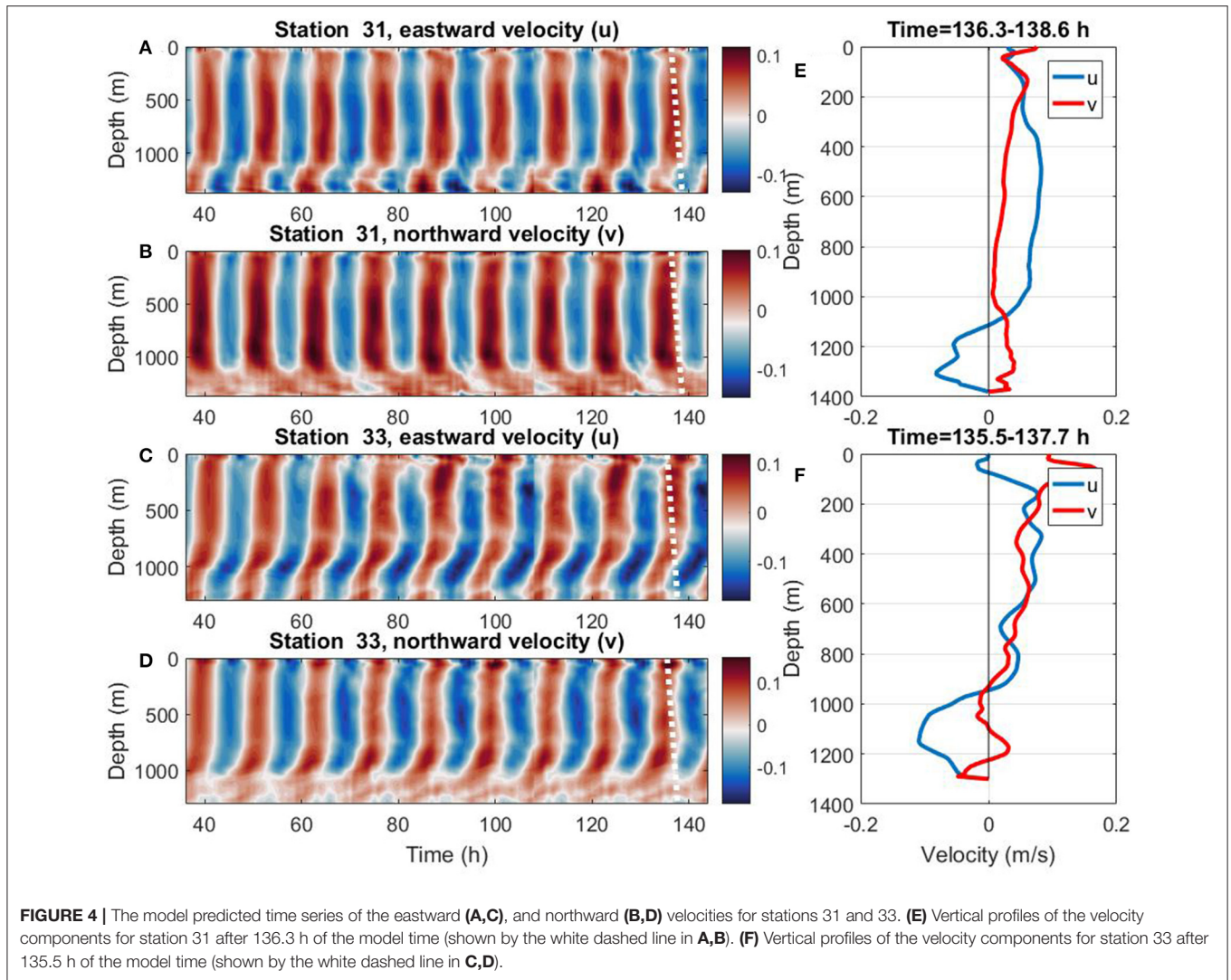
The model-predicted time series of eastward and northward velocities for stations 31 and 33 were considered to check the idea of two independent waveguides. **Figures 4A,B** present these data for station 31, and **Figures 4C,D** for station 33. The model output supports the hypothesis of two internal waveguides. They are separated by the layer with a strong barotropic tidal signal which does not reveal any baroclinic activity (constant velocity between 100 and 1,100 m depth). The velocity structure in this layer is nearly the same through the whole water column with sine-type periodicity in time. Note that thin surface 100- and 250-m thick bottom layers demonstrate quite a different wave activity. Horizontal motions in these layers are not in phase with the principal part of the water column (this is obvious in all velocity series of **Figure 4**).

Similar sampling was arranged in numerical experiments to compare the model predictions with the observational LADCP time series. **Figure 4F** (station 31) and **Figure 4D** (station 33) present instant vertical profiles of horizontal velocities at one particular moment of time depicted in **Figures 4A–D** by white dashed lines. These profiles show the consistency of the observational records for stations 31 and 33, with the model output, **Figure 2**. The velocity profiles at all CTD-LADCP stations, **Figure 2**, can be treated in terms of the formulated hypothesis of two internal waveguides separated by a thick intermediate layer. (Some extra Figures for four other CTD stations are shown in the **Supplementary Material Document**.)

The principal conclusion from the comparative analysis of the model outputs and the *in-situ* collected data can be formulated as follows: the intensification of the bottom located horizontal currents below 800 m depth is not associated with the tidal beams but has a different origin. One of the possible mechanisms is bottom trapped internal waves which are discussed below.

4.1. Bottom Trapped Sub-inertial Internal Waves

The intensification of bottom currents over RBS, **Figures 2, 3**, could be generated by bottom trapped internal waves. The theoretical background of such types of motions was provided by Huthnance (1978) who developed an analytical solution



for trapped internal waves. This study was completed later by Dale et al. (2001) who provided some numerical evidence explaining the properties of the bottom-trapped internal waves at the transition from sub-inertial to super-inertial regimes of generation. Here we present a brief extract from the theory which is relevant to the RBS area.

Consider a periodical bottom trapped internal wave $\exp[i(ky + \omega t)]$ propagated in a stratified fluid with the buoyancy frequency $N(z)$ along a two-dimensional topography $H(x)$. Here x and y are referred to as horizontal $0x$ and $0y$ axis, respectively, z is the vertical coordinate calculated from the surface, k is the wavenumber, ω is the wave frequency, and t is time. In terms of pressure, $p(x, y, z, t) = P(x, z) \exp[i(ky + \omega t)]$, internal wave motions are described by the following equation (Huthnance, 1978):

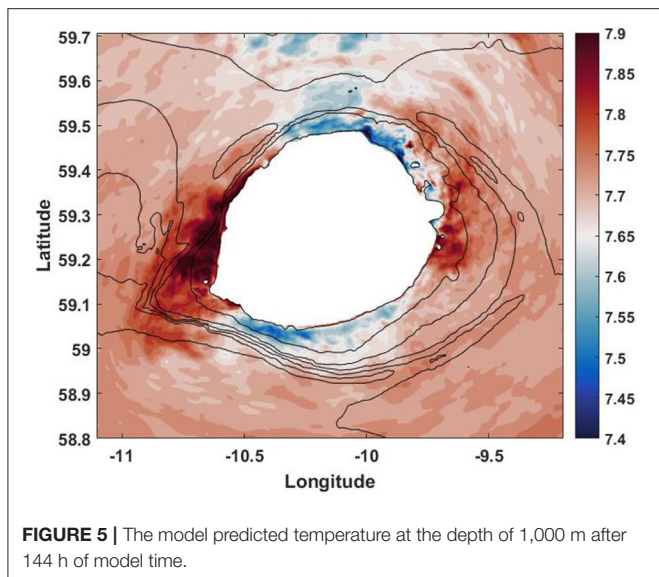
$$\frac{\partial^2 P}{\partial x^2} + \frac{(1 - \sigma^2)}{S} \frac{\partial}{\partial z} \left(\frac{1}{N^2} \frac{\partial P}{\partial z} \right) - l^2 P = 0. \tag{3}$$

Here $l = kL$, L is the length scale (width) of the topography, $\sigma = \omega/f$, and f is the Coriolis parameter. A non-dimensional parameter $S = (NH_m/fL)^2$ is the Burger number, in which H_m is the maximum depth. The Burger number shows the relative contributions of rotation and stratification to the wave process.

The boundary conditions for the problem are:

$$\begin{aligned} \frac{dH}{dx} \left(\frac{\partial P}{\partial x} + \frac{l}{\sigma} P \right) + \frac{1 - \sigma^2}{SN^2} \frac{\partial P}{\partial z} &= 0 \text{ at } z = -H(x), \\ \frac{\partial P}{\partial z} &= 0 \text{ at } z = 0, \\ P &\rightarrow 0, \text{ at } x \rightarrow \infty, \\ kP - \sigma \frac{\partial P}{\partial x} &= 0 \text{ at } x = 0. \end{aligned} \tag{4}$$

The wavelength of the model predicted wave can be estimated from Figure 5 as ~ 27 km. For such scale topographically trapped internal waves with the wavelength in the range between 10 and



30 km (Huthnance, 1978), the solution of (3)–(4) reads:

$$P(x, z) = H_m(\beta(x)) \exp \left[-\frac{\beta^2(x)}{2} \right] \exp \left[-k \frac{z + H(x)}{\sqrt{\phi(z) + \left(\frac{dH}{dx} \right)^2}} \right], \tag{5}$$

where H_m is the Hermite function of the m -th order,

$$\beta(x) = (x - x_0) \frac{N_{\max} H_0}{f} \left[\frac{\left(\frac{dH}{dx} \right)^2 \frac{d^2 \phi}{dz^2}}{2\phi(z)} - \frac{d^3 H}{dx^3} \right]_{(x_0, z_0)},$$

$$\phi(z) = \frac{(f^2 - \omega^2)}{N^2(z)} \left(\frac{L}{H_0} \right)^2.$$

Here (x_0, z_0) are the coordinates of the sea bed point where the product $N(z) \frac{dH(x)}{dx}$ has maximum value, and $H_0 = H(x_0, z_0)$. For the bottom profile under consideration (water depth deeper 500 m), the maximum of the buoyancy frequency N_{\max} is located at a depth of the main pycnocline (below 1,000 m depth, see **Figure 1C**) where the core of the bottom trapped internal wave is expected.

Note that the analytical solution presented above was developed for a two-dimensional topography. It can also be applied for the qualitative analysis of the bottom trapped waves considered in our case. In doing so, the solution was replicated for four transects shown in **Figure 6E**. **Figures 6A–D** demonstrate the analytical results for each transect separately. The analytical solution shows that the maximum of horizontal velocity in all positions is located below 1,000-m depth, **Figures 6A–D**. This theoretical result is consistent with **Figure 2** where *in-situ*

recorded data reveal the great intensity of horizontal velocities at the bottom.

The power spectra calculated using a 144-h model predicted time series of horizontal velocity (the sampling interval was equal to 1 min) also reveal the maximum for bottom-located baroclinic tidal motions in the position of all CTD stations, **Figure 7**. The data set contains only the internal wave signal extracted after the removal of barotropic velocity. **Figure 7** illustrates the predominance of the semidiurnal tidal signal. Note that 6- and 3-h harmonics are also evident in all graphs. Their peaks are comparable to the semidiurnal signal or even higher in the energy level (station 31), which testifies the strong non-linearity of the internal wave process. Such waves will increase the mixing process that can contribute to better larvae dispersion (van Harren et al., 2014; Cyr et al., 2016). A general tendency of all graphs is that the energy level at the bottom and in the surface layer (red and blue lines in **Figure 7**, respectively) substantially exceeds a similar level calculated for the mid-depth segments (green-yellow colors). This fact confirms the hypothesis of two internal waveguides separated by a less active intermediate layer.

4.2. Waves in the Surface Layer

The summit of RBS has a group of parasitic volcanic cones, **Figure 8A**. Water depth at the highest cone is about 300 m (Howe et al., 2006). The interaction of tidal currents with cones can generate internal lee waves in sharp seasonal pycnocline. If this statement is correct, the phase speed c of internal waves in the area of volcanic cones should be comparable or lower than the maximum of tidal velocity U . In other words, the Froude number $Fr = U/c$ should be close or exceed one. Below we estimate the maximum of the Froude number.

The periodic tidal currents, together with tidally induced residual currents, control the dynamical regime around RBS. According to TPXO8.1 model predictions, tidal velocities above the RBS summit can reach 0.35 m s^{-1} (see tidal ellipses in **Figure 8B**). The residual currents calculated using long-term velocity time series show the maximum value of 0.11 m s^{-1} , **Figure 8C**. Superposition of both can give 0.46 m s^{-1} maximum value of the velocity U at some moments of tidal phase.

The phase speed of short-scale internal waves c was found from the boundary value problem (Benny, 1966):

$$\begin{aligned} w_{zz} + \frac{N^2(z)}{c^2} w &= 0, \\ w(-H) = w(0) &= 0. \end{aligned} \tag{6}$$

Here w is the vertical velocity. Solution of (6) was found by shooting method, that gave the first eigenvalue $c = 0.36 \text{ m s}^{-1}$. The estimation of the Froude number shows that it slightly exceeds one in the area of the cones, i.e., $Fr > 1$, **Figure 8D**. Thus, the generation of internal lee waves at the cones explains the presence of short-scale internal waves over RBS, **Figure 3**. The area occupied by these groups of short waves above RBS over one tidal period is shown in **Figure 9A**. This pattern presents a superposition of hourly recorded amplitudes of horizontal

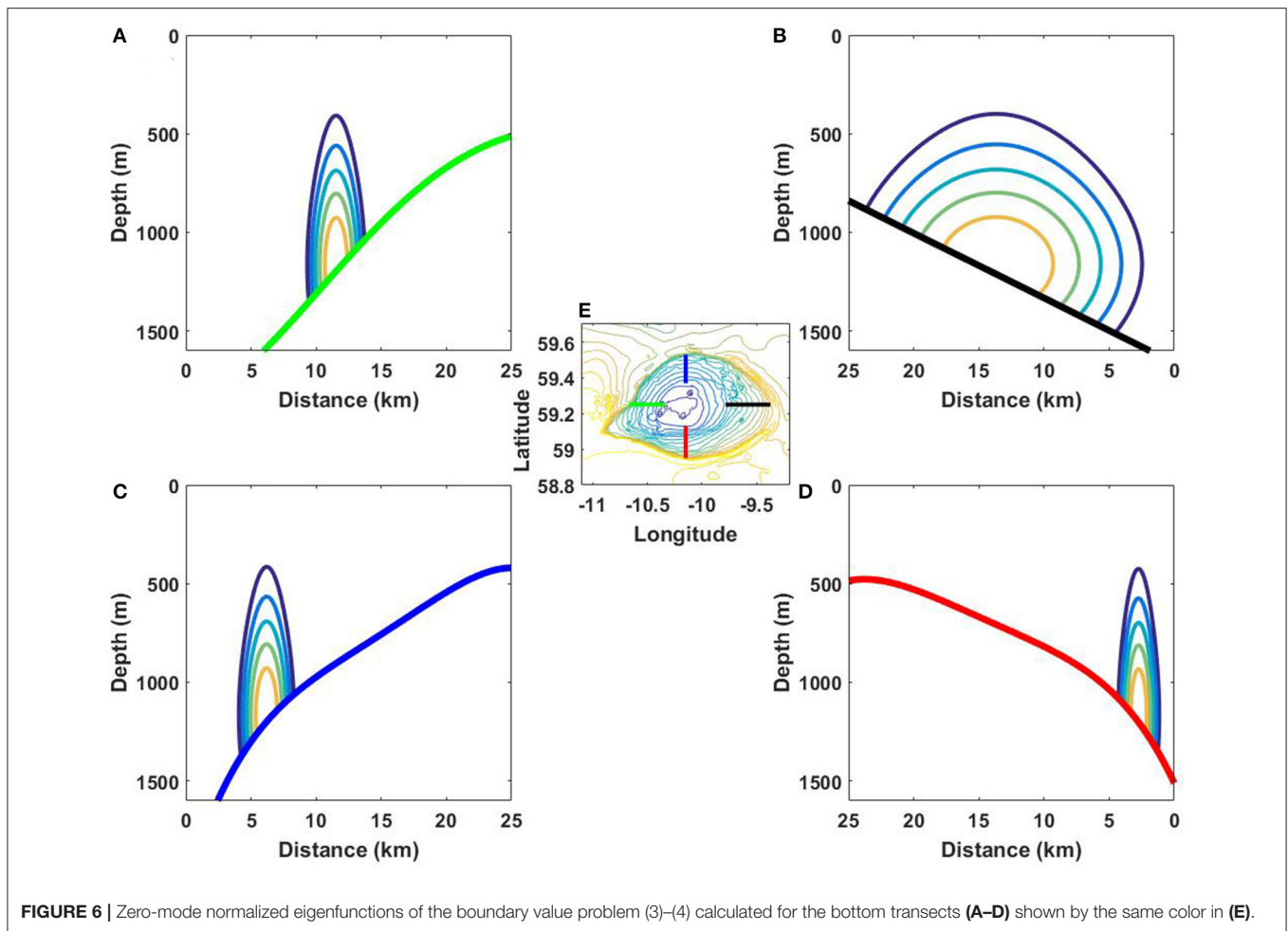


FIGURE 6 | Zero-mode normalized eigenfunctions of the boundary value problem (3)–(4) calculated for the bottom transects (A–D) shown by the same color in (E).

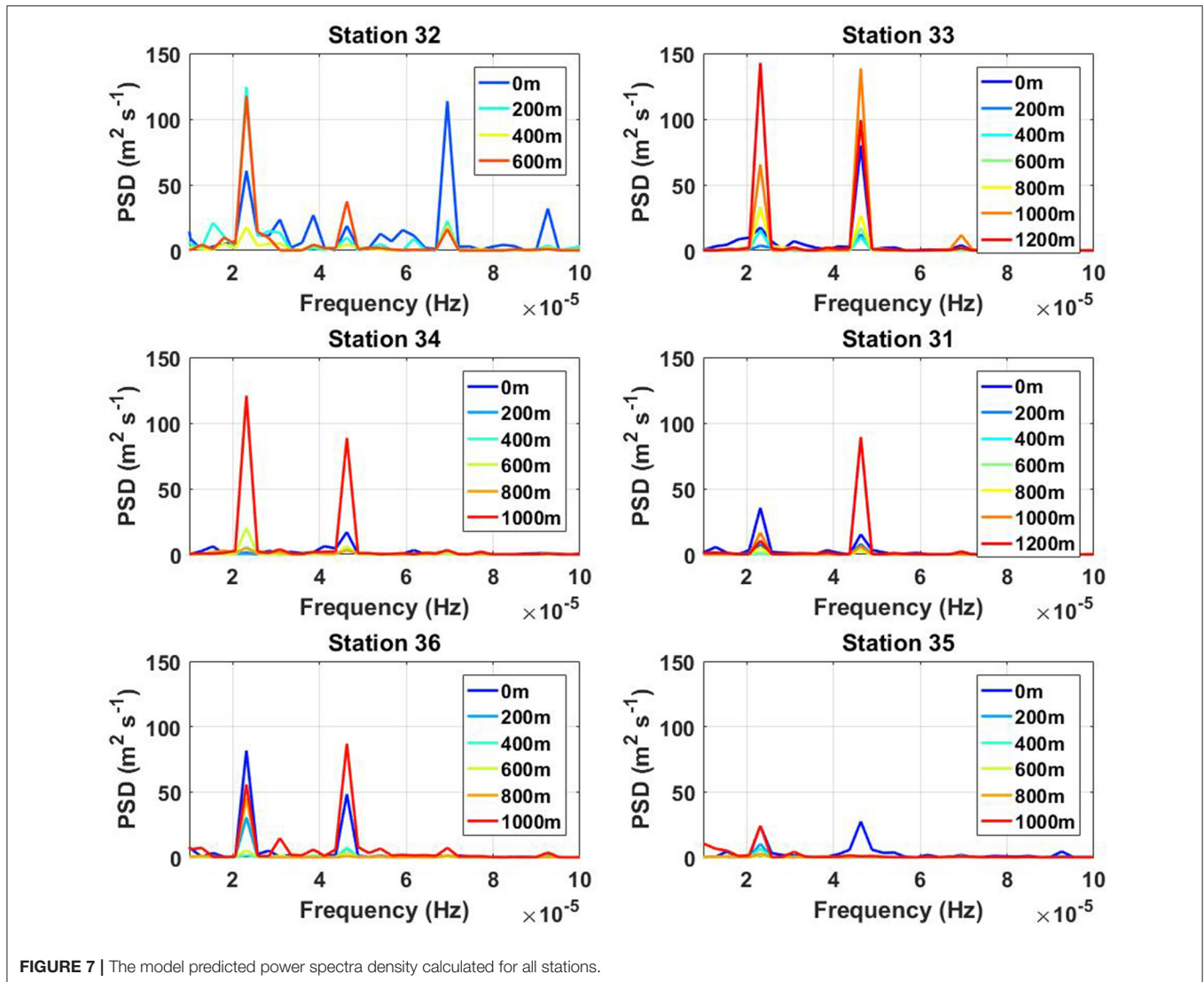
velocity $\sqrt{u^2 + v^2}$ taken over one tidal cycle overlaid in one plot. The dark red curved stripes depict the wavefronts of internal waves (horizontal velocities) at the free surface. The shape of wavefronts, their orientation, and their spatial position suggests that these waves propagate to the northeast and southwest. They are generated above volcanic cones according to the lee-wave mechanism. The areas with $Fr > 1$ are colored in yellow in **Figure 9A**.

Using the model-predicted time series of temperature recorded with 1-min sampling interval at the position of station 32, **Figure 9B**, one can estimate the vertical structure and temporal variability of these short-scale internal waves generated over volcanic cones. It is clear from **Figure 9B** that the internal wave packets occupy mostly surface 100 m thick layer, i.e., the seasonal pycnocline. The intensity of short-scale waves below this level is much lower. As a confirmation, analysis of *in-situ* recorded vertical profiles shown in **Figure 2** reveals the same tendency, i.e., a higher level of intensity of horizontal velocities in the upper surface layer at all stations.

Evidence of lee wave generation in the surface layer is demonstrated here for summer conditions. The internal wave dynamics in the area are controlled by water stratification,

which varies from season to season. **Figure 10** shows that the water stratification in the surface layer is quite sensitive to the seasonal variability. The surface layer is well stratified during summer and almost homogeneous in winter. The buoyancy frequency profiles shown in **Figure 10** were calculated for the RBS area using monthly averaged temperature and salinity data sets based on 94 CTD stations (Levitus and Boyer, 1994). It is expected that the seasonal variability of the fluid stratification can modify the internal wave dynamics over RBS. Note that the fluid stratification below 400 m depth is relatively conservative and does not reveal any essential seasonal variability. The surface seasonal pycnocline does not exist from November to March, but the main pycnocline is relatively stable over the whole year. One can assume that no internal wave activity in the surface layer can be expected during the winter season, but it can be pretty active in the summertime.

Thus, one can assume that during winter, the water dynamics over RBS are controlled by the bottom trapped sub-inertial internal waves. Surface internal waves that are active under summer conditions can not affect the deep-water coral dispersion during the wintertime, controlled by bottom trapped internal waves.



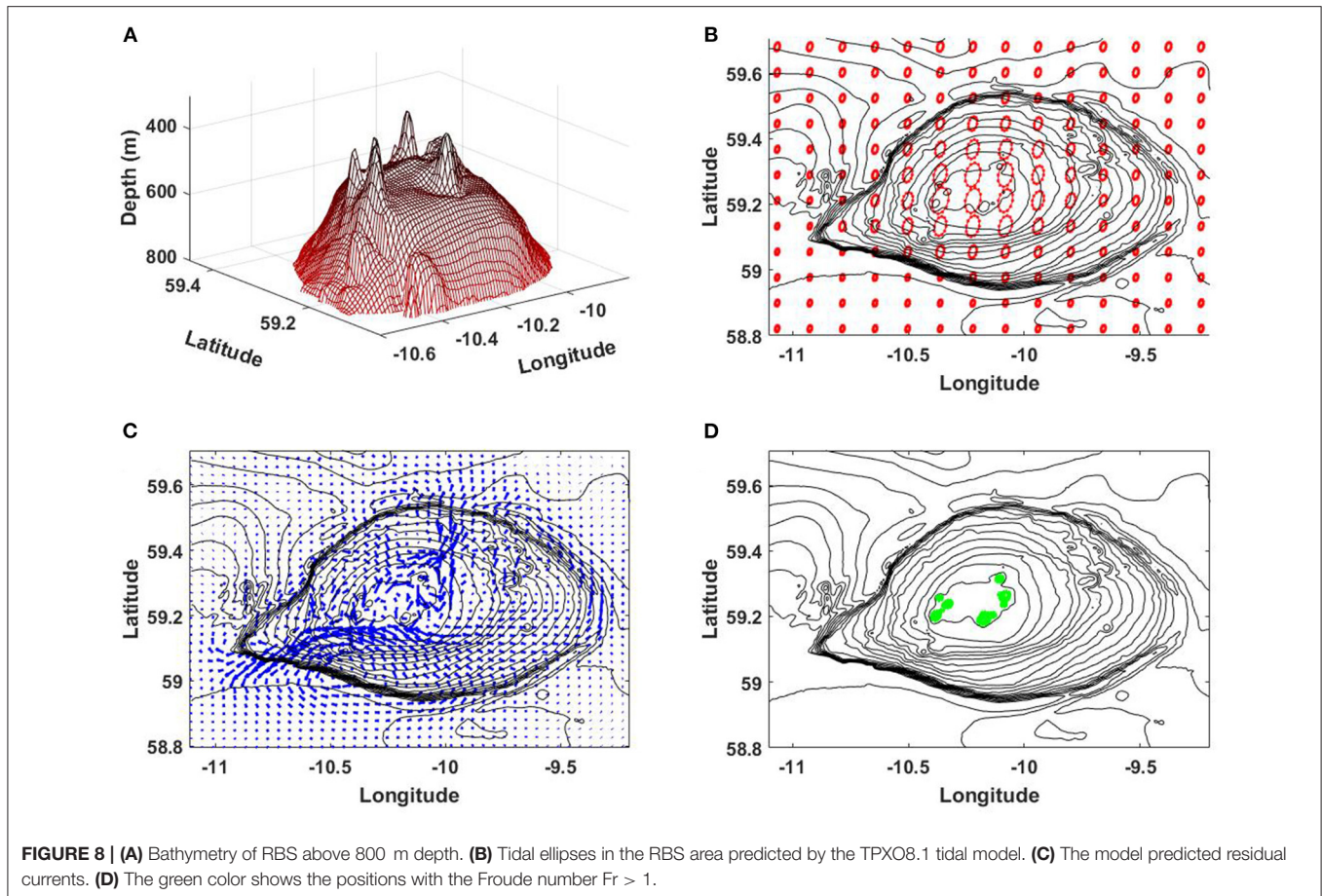
5. LARVAE DISPERSION

Together with the *in-situ* data, the modeling experiments reveal two types of internal waves generated by tidal currents over the RBS summit. The short-scale internal waves, **Figure 9B** are located in the surface stratified layer (seasonal pycnocline, **Figure 1C**). The bottom sub-inertial trapped internal waves are concentrated in the area of the main pycnocline below 600 m depth. Both types of waves can produce water mixing that supplies nutrients and food for deep-water corals and facilitate coral larvae dispersion (Mohn et al., 2014; Cyr et al., 2016).

Numerically wise, having a model velocity as a background process, one can estimate all possible ways of deep-water coral larvae transport around RBS using a Lagrangian approach. A trilinear interpolation with 5-min velocity model outputs was used in these experiments (for the details, see **Supplementary Material**, the Lagrangian model.) This method

can help in understanding to what extent the cloud of larvae released over the bank disperse and escape from RBS.

We consider the larvae as particles with zero buoyancy. Strömberg and Larsson (2017) studied the swimming behavior of the larvae in laboratory tanks. They found that the larvae can move along spirals in circles rather than bullet-style swimming. Considering the larvae trajectories, they look like a Brownian chaotic motion without preferential directions. So, in this paper, we decided to consider the larvae as passive particles. In doing so, 11,000 particles were seeded uniformly on the RBS summit. The experiments were restricted by 1,400 m depth. The spatial step between the position of the released particles was 450 m. The output model velocities were used as an input data set for the Lagrangian-type passive particle tracking model (Stashchuk et al., 2018) to reproduce the pathway of larvae from their initial position. In setting the time scale for the larvae spreading experiments, we followed the results of Larsson et al. (2014)



who showed that 50 days is the most real lifetime for larvae to be dispersed.

The results of the 50 days passive tracer experiments are summarized in **Figure 11**. It was found that the particles disperse differently in different directions depending on their initial position at the RBS summit. Four groups of particles can be classified based on the analysis of their tracks:

- (i) particles that lifted to the surface above 300 m depth;
- (ii) the group of particles that migrated over the summit but always remained within the bank area;
- (iii) the particles that leave the RBS summit and propagate northward;
- (iv) the group of particles that leave RBS and propagate to the west.

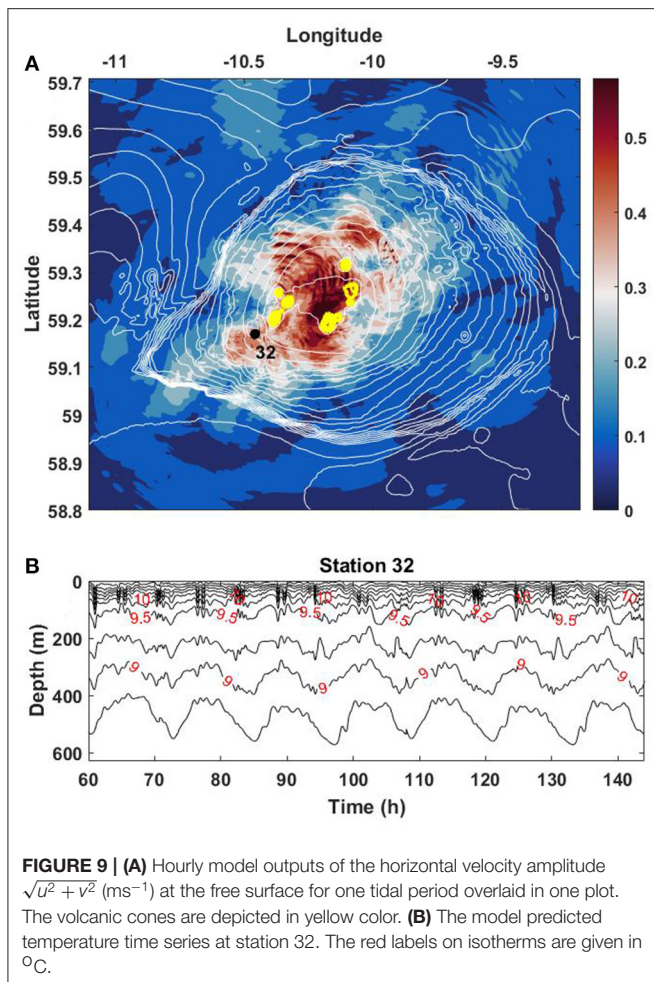
The initial position of these four groups of particles is shown in **Figure 11A**. The color is used to mark the particle of the same group: red for the group (i), yellow for the group (ii), blue for the group (iii), and cyan for the group (iv).

Technically, it is impossible to show the trajectory of all 11,000 particles seeded on RBS in one plot. Instead, we demonstrate here only some typical scenarios of evolution showing their tracks in three dimensions, **Figure 11B**, or presenting the plan view of the particle trajectories, **Figure 11D**. The pie-plot,

Figure 11C, summarizes the specific weight of every particular group (percentage calculated from the total amount). The larvae population lifted to the surface (red color), and those leaving the bank in the northern direction (blue color) are the smallest. The vast majority of particles migrate over the summit without leaving the seamount. Quite a remarkable number of larvae (at least 18%) could escape from RBS propagating to the west.

Interestingly, all particles which propagated vertically to the surface were located initially at the top of RBS, **Figure 11A**. Their ascent can be associated with vertical motions induced by the generated internal waves. Taking into account the seasonal variability of water stratification in the RBS area, **Figure 9**, one can conclude that this mechanism of larvae dispersion is possible only at summertime when seasonal pycnocline is developed. Statistically, most particles propagate horizontally by the residual currents associated with the bottom trapped internal waves. The main pycnocline is stable during all seasons, so one can conclude that this mechanism is active over the whole year.

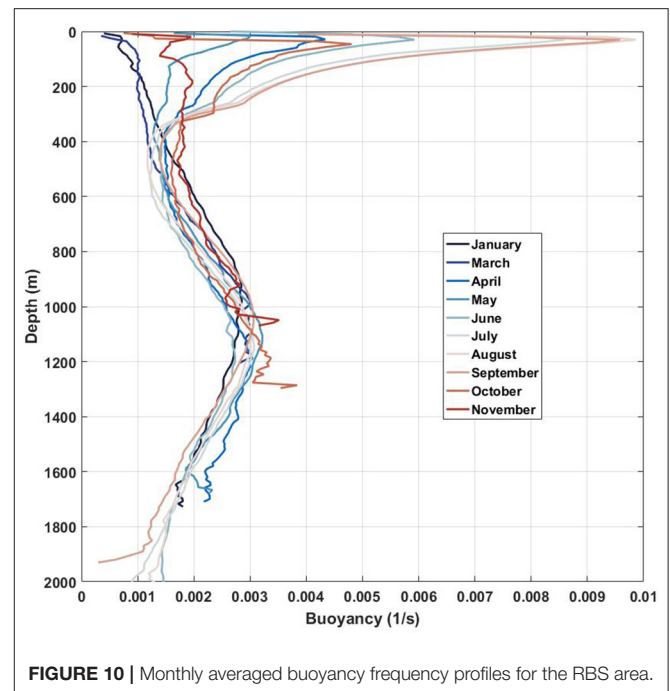
Samples of two different coral species, *Lophelia pertusa* and *Madrepora oculata*, were collected and filmed during a series of JC136 ROV dives. In the North Atlantic, *Lophelia pertusa* spawns once a year between January and March, when



two waveguides do not exist. However, *Madrepora oculata* spawns twice a year (Waller and Tyler, 2005), and vertical motion may influence the larvae dispersion. This circumstance should be taken into account considering possible scenarios of larvae dispersal, **Figure 11**, applying them to different types of deepwater corals.

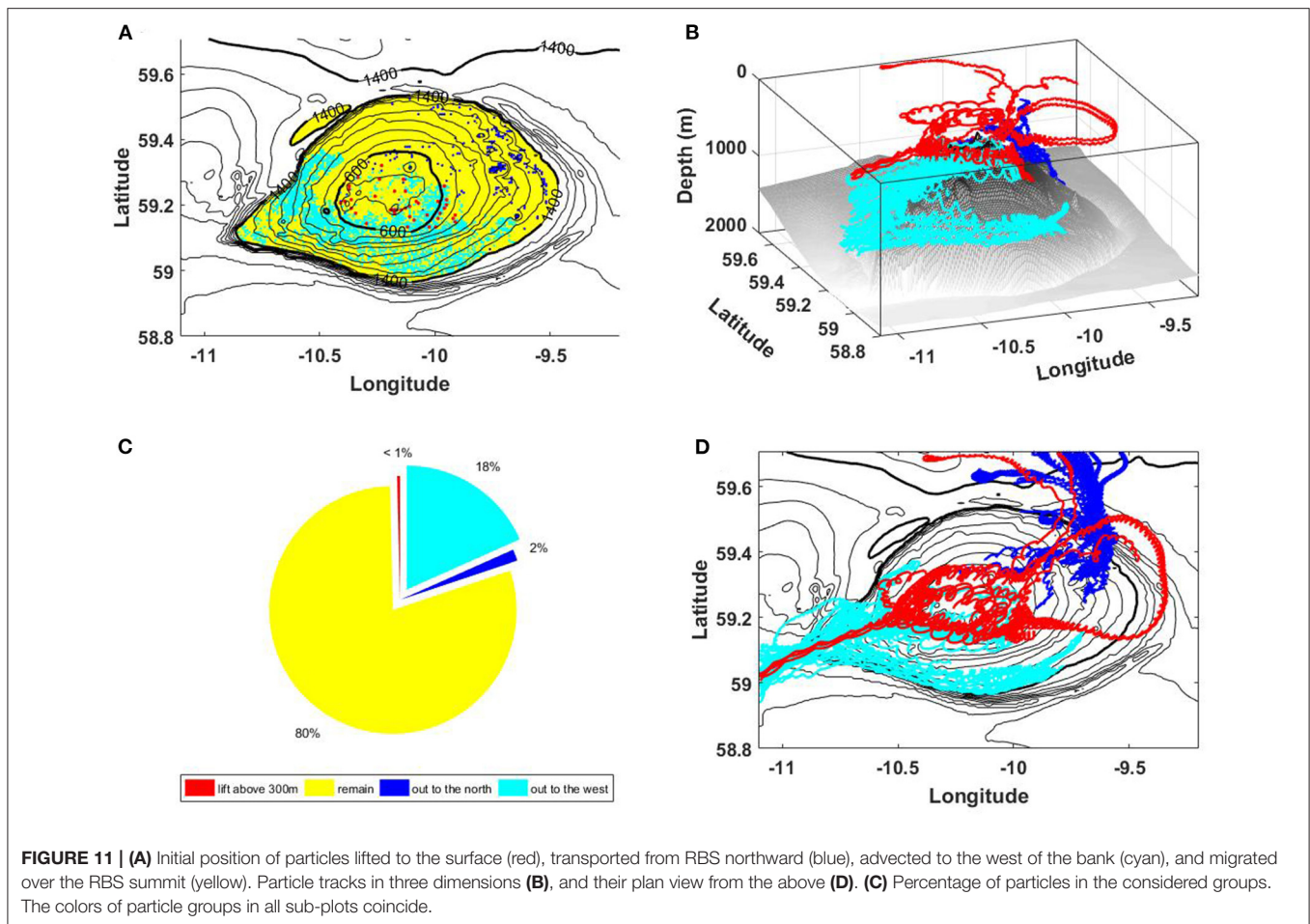
6. DISCUSSION AND SUMMARY

The great importance of seamounts for cold-water coral connectivity in the North Atlantic was acknowledged in many papers (e.g., Fox et al., 2016). The significant effect of internal tides for the coral larvae dispersion was also confirmed by Vlasenko et al. (2018) who numerically quantified the tidally-driven larvae transport in the area of Anton Dohrn Seamount. One of the ideas reported recently is that global-scale modeling can predict the deep-water coral larvae spreading. Ross et al. (2020) discussed the global scale effect of coral larvae dispersion in the North Atlantic estimating the connectivity between different coral communities. In this study, the larvae transport was modeled using a Lagrange passive tracer model. The oceanic background currents were



taken from the output of two large-scale hydrodynamic models, HYCOM (Black, 2002) and POLCOMS (Holt and James, 2001). The aim was to estimate the ways of larvae transport in the North Atlantic over several months. Their study revealed a very great sensitivity of the larvae dispersion trajectories to the model grid scales. Specifically, the uncertainty of hydrodynamic model predictions could result in contrasting ecological interpretations. The principal conclusion of this paper was that high-resolution modeling is required for making more robust predictions.

In this context, the high-resolution modeling of tidal action, as presented in this paper, is quite efficient for describing the local dynamics and larvae spreading. Such an approach we used considering coral larvae dispersion over two seamounts in the NE Atlantic, ADS (Stashchuk et al., 2018; Vlasenko et al., 2018) and RBS (reported in the present paper). These two oceanic banks, RBS, and ADS are located at a distance 170 km (**Figure 1A**). They are quite different in form. ADS is a table-bank formation with very abrupt slopes. RBS has a Gaussian-type shape. It is more massive in size and contains several tall, steep volcanic cones on its summit. As a result of different geometrical forms, these two seamounts reveal quite different internal wave dynamics. Specifically, this concerns the internal tides generation mechanisms. ADS reveals evidence of internal tidal beams radiated from the flanks of the seamount focusing on the central part over the topography. The synthesis of observational data and modeling results confirms the beam structure of internal tides over ADS. A variety of short-scale internal wave motions is produced by the tidal beams hitting the seasonal pycnocline over the ADS summit (Stashchuk et al., 2018; Vlasenko et al., 2018).



The structure of the tidally generated internal waves in the RBS area is quite different. First of all, no internal tidal beams were recorded over RBS in observations. The numerical experiments also confirmed the same result. The bottom currents intensification recorded experimentally at the CTD stations is explained here in terms of the bottom trapped internal wave theory discussed above. The second difference between the internal wave dynamics is the generation of short-wave internal waves over RBS. The existence of tall volcanic cones over the RBS summit creates the conditions for the generation of short internal waves in the seasonal pycnocline according to the lee-wave mechanism. That is not the case with ADS, so the larvae dispersion in these two areas is different. In any case, internal wave activity in both areas is a good source of nutrients and organic matter supply for coral communities, White and Dorschel (2010).

The larvae transport depends on the residual currents that are formed by tides around seamounts. In the ADS area, such currents produce four eddies, Vlasenko et al. (2018); Stashchuk et al. (2018). They provide four main directions for possible larvae trajectories: westward, southward, northward, and northeastward. Thus, potentially, the coral larvae from ADS can reach RBS and deposit there. As distinct from ADS, in the RBS

area, only two eddies are formed by the tidal currents. **Figure 8C** shows possible larvae tracks, mostly in northern and westward directions, without any chance to settle at ADS. These modeling results indicate possible connectivity between ADS and RBS that is controlled by tides.

For both seamounts, ADS, and RBS, the coral larvae were considered purely passive initially. However, taking into account their possibility to swim (Larsson et al., 2014) the initial position of the particles was 5-m above the bottom.

The model prediction time of larvae dispersion in the present paper is based on the results reported by Larsson et al. (2014). In their laboratory investigations of embryogenesis and larval development of cold-water coral *Lophelia pertusa* have shown that nematocysts appear when larvae are 30 days old. After this time, they can settle and give rise to a new coral colony. We have used a planktonic larval duration of 50 days. That is close to 43 days reported by Hilário et al. (2015) as the mean minimum duration for eurybathic species.

The principal outcomes can be summarized as follows:

- *Internal wave dynamics*

Barotropic tide generates two types of internal waves over RBS. Long-scale semidiurnal internal waves are

active below 800 m depth in the layer of the main pycnocline. Their spatial structure is well described by a zero-eigenfunction of the boundary value problem (4). The maximum velocity of this function is located at the bottom.

Short-scale internal waves occupy mostly surface 100-m layer. They can be registered only during the warm season when the seasonal pycnocline exists. These short internal waves are generated by the tidal flow interacting with a cluster of narrow, tall bottom cones, **Figure 8A** that has a volcanic origin. The conditions for the generation of these short internal waves, **Figure 9**, is supercritical in terms of the Froude number, Fr . Specifically, these waves are excited when $Fr > 1$. These surface layer short-period internal waves can be classified as unsteady lee waves.

- *Deep water biological communities*

The internal tides developing in the RMS area can have a significant implication on deep-water coral populations. The larvae live in the water column for more than a month and move with currents before settling down in a new area. The deep-water transport produced by internal tides is one of the principal drivers for coral dispersion (Henry et al., 2014). In this study, we show that the deep-water dynamics over the RMS summit are controlled by bottom trapped internal waves that can initiate residual currents transporting the larvae similar to the mechanism described in Stashchuk et al. (2018). The modeling results help in understanding the larvae transport, i.e., how far the particles can migrate from their initial positions, **Figure 11**.

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DATA AVAILABILITY STATEMENT

The datasets presented in this study can be found in online repositories. The names of the repository/repositories and accession number(s) can be found below: <https://figshare.com/articles/RBS/11688990>. More details on the 136th cruise of the RRS “James Cook” can be found at https://deeplinksproject.wordpress.com/inventories/cruise_inventory/report/16050.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

FUNDING

This work was supported by the UK NERC grant NE/K011855/1.

ACKNOWLEDGMENTS

The authors would like to thank the captain, the crew, and scientific team working together during the JC136 cruise in 2016. The authors appreciate also the collaboration with the University of Plymouth High Performance Cluster team.

SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fmars.2021.735358/full#supplementary-material>

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