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Results suggest that the sands of the dune are sourced predominantly from upwind dunes and sand sources, and that likely contributions from neighbouring dune swales are typically <20%. As such, windrift mechanisms of linear dune formation are not supported by these data. More complex sediment pathway configurations (i.e. other than a binary approach: interdune vs. along-dune), whilst confirming the initial findings, had reduced discriminatory power. Further separation of source pathways (e.g. identifying the relative roles of different upwind sources) was not possible with any confidence.

The findings suggest recent sediment accretion of a linear dune dominated by along-dune sand flux, and thus support an extensional component for the development of such dunes. Whilst it is noted that at a point-by-point basis this might not exclude accretion by vertical growth, as some have observed, there is no clear support for a substantive contribution to the dune sands from adjacent interdunes. Moreover, the use of
contemporary sediment fingerprinting methods to question hypotheses of aeolian geomorphology suggests that such methods have great potential for addressing other terrestrial geomorphological questions where identifying sediment pathways can provide vital insight.

Research Data Related to this Submission
---------------------------------------------
Title: Data for: Testing models of linear dune formation by provenance analysis with composite sediment fingerprints
Repository: Mendeley Data
https://data.mendeley.com/datasets/f6n4rkxhx7/draft?a=947f7067-3a11-4916-adb5-9225310ef503

Title: Data for: Testing models of linear dune formation by provenance analysis with composite sediment fingerprints
Repository: Mendeley Data
https://data.mendeley.com/datasets/rb5676cxsw/draft?a=0aaa36d1-2e76-487c-b2ba-d3bf6044d73e
Response to Reviewers

Reviewer #1

The manuscript is very strong on the analysis but lacks information on (1) local geomorphology to provide context; (2) the sand sampling and analytical methods; and (3) a proper description of the sediment analysis results.

These are now added, and discussed in appropriate places below.

The discussion section is rather lengthy, but the conclusions appear sound.

For this reason, we go only halfway with the suggestion of the second reviewer to move the content of the intro to the discussion.

Specific Comments

1.1 (Mis labeled-should be 1.2) Models for linear dune formation –
Now corrected

Need to include the Courrech du Pont (2014) model in the discussion.
We agree that this is an important development, which merits discussion. This is now mentioned, albeit it briefly as it is less directly relevant to the aims of this study, in the discussion of linear dune models.

Suggest merging Experimental Set up with this section
This section is now moved to open materials and methods, as suggested

include a better description of the field sampling strategy - e.g. explain "ten locations", so that they can be reconciled with the figures that describe the modeling results. I had to look back to Figure 1 to remind myself that X and Y are dune crest samples.
Moving Figure 1 into this section hopefully clarifies this. We have also clarified the nature of the sampling.

Analytical Methods - which elements were analyzed using the ICP.
The full suite of elements analysed, and the methods used, are now included in the methods.

The particle size analysis and geochemical tracers need to be clearly described and tabulated in this section. Describe PS and geochemical patterns on dune and interdune and explain Table 1.
I would move the particle size information (section 3.3) to the start of the section and provide some information on the significance of these data - how do they compare to studies such as Folk (1970)?
We agree that clearer basic description is needed here, as well as greater clarity on the organisation of the results section. We now begin this section with an overview of the structure of this section.
The particle size data are brought forward as suggested, and Folk (1971) and Lancaster (1982) cited here. The grain size data are very much in line with what is well established, and on their own are little new. We retain the geochemical data ahead of the particle size data, though, as that is very much the focus of the interpretation of the paper.

Table 1 - what are the units?
This is now corrected, with apologies.
In addition, table 2 is amended to correct significance rounding to a more consistent and meaningful figure – This includes, where relevant, substitution of zero values; whilst 0.000 may be correct to four significant figures, the true value is not zero, and thus <0.001 has been substituted.
Discussion - Tracer elements - also cite Muhs (2017) for a discussion of the significance of these and other elements
This highly relevant paper is now mentioned, especially with regard to origins of variance in K and Ba concentrations, and the relative weathering resistance of K-feldspars.

Folk, R., 1970. Longitudinal dunes of the northwestern edge of the Simpson Desert, Northern Territory, Australia, 1. geomorphology and grain size relationships. Sedimentology 16, 5-54.
References added as suggested.

Reviewer #2
Minor issues:
1. In a normal paper in Geomorphology, the section of introduction should be short. The different opinions or ideas would be discussed in the section of Discussion. Thus the text from Line 47 to 152 should be combined or shortened.
We shorten this section by moving line 134-152 to the methods section, where we agree it clearly sits better, as suggested by both referees. However, as both reviewers suggest some additions (see below) to the introduction, and we feel that the research question needs framing to justify the methodology and sampling strategy, we retain the section on linear dune formational hypotheses.

Now added as suggested.

3. Geographical coordinates should be added to Figs. 2 and 13.
We have added these to figure 2, and also provided a link in the methods to a .kmz file giving exact sample locations. We suggest that repeating these coordinates is not needed in Figure 13 for a number of reasons: 1) It may detract from the visual impact of the figure, 2) Relational, rather than actual locational, information is more important in this figure and 3) If locational information is needed, the accompanying .kmz file can be used.
The formative mechanisms of linear (longitudinal) dunes and dunefields remain uncertain, and multiple hypotheses have been proposed. A central debate is the degree to which dunes act as along-dune sediment transport corridors, implying that dunes grow primarily by extension, or whether they are comprised of locally-derived sands moved from adjacent interdunes (the ‘wind-rift’ model). Sediment fingerprinting studies, with origins in fluvial science, have been shown to offer the possibility to trace the provenance of aeolian sands, and thus elucidate transport pathways.

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Testing models of linear dune formation by provenance analysis with composite sediment fingerprints

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Highlights

- Two sediment fingerprinting methods used to determine sources of linear dune sand.
- Models consistent in supporting along-dune sediment flux.
- Little evidence of wind-rift mechanisms of linear dune formation.
- Sediment fingerprinting methods can address questions in aeolian geomorphology.

Key words: Linear dunes, Dune extension, Sediment provenance, Monte Carlo simulation.
Abstract

The formative mechanisms of linear (longitudinal) dunes and dunefields remain uncertain, and multiple hypotheses have been proposed. A central debate is the degree to which dunes act as along-dune sediment transport corridors, implying that dunes grow primarily by extension, or whether they are comprised of locally-derived sands moved from adjacent interdunes (the ‘wind-rift’ model). Sediment fingerprinting studies, with origins in fluvial science, have been shown to offer the possibility to trace the provenance of aeolian sands, and thus elucidate transport pathways.

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Testing models of linear dune formation by provenance analysis with composite sediment fingerprints

1. Introduction

Linear (longitudinal) dunes are probably the most abundant desert dune morphology, and yet the mechanisms of formation and development of these dunes remains unclear. Multiple hypotheses, probably working in conjunction, and perhaps at different temporal and spatial scales, have been proposed for the formation of linear dunes. An equally diverse range of methods have been used to investigate the problem, including field-based monitoring of dunes (Craddock et al., 2015), time series of remotely sensed images (Lucas et al., 2015), geophysical surveys to reveal internal sedimentary structures using radar (Bristow et al., 2000, Bristow et al., 2007a, Bristow et al., 2007b, Hollands et al., 2006) and gravity surveys (Yang et al., 2011), chronostratigraphic surveys (Telfer, 2011), numerical modelling (Werner, 1995) and sediment provenance studies (Pell et al., 1999, Pell et al., 2000, Pell et al., 2001).

A crucial, and as yet unresolved, aspect of the formation of linear dunes lies in the provenance of the sands of which the dunes are formed. Amongst a diverse range of hypotheses for the formation of these features, two models emerge which can be seen as end-members of a long-standing (Melton, 1940, Mabbutt and Sullivan, 1968) debate regarding the degree to which linear dunes are extensional depositional features (Lucas et al., 2015, Telfer, 2011), perhaps serving as long-distance transport corridors for wind-blown sand, or whether they primarily accumulate by sand derived from adjacent interdunes (the so-called ‘wind rift’ model) (Wopfner and Twidale, 2001, Zhou et al., 2012, Hollands et al., 2006).

Composite sediment ‘fingerprinting’ methods, originally developed for identifying the origin of fluvial sediments (Collins et al., 1997, Walling et al., 1993), and since developing in sophistication with Monte Carlo and/or Bayesian methodologies (Motha et al., 2003, Fox and Papanicolaou, 2008), have demonstrated the ability of the methods to identify the sources of aeolian sediment. Although
the term ‘fingerprinting’ covers a diverse range of properties and methods, ranging from geochemical analyses to radionuclides and magnetic properties, today most composite sediment fingerprinting methods attempt to identify the optimal properties for discerning the relative contributions of different sources of sediment to a target location, and use these to derive quantitative estimates of contributions with robust estimates of uncertainty.

Gholami et al. (2017) demonstrated the potential of quantitative fingerprinting of aeolian dune sands in elucidating aeolian transport pathways and revealing sediment sources, and Behrooz et al. (2019) identified the provenance and pathways of aeolian dust affecting a region in eastern Iran. Gholami et al. (2019a) revealed that both long (10 to km) and short (1-10 km) transport had contributed to the sands of a small erg, and highlighted the potentially complex nature of aeolian transport pathways.

Here, quantitative composite fingerprinting methods are used to test hypotheses regarding the source of sand in a linear dune in the central Simpson Desert, in central Australia. We use a sediment source fingerprinting method within two different modelling frameworks including Generalized Likelihood Uncertainty Estimate (GLUE) and Monte Carlo (MC) simulations to provide quantitative estimates of the source of dune sands.

1.1 Aims

This study aims to identify local-scale source contributions to linear dunes to improve understanding of their formative mechanisms. In order to do this, we address the following objectives:

1) Quantify contributions and uncertainties for different possible source contributions for aeolian linear sand samples in the Simpson Desert, Central Australia, with two different fingerprinting approaches (GLUE and MC).

2) Assess the performance of both MC and GLUE models by goodness of fit (GOF) in the different source-sink configurations to identify the most likely sediment transport pathways.
1.2 Models of linear dune formation

The debate about the formative mechanisms of linear dunes is exemplified in research in the Australian dunefields, where debates have sometimes been most starkly expressed, but draw from evidence worldwide; observational, experimental, modelled, and based upon field and laboratory analyses. Several simultaneous debates emerged. Some suggested that linear dunes did not move laterally (Bourne et al., 2019, Tsoar et al., 2004, Fujioka et al., 2009), but other evidence was more equivocal (Nanson et al., 1992, Rubin et al., 2008, Rubin and Hunter, 1985), and some contradictory (Hesp et al., 1989), until stratigraphic evidence from geophysical surveys proved convincingly that linear dunes can indeed move laterally (Bristow et al., 2000, Bristow et al., 2005, Bristow et al., 2007a). Others sought to reconcile the degree to which linear dunes grew by extension (Tsoar et al., 2004), or by vertical accretion of locally-derived material (Pell et al., 1999, Pell et al., 2000, Zhou et al., 2012). It is worth noting that, on a point-by-point basis, all accumulation is by necessity ‘vertical’, and only on a landform scale does the term ‘vertical accretion’ really have any meaning. An extension of the latter argument, taken to its most extreme, views linear dunes as erosional rather than depositional features, an idea which has been vigorously contested (Zhou et al., 2013, Rubin and Rubin, 2013). Whilst evidence for very long-distance (inter-basin, or at least >~10^3 km) along-dune transport is lacking on grounds of geochemical provenance (Pell et al., 1997, Pell et al., 1999, Pell et al., 2000), and chronostratigraphic evidence over similar scales lacks support for a purely extensional mode of linear dune formation (Hollands et al., 2006), there is decisive evidence of smaller scale (<10 km) elongation from geophysical (Bristow et al., 2007b), chronostratigraphic (Telfer, 2011, Miller et al., 2018) and observational evidence (Lucas et al., 2015) that linear dunes do develop, at least in part, by extension. Taken to its extreme, the extensional argument has been applied to streaming of sand over the entire north African deserts, including across mountain ranges,
for $10^2$-$10^3$ km (Wilson, 1971, Mainguet and Callot, 1978). It is, perhaps, telling, that some papers within this debate were characterized by distinctly didactic or binary titles; “Longitudinal dunes can move sideways” (Hesp et al., 1989) or “Australian desert dunes; wind rift or depositional origin?” (Wopfner and Twidale, 2001).

The concept that linear dunes may be better considered at the dunefield scale, rather than as individual bedforms, was perhaps best highlighted by Werner’s classic simulations (1995), which demonstrated that characteristic landscapes similar to those observed in the field could emerge when forced with only large-scale forcing parameters, and that individual dune types could be considered as attractors within the phase-space of a complex system. This work, followed by numerous other modelling studies – though infrequently on linear dunes per se – suggested that numerous processes may occur concurrently, and that lateral stability vs. sideways movement, or vertical accretion vs. extension were not mutually exclusive conditions at the dunefield scale. Moreover, new evidence emerged that long-standing theories regarding linear dune orientation may not fully account for the range of alignments observed in the field, and that sediment supply also plays a role in controlling dune orientation (Courrech du Pont et al., 2014). Field evidence also revealed that even adjacent dunes may behave very differently in their accumulation record (Telfer and Thomas, 2007, Telfer et al., 2017). This paper seeks to contribute to this discussion by applying methodologies only recently applied to aeolian settings to address a specific question; at a local scale, are dunes supplied with sediment more by downwind dune sources under a net time-averaged wind regime, or adjacent interdunes fed by individual components of the wind regime?

2. Materials and Methods

2.1 Experimental set-up

To isolate the possible contributions of several different geomorphological settings, we identified a dune where a) clear adjacent interdunes are present on both sides, b) the upwind termination of the dune is clearly visible, where the dune ends in a low, ill-defined slipface-less sand ridge and c) where
a downwind-joining junction also merges laterally into the target dune. This is shown schematically in Figure 1. Samples were collected from ten locations at each site, from the top 1-5 cm of the sands.

Figure 1. Schematic of the sampling strategy for identifying source contributions to the target dune crest. A and B represent upwind contributions, suggesting extensional mechanisms from the snout of the dune and a merging upwind dune, respectively. C and D represent adjacent interdunes. X and Y are the target locations on the main dune crestline.

This structure facilitates the testing of different hypotheses, as different combinations of source area definitions can be considered either together, or separately. Thus it is possible to simply consider all potential upwind source samples as a single region (i.e. A+B), and all adjacent interdunes as a possible source (i.e. C+D); or to isolate individual sources (for instance, consider A and B as distinct).

2.2 Field location

The Simpson Desert lies in the arid centre of the Australian continent (Figure 2a), and the dunefield is composed almost exclusively of linear dunes, occupying an area of around 180,000 km$^2$. Part of the continent-scale whorl of linear dunes formed under anticyclonic influence, the dunes of the Simpson are oriented approximately NNW-SSE (Figure 2b and 2c), and experience a net southerly
wind regime (Hesse, 2010). The misalignment of many Australian dunefields with the modern wind
regime has long been noted (Hesse, 2011), and whilst some young (Holocene) dunes of the
northwestern areas of the Simpson align with current net sand-transporting winds (Hollands et al.,
2006, Nanson et al., 1995), Pleistocene dunes in the southern Simpson do indeed appear out of
alignment (Nanson et al., 1992). The dunefield is of considerable antiquity, with luminescence dating
suggesting dunefield initiation prior to ~590 ka (Fujioka et al., 2009). Ages for the emplacement of
individual dunes suggest that some dunes have been in their current location for at least ~100 ka
(Nanson et al., 1992, Nanson et al., 1995), and possibly substantially more (Fujioka et al., 2009).

Figure 2. The location of the dune studied, in the central Simpson Desert. a) The location of the
Simpson dunefield, in the arid centre of Australia. b) Sampling location set amongst hundreds of SSE-
NNW trending dunes. c) More detailed inspection reveals the presence of both dune terminations
and some junctions and bifurcations within the patterning. d) Local view of the study site, with main
dune crestlines highlighted with dashed lines, target dune samples (blues), possible upwind dune
crest sands (yellows) and possible adjacent interdune source sands (reds).

Samples were taken from the top 1-5 cm of sand, and a .kmz file of the exact locations of samples is
provided along with the online version of this article.

2.2 Analytical Methods
2.2.1 Geochemical and Sedimentological Analysis

Geochemical assays were performed at the ISO9001-accredited Analytical Research Facility at the University of Plymouth. Preparation involved fusion with lithium metaborate/tetraborate mixture, and samples were fused at 950 °C for 20 minutes in graphite crucibles. The fused mixture was dissolved in 40 mL of 10% nitric acid and then diluted to 100 mL. A further ten-fold dilution with 10% nitric acid was required prior to analysis. Analysis of the samples was undertaken using a Thermo Scientific iCAP 7400 ICP-OES instrument and an X Series 2 ICP-MS instrument (both Thermo Scientific, UK). A total suite of 30 elements was analyzed (V, Cr, Mn, Co, Ni, Cu, Mo, Sb, Ba, Ce, Pr, Nd, Sm, Eu, Tb, Dy, Ho, Er, Tm, Yb and Lu by ICP-MS, and Na, Mg, Ca, Al, Si, Fe, K and Ti by ICP-OES).

Calibration standards were prepared by dilution of stock standards, either 10,000 or 100 mg/L and were matrix matched to the samples with the appropriate amount of flux. The performance of each instrument was checked against the manufacturers’ specifications prior to use. A certified reference material, BCR 667, and procedural blanks were prepared and analyzed in the same way as the samples.

Particle size data was provided by laser granulometry using a Malvern Mastersizer 2000 with a Hydro-G wet sample unit. Five subsamples of each sample were each analyzed five times, and mean values taken. Ultrasonic dispersion @90% power was employed for 90 seconds prior to measurement, and derivation of grain size fractions used Malvern’s general analysis model (software v5.6), with enhanced sensitivity and assuming irregular particle shape, a refractive index of 1.56 and light absorption of 0.01 to 0.001.

2.3 Sediment fingerprinting

In this study, once an optimum fingerprint was identified for each permutation of source/target sample, we used two different methods to quantify source contributions; a Monte Carlo framework
(Gholami et al., 2019b), and a Generalized Likelihood Uncertainty Estimate (GLUE; Beven and Binley, 1992, Behrooz et al., 2019) model. The use of fundamentally different procedures allows assessment of the dependence of the results on the choice of methodology, as several studies have highlighted potential dependence of model outputs on the choice of model employed (Palazón et al., 2015, Laceby and Olley, 2015, Haddadchi et al., 2013, Haddadchi et al., 2014).

2.3.1 Selection of the optimum composite fingerprints

A two-stage statistical process including range test and stepwise discriminant function analysis (DFA) was applied for selecting optimum composite fingerprints (Habibi et al., 2019). In the range test (stage 1) (Collins et al., 2010), the maximum and minimum fingerprint values in the source and sediment samples were used for identifying outliers. Tracers failing the range test were removed from further analysis. In stage 2, a stepwise DFA based on the minimization of Wilk’s Lambda was used to select the optimum composite fingerprints (Gholami et al., 2017, Pulley and Collins, 2018).

Bi-plots, as a further test of the conservative behavior of the tracers included in the optimum composite fingerprints, were used to assess similarities in the relationships between tracers in the sediment and source samples (Habibi et al., 2019).

2.3.2 Quantifying source contributions of aeolian sediment using a mixing model within a Monte Carlo simulation framework

A mixing model (Collins et al., 1997) within a Monte Carlo simulation framework (Gholami et al., 2019b) was applied to quantify contributions of the potential sources in three different permutations (A+B and C+D; A, B and C+D; A, B, C and D) to twenty aeolian sediment samples (X1-X10 and Y1-Y10). The probability density functions (pdfs) (Collins et al., 2013) were constructed based on the means and standard deviations of the optimum composite fingerprints for the sediment and source samples, and these were repeatedly sampled during the Monte Carlo simulations (Hughes et al., 2009). Using Latin Hypercube Sampling (LHS), 50,000 random samples
were drawn from the pdfs to permit Eq. (1) to be solved 50,000 times. The contributions of the two potential sources were calculated by the model with 95% confidence limits.

\[
f(X_j) = \sum_{i=1}^{n} \left( \frac{(C_i - \sum_{j=1}^{m} P_j \cdot X_{j,i})}{C_i} \right)^2
\]  

(Eq.1)

Where \( n \) is the number of fingerprint properties (here varying from 2 to 3), \( m \) is the number of sediment sources (that is, between 2 and 4 depending on experimental set-up), \( C_i \) is the mean concentration of fingerprint property (i) in the sediment sample, \( P_j \) is the relative contribution of source \( j \) to the sediment sample, \( X_{j,i} \) is the mean concentration of fingerprint property (i) in source \( j \). The mixing model must satisfy two boundary constraints: each source contribution must be between 0 and 1, and all the contributions must sum to 1.

2.3.3 Quantifying source contributions of aeolian sediment using the Generalized Likelihood Uncertainty Estimate (GLUE) model

The GLUE methodology followed Behrooz et al.’s (2019) implementation of the original methodology proposed by Beven and Binley (1992) and used the same permutations of target and source. This utilizes five steps, and is described in full in Behrooz et al. (2019), but to summarize:

1) Latin Hypercube Sampling (LHS) (Collins et al., 2013) is used to sample the parameter sets for 200,000 iterations, based upon a uniform distribution for all parameters, due to lack of \textit{a priori} knowledge. It is assumed all source contributions are non-negative, and sum to unity.

2) The Nash–Sutcliffe coefficient (ENS) is used as the likelihood function, and is defined thus:

\[
ENS = 1 - \frac{\sum (O_{obs} - O_{sim})}{\sum (O_{obs} - O_{obs})} = 1 - \frac{\sigma_i^2}{\sigma_{obs}^2}
\]  

(Eq.2)

where \( O_{obs} \) is the mean value of the observed tracer concentration; \( O_{sim} \) is the simulated tracer concentration; \( O_{obs} \) is the observed tracer concentration; \( \sigma_i^2 \) is the error variance for the \( i \)th model
(i.e., the combination of the model and the \( i \)th parameter set) and \( \sigma^2_{\text{obs}} \) is the variance of the observations.

3) The sampled parameter sets from step 1 are fed into the mixing model (equation 2), and the likelihood function is calculated for each parameter set as:

\[
C_{\text{Sediment}} = C_{\text{Sources}} \times P \quad \text{(Eq. 3)}
\]

where \( P \) is an \( m \)-dimensional column vector of sources contribution (sampled parameter sets), \( C_{\text{Sediment}} \) is an \( n \)-dimensional column vector of element concentration in sediment sample, \( C_{\text{Sources}} \) is an \( n \times m \)-dimensional matrix representing mean tracer concentration in sources (each row represents mean tracer concentration in each source).

4) Each parameter set is defined as either behavioural or non-behavioural types, depending on whether their likelihood function exceeds a threshold value (Zhou et al., 2016). Non-behavioural parameter sets were discarded.

5) For each parameter set defined as behavioural, likelihood weights are rescaled such that they sum to one, and a cumulative distribution derived for each parameter, to enable the derivation of uncertainties.

### 2.3.4 Assessing performance of the MC and GLUE models

A Goodness of Fit (GOF) test (Manjoro et al., 2016; Gholami et al., 2019b) was applied to evaluate performance of the two models - MC and GLUE. Although not without critics (Palazón et al., 2015), the method is widely used to give an indication of the validity of model findings (e.g. Habibi et al., 2019, Zhou et al., 2016), and here we use it relatively to assess differences of the proposed source configurations. Goodness of Fit, using the terms of Eq. 1, is thus defined:

\[
GOF = (1 - \sqrt[n]{\frac{\sum_{i=1}^{n} \left( \frac{C_i - (\sum_{j=1}^{m} P_j X_{ij})}{C_i} \right)^2}{n}})^{2/4} \quad \text{(Eq. 4)}
\]
3. Results

In the first part (3.1) of the section, the basic geochemical and particle size data for the samples are presented. The second section discusses the development of the statistical fingerprinting methods from the geochemical data, and lastly, section 3.3 presents the outcomes of different combination of source-target configurations and modelling frameworks.

3.1 Geochemical and particle size results

3.1.1 Geochemical assays

The results of the ICP analyses are presented in Table 1. The major species are, unsurprisingly, indicative of quartz-dominated sands (indeed the Si values seem low, with even 38% Si corresponding to an equivalent pure quartz concentration of 80%) with a more minor K-dominated feldspar component. This is broadly inline with the few other quantitative studies of sand mineral composition from central Australia, with Fitzsimmons et al. (2009) reporting 80-95% quartz and 1-15% feldspar for linear dunes of the Strzelecki to the southeast.

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<td>37.83</td>
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<tr>
<td>Min</td>
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<td>339</td>
<td>0.84</td>
<td>16.61</td>
<td>0.41</td>
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<td>29.94</td>
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<td>2835</td>
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Range test

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<td>Ba (ppb)</td>
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<td>Nd (ppm)</td>
<td>Sm (ppm)</td>
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<td>2.47</td>
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<td>251</td>
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<td>2.98</td>
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<td>Mean</td>
<td>628</td>
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<td>276</td>
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<td>Tb (ppb)</td>
<td>Dy (ppb)</td>
<td>Ho (ppb)</td>
<td>Er (ppb)</td>
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<tr>
<td>Sediment Min</td>
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<td>70</td>
<td>421</td>
<td>87</td>
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<td>638</td>
<td>110</td>
<td>612</td>
<td>129</td>
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<td>Sediment Max</td>
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<td>163</td>
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<td>Source Min</td>
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<tr>
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<td>Lu (ppb)</td>
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<tr>
<td>Min</td>
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<tr>
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<td>74</td>
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<tr>
<td>Sediment</td>
<td>Max</td>
<td>729</td>
<td>128</td>
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<tr>
<td>Min</td>
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<td>54</td>
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<td>Mean</td>
<td>675</td>
<td>112</td>
<td></td>
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<td></td>
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<td></td>
</tr>
<tr>
<td>Source</td>
<td>Max</td>
<td>1015</td>
<td>183</td>
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<td>Range test</td>
<td>F</td>
<td>F</td>
<td></td>
<td></td>
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</tr>
</tbody>
</table>

Table 1: Minimum, mean and maximum concentrations of the geochemical tracers in all samples.

the source and target sediment samples. p and f indicate passing and failing the range test, respectively; see section 3.2.1.

3.1.2 Physical sediment characteristics
Figure 3. Particle size distributions for all samples. Sand source samples a) A and b) B are dominated by very fine – medium sands, with a marked positive tail towards coarse sands, and whilst the interdune source samples c) C and d) D are also dominated by very fine – fine sands, here there is a negative tail in the distribution, with up to 20% silt in some samples. The target dunes e) X and f) Y are the best sorted, with little other than very fine – medium sand.

All samples (Figure 3) are characterized by a dominance of fine sands (31.5 – 64.6%; mean 48.7%) and very fine sands (11.5 – 50.7%; mean 30.7%). In total, sands comprise 78.7 – 100% of the sediments (mean 96.0%), and silts comprise 0 – 20.4% (mean 3.9%). The interdune samples (C and D; Figure 3c and 11d) however, are typified by an increased silt component (averaging 10.2%, and up to 20.4% in one sample), compared to the source and target dune sands where silts average just 0.8% and the maximum observed value is 3.6%. There is also a slight positive tail to all candidate sources
samples (A-D), with a minor component of coarser sands; this is in line with well-reported trends in linear dunes/interdunes (e.g. Lancaster, 1982, Folk, 1971).

3.2 Discrimination of sediment sources by range test and stepwise DFA

3.2.1 Range test

Prior to applying a statistical procedure for selecting final fingerprints, a range test (Collins et al., 2010; Gellis and Noe, 2013) was used to identify outliers and, therefore, significantly non-conservative tracers for exclusion from further analysis. Here, the maximum and minimum tracer concentrations in the source and sediment samples were used for identifying outliers (Table 1). Tracers failing the range test (i.e. tracer concentrations measured for the target sediment samples that fell outside the corresponding ranges of the source sample tracer concentrations) were removed from further analysis (Gholami et al., 2019a, Gholami et al., 2019b, Nosrati et al., 2018).

Five tracer elements were identified as significant for the three models of sediment pathway, but only one (Na) is consistent throughout. Antimony (Sb) and potassium (K) are identified as the other most significant tracers for the two-source scenario, molybdenum (Mo) as the additional tracer in the three-source model, and barium (Ba) in the four-source configuration. The likely sources of these elements are considered in section 4.1, though for now it is worth noting that whilst some mobility of soluble Na salts cannot be ruled out, antimony, with a near-equal predictive power, is very insoluble in the natural environment. It is likely significant that Na and Ba together have lower predictive power in the case of the four-source scenario in the later interpretation of results, as indicated by the markedly lower sum of the Wilk’s Lambda; the implications of this are considered in section 4.1. Figure 4 shows scatterplots of the three- and four-source permutations of the stepwise DFA; the two-source model yielded a single predictive discriminant function.
<table>
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<th>Step</th>
<th>Tracer selected</th>
<th>Wilk’s Lambda</th>
<th>Sig</th>
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<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>With two potential sources (A+B and C+D)</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>Na</td>
<td>0.269</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>2</td>
<td>Sb</td>
<td>0.230</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>3</td>
<td>K</td>
<td>0.204</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td><strong>With three potential sources (A, B and C+D)</strong></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>1</td>
<td>Na</td>
<td>0.262</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>2</td>
<td>Mo</td>
<td>0.186</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td><strong>With four potential sources (A, B, C and D)</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>Na</td>
<td>0.13</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>2</td>
<td>Ba</td>
<td>0.068</td>
<td>&lt;0.001</td>
</tr>
</tbody>
</table>

*Table 2: Results of DFA for selecting optimum composite fingerprints with two (A+B and C+D), three (A, B and C+D) and four (A, B, C and D) potential sources.*
Figure 4: Scatterplots were constructed from first and second functions in the stepwise DFA, a) with three potential sources (A, B and C+D); and b) with four potential sources (A, B, C and D). With two potential sources (A+B and C+D), scatterplots are not applicable because there is a single discrimination function. 97.4, 84.6 and 92.3% source samples were classified correctly for two, three and four potential sources, respectively.

3.2.2 Conservative behaviour of optimum composite fingerprints in the sediment and source samples

Results from the bi-plot test are presented in Figure 5. Plots wherein the source and sediment samples do not fall in the same general space suggest non-conservative behaviour of the tracers in question.
Figure 5: Bi-plots for all pairings of the geochemical tracers in the final composite signature, measured on the source and target sediment samples: a, b and c) with two potential sources (A+B and C+D), d) with three potential sources (A, B and C+D) and e) with four potential sources (A, B, C and D).

3.3 Source contributions from different models and various sediment pathway configurations

Three different source-target configurations are considered here, each with the two models proposed; Monte Carlo modelling and the GLUE framework.
3.3.1 Two-source configuration: upwind and adjacent sources (A+B; C+D)

Figure 6: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A+B and C+D indicate two potential sources for aeolian sediment samples.

The results of the two-source configuration from both models are encouragingly consistent (Figures 6 and 7); both imply a system dominated by dune sands sourced from upwind locations (both the upwind dune snout (A), and the merging dune (B)). By either assessment, sixteen of the twenty samples are clearly dominated (>70%) by sediments with affiliation to these sources, with X6 (most markedly), Y2, Y6 and Y7 as notable exceptions. Both modelling approaches are consistent in the identification of which samples share greater affinity with the two possible sources. GLUE estimates are typically characterized by their smaller uncertainties.
Figure 7: GLUE results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A+B and C+D indicate two potential sources for aeolian sediment samples.
3.3.2 Three-source configuration: dune snout, merging dune and adjacent sources (A; B; C+D)

Figure 8: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B and C+D indicate three potential sources for aeolian sediment samples.
Figure 9: GLUE results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B and C+D indicate three potential sources for aeolian sediment samples.

The three-source configuration (Figures 8 and 9) offers much support for the two-source scenario, but also offers further information. With both Monte Carlo and GLUE methodologies, source B – the merging dune – is seen to dominate the likely source contributions. Extreme uncertainties –
especially for the Monte Carlo method - are undoubtedly wider, but interquartile ranges (indicated by the blue box on the box-and-whisker plots of Fig 7 and Fig 8) are generally supportive of a dominant source contribution coming specifically from the merging dune (source B), beyond that contributed from the immediate upwind sand source (source A). Sample X6, especially, remains a clear outlier to the general trend, with greater similarity to the interdune samples.
3.3.4 Four-source configuration: dune snout, merging dune and eastern and western interdune
Figure 10: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B, C and D indicate four potential sources for aeolian sediment samples.

Results from the four-case scenario are more complex, and characterized, especially in the case of Monte Carlo modelling (Figure 10), by much greater uncertainties. There is still broad agreement that the contribution of the upwind sources (that is, A and B) dominates that from the interdunes (that is, C and D), but interquartile variance in the estimates typically exceeds 50% and, in some cases, approaches 100% for the upwind sources. GLUE estimates (Figure 11) also suggest greater importance of the upwind sources, and has tighter constraints on uncertainty, but it is noticeable that variance is greater under this scenario than others approached with the GLUE methodology (Fig 7 and 9). Despite the greater uncertainties, the relative contribution of the upwind sources (the immediately-upwind low sand pile, and merging dune) is apparently somewhat reversed under this approach, with a greater role indicated for the immediate upwind source. Both modelling approaches suggest a slightly higher input from the western interdune, compared to the eastern side, with the notable exception of sample X6, with a median contribution of around 50% total from the eastern interdune and just 20-30% from the west.
Figure 11: GLUE results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B, C and D indicate four potential sources for aeolian sediment samples.

4. Discussion

The performance of the models is considered first, before considering the implications of the most robust findings for models of linear dune formation.

4.1 Sediment fingerprinting model performance

The elements identified as the most significant tracers vary from abundant mineral-forming alkali metals (Na and K), to much scarcer alkaline earth metals (Ba), transitional metals (Mo) and metalloids (Sb); all are relatively enriched in the source sediments relative to the target dune sands.

The alkali metals are likely associated with weathering products from feldspars and micas, and Ba may substitute for K in the lattice of these minerals (Kasper-Zubillaga et al., 2007). Indeed, K/Ba ratio (along with K/Rb) in aeolian K-feldspar sands was one of the indices identified by Muhs (2017) as the most promising for identifying the provenance of North American dune sands. Whilst the possibility of a soluble sodium component in the sands cannot be entirely discounted, most of the other tracers identified are insoluble in this environment, and Muhs also note the relative chemical resistance of K-feldspars (orthoclase and microcline), and likely variance in K and Ba as being attributable to source geology, and not weathering. The dominant heavy minerals in the study region belong to Pell et al.’s (2000) ‘northern Simpson’ population, in which haematite, epidote and muscovite are abundant, and garnet, tourmaline, monazite and zircon significant. Molybdenum is most often associated with Cu ores, an observation consistent with Pell et al.’s (2000) attribution of the Mount Isa block, which contains substantial Cu deposits (Gregory et al., 2008), as the ‘proto-source’ for the sands of the Simpson. Antimony is also known from the Mount Isa block, associated with lead mineralization. In short, the tracers identified seem likely to reflect both primary mineralization and
long-distance transport of heavy minerals from proto-sources, and subsequent elemental differences in sands and silts as a result of weathering.

Figure 12 presents the results of the evaluation performance of the Monte Carlo simulation (MC) and GLUE model by GOF for the different configurations of sources (two-, three- and four-sources). Both MC and GLUE models have the highest performance associated with the simplest (two-source) configuration, with GOF values for the majority of sand samples of > 80%. In the 3-source model, the GOF values for majority of the samples were 50-80%, and yet poorer performance for the four-source model is indicated by GOF values typically < 50%. Overall, based on the GOF values (for majority of samples > 80%) and scatterplot constructed stepwise DFA (97.4% source samples were classified correctly), the two-sources grouping (A+B and C+D) is the best grouping for discriminating sources of sand dunes in the Simpson Desert.
Figure 12. The Goodness of Fit (GOF) values for the MC and GLUE models for 20 sand dunes samples

a) X1-X10, and b) Y1-Y10. In the majority of cases, the two-source model is seen to provide the strongest predictive power, followed by the three-source scenario and lastly the four-source configuration.
4.2 Implications for linear dune formation

4.2.1 Interpreting the provenance analyses

The results of the six provenancing assays are shown spatially in Figure 13.

Figure 13. Spatial representation of the median estimate of source contributions under different assumed sediment pathway configurations and using two different methodologies for the fingerprinting. The simplest situation simply compares upwind and adjacent sources using a) Monte Carlo and b) GLUE frameworks. c) and d) differentiate between the immediate upwind low sands (A) and a flanking dune which merges with the target (B). e) and f) treat all four possible sources individually. Pie charts are shaded according to the colours of the source labels in panels a), c) and e).

Under all permutations, sands from upwind sources dominate; more detailed breakdown of the sources is less unequivocal.
Results from the provenance analyses, using either methodology, and, broadly, under any of the source configurations considered, suggest a dominant source component for the dune studied from immediately up-wind sources; the upwind ill-defined sand ridge, and the merging dune to the southwest. This is more consistent with the concept of along-dune sediment transport than wind-rift models of dune formation, whereby the sands of the dune are derived from adjacent interdunes. Some caveats must ride with this interpretation, under any of the suggested sediment configurations, though. Firstly, this interpretation necessarily assumes that the sands – and typically the interdunes are ~90% sand-sized (Figure 3) - found in the interdune today are the same as those found in the interdune at the time of dune formation. Whilst no ages are available for this dune, similar dunes from the Simpson are characterized by basal (i.e. emplacement) ages of \(10^4-10^5\) years (Fujioka et al., 2009, Hollands et al., 2006, Nanson et al., 1992), and thus the formative timescales of such landforms are long. Are the potential sources of dune sand today (i.e. interdunes vs. dunes) the same as they were at the time of dune emplacement? This is, and must always be, a hypothetical question; it is not possible to directly assess this. It should be noted that the sediment samples taken – both source and target – are essentially surface samples, and we cannot \textit{sensu stricto} conclude that the same pathways would have been followed at the time of dune emplacement at this location. The assays here address the question of recent sand transport most directly, and it is not advisable to extrapolate necessarily to the timescale of tens of thousands of years.

Secondly, the question of similarity of the source and target samples must be addressed. It was hypothesized that the most likely causes for the choice of tracers found to be the most suitable by the stepwise DFA (that is, sodium, potassium and antimony for the two-source model) are most likely driven by weathering of non-quartz minerals such as feldspars (which may well be found in greater quantities in the finer-grained silts of the interdunes) and in resistant, heavy minerals found as sand-sized grains. Given the differences observed in grain sizes, might the observed results be driven not by aeolian sand transport, but by \textit{in-situ} weathering of the interdunes? Some evidence that this is not the case can be drawn from the outlying sample (X6) in the target group, which, of
the twenty target samples analysed, was the only one showing much clearer affinity with the interdune samples that the upwind sources. If it were the case that the differences observed between the possible sources are attributed largely to a size-fraction dependent cause, then it might be expected that this is evident in the physical properties of sample X6 – it should be more similar in texture to the interdunes, with an enhanced fine-grained component. However (Figure 14), this is not evident from the physical characteristics of this sample; from this, it seems most likely that the provenancing methodology is indeed identifying sediment transport-driven differences.

Figure 14. Grain size properties for sample X6, alongside those of other samples from the target site X. Although the provenance analysis identified X6 as being an outlying sample, and more likely derived from the adjacent interdunes, it is physically indistinguishable from the well-sorted sands of the other samples.

4.2.2. Differing source configurations

The dominance of upwind sources is clear across all methods, and all source configurations tested (Figure 13). Further interpreting the three- and four-source configurations, however, is harder, and much more equivocal. This is likely due in part to the weaker performance of both models under
these configurations (Table 2 and Fig 12). Both MC and GLUE models, under the three-source configuration, do suggest some additional information. The contribution from the merging dune for both target sites is markedly greater than that of the immediate-upwind low sand ridge for both target sites (X and Y), and both models are in agreement that this effect is more marked for the northerly target site, Y (Figure 13). This could be seen as consistent with the idea of linear dunes as preferential transport pathways in the landscape. In the case of the four-source model, however, this result is no longer visible, and both upwind sources are attributed approximately equal importance as contributions. Similarly, there is no clear differentiation between eastern and western interdunes as the dominant source of the lesser lateral component of transport. Thus, whilst the different configurations tested are unanimous in identifying a dominant role for the upwind sources, further granularity in identifying sources is not possible from these findings.

4.2.3. Results in context

We interpret the results of this study as being consistent with a model favouring along-dune sediment flux, and less supportive of ‘wind-rift’ models whereby dune sands are derived from adjacent interdunes, and accretion is primarily vertical. How, then, can these findings be reconciled with the findings of others (e.g. Craddock et al., 2015, Hollands et al., 2006) who have supported the wind-rift/vertical accretion model? It is worth considering the very different methodologies that have been employed to address the questions surrounding linear dune extension/wind-rift formation. Craddock et al. (2015), for instance, used decadal-scale (8-year) field observation of erosion pins, and differential GPS surveying. Others have used chronostratigraphies (e.g. Hollands et al., 2006, Telfer, 2011) or stratigraphies derived from geophysical surveying (e.g. Bristow et al., 2007b). Previous provenance studies have used geochemical and geochronological methods to assess the role of long-distance sediment transport (e.g. Pell et al., 1997, Pell et al., 2000). Inherent in these different methodologies are a vast range of timescales (from $10^3$ years for field study – $10^6$ years in the case of zircon U-Pb provenance analyses), and spatial scales (from $10^2$ m scale accretion
in the case of field survey, to $10^3 - 10^4$ m scale for some stratigraphic studies). The challenges in reconciling such data are self-evident, and part of a wider narrative within the aeolian community that has sometimes questioned the instructiveness of reductionist approaches (Livingstone et al., 2007). A useful exercise may, thus, be to look for similarities, not difference, in the findings of this study and the most recent study with apparently contradictory findings in this region; that of Craddock et al. (2015).

Firstly, both studies seek to address the changes that have affected linear dunes of the Simpson desert in the recent past – in the case of Craddock et al. (2015), over an eight-year period of observation, and here by focusing on surficial sediment. Although it is not possible to directly assess the timeframe of observation here, late Holocene ages are recorded at depths of ~1 m in the Tirari and northern Strzelecki desert (Fitzsimmons et al., 2007, Telfer et al., 2017), as well as the western Simpson (Nanson et al., 1995). For samples collected within the top 5 cm of the dune, it seems reasonable to infer that timescales of > 100 years are likely for the sands in this study. Both studies observe spatial scales on the order of $10^2 - 10^3$ m, but, perhaps significantly, the dune chosen to for study by Craddock et al. (2015) is located at a downwind termination, whereas this study focuses on an upwind dune termination. Craddock et al. (2015) observed ~10 cm – 1 m of net accumulation on most stakes, with some showing periodic exhumation towards the lower end of this range, but did not see evidence of dune extension during this time in the form of progradation of the dune snout; this was interpreted as dune growth by vertical accretion, which, over the timescale under consideration, is clearly the case. Craddock et al. (2015) note that their findings are not necessarily at odds with the millennial-scale chronostratigraphies of Telfer (2011), which were interpreted as showing evidence both for elongation, and dune mobility without concurrent lengthening; conclusions echoing those of Bristow et al.’s (2007b) geophysical surveys, which suggested that both lengthening and vertical landform growth were possible at different times/places. Miller et al. (2018), working on a linear dune whose origin is clearly tied to the adjacent Wolfe Creek meteor impact crater by the deflection that the crater has imparted on the dune planform, were able to
estimate a minimum extension rate of ~3 km over ~ 120 ka, or of the order of 35 m ka\(^{-1}\); it is unsurprising that studies working at observational timescales of ~10 years may not observe dune extension.

The interdune areas surveyed by Craddock et al. (2015) experienced both net accumulation and deflation of a few cm, with no clear spatial patterning. As such, there is no specific evidence here for the source of the sand which, over their decadal-scale survey, contributed to vertical landform growth; a condition which seems necessary for the wholesale adoption of the wind-rift model. Whilst the work of Pell and colleagues on numerous Australian dunefields provides convincing evidence for a lack of continental-scale aeolian sand transport fluxes (Pell et al., 1999, Pell et al., 2000, Pell et al., 2001), there is again no mutual exclusivity with the findings of these studies, and those suggested here. Pell et al. (1999, 2000, 2001) were considering the ultimate ‘proto-source’ of the heavy mineral assemblages of dunes, and as such, constrained by U-Pb zircon dating, considering timescales of 10\(^8\)-10\(^9\) years. As there is evidence (Fujioka et al., 2009) that the Simpson dunes likely have an early Pleistocene initiation age, such conclusions, whilst relevant to the degree to which continental-scale wind transport has occurred, does not necessarily support the dunes sands as being locally-derived over scales of 10\(^0\) – 10\(^1\) km, as has sometimes been inferred (Hollands et al., 2006). Here, we demonstrate evidence that the sands near the upwind snout of a linear dune are predominantly derived, not from the adjacent interdunes as required by a pure wind-rift model, but by downwind sediment transport, either from upwind interdune sediment sources, or by sediment flux along a merging dune. Given local spatial differences in dune accumulation histories over even the most local of scales (Telfer et al., 2017), we note that this does not preclude net vertical accumulation of dunes occurring at certain places and times, or even that such sediment might not periodically come from interdune sources.

In summary, there is now sufficient evidence from diverse sources that linear dunes can, at different times and places, grow by extension and predominantly vertical growth at landform-scale; that they
can migrate laterally, and yet often do remain in the same place for $10^4$-$10^5$ years; and that whilst we
cannot rule out predominantly lateral accretion of sediment at times, that they act as downwind
corridors of sediment flux, resulting in dunes which, at times, clearly grow by extension. Whilst such
statements may seem paradoxical, there is no reason that they cannot all be true, given sufficient
time and spatial timeframes, which both seem generously available for the formation of linear
dune fields.

5. Conclusions

We demonstrate here that sediment fingerprinting studies have the potential to elucidate transport
pathways at a scale relevant to understanding landform formation. Two different sediment
fingerprinting modeling frameworks (a Monte Carlo approach, and the GLUE methodology) provide
consistent estimates that the upwind sources, including a low sand ridge, and a merging dune, are
the most significant contributions for the sands of a linear dune in the central Simpson Desert,
compared to the adjacent interdunes. Both frameworks performed with greater success when
considering simpler configurations of possible sources, and metrics of model performance
(Goodness of Fit) suggest a high degree of confidence in the findings. The data imply greater
importance for along-dune sediment flux than deflation from the surrounding dune swales, and thus
do not provide supporting evidence for a pure ‘wind-rift’ model of dune formation. It is noted that as
such this does not preclude the possibility of primarily vertical accretion of linear dunes, especially at
a point-by-point basis, at certain points on dunes, at certain times. It does, however, provide a new
line of support for along-dune sand transport, which ultimately implies an extensional component to
linear dune development. Attempts to further dissect possible pathways by increasing the number
of possible pathways under investigation came only at the expense of reduced predictive power of
both models, and ultimately it was not possible to further isolate sources to any greater degree of
granularity with any reasonable degree of confidence.
As such, the findings suggest the potential for modern sediment provenancing studies to directly address aeolian geomorphological questions of landform development. This applies beyond the question of linear dune formation, and may apply to other bedforms and aeolian deposits such as loess. Although not addressed here, the scope for the combination of such studies with geochronological methods offer potentially valuable new means of adding long-term temporal controls over studies of aeolian sediment pathways. Whilst this study deliberately targeted a ‘typical’ linear dune in the central Simpson, it is also possible that careful locational choice (for instance, in dunefields where sediment sources are characterized by more marked variability in local geology) may have even more power in determining aeolian transport pathways.

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This paper is dedicated to the memory of the late Russell Field, without whose logistic expertise the fieldwork for this project would have never happened, and whose company made long drives and long field days a positive pleasure.

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References


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Testing models of linear dune formation by provenance analysis with composite sediment fingerprints

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Highlights

- Two sediment fingerprinting methods used to determine sources of linear dune sand.
- Models consistent in supporting along-dune sediment flux.
- Little evidence of wind-rift mechanisms of linear dune formation.
- Sediment fingerprinting methods can address questions in aeolian geomorphology.

Key words: Linear dunes, Dune extension, Sediment provenance, Monte Carlo simulation.
Abstract

The formative mechanisms of linear (longitudinal) dunes and dunefields remain uncertain, and multiple hypotheses have been proposed. A central debate is the degree to which dunes act as along-dune sediment transport corridors, implying that dunes grow primarily by extension, or whether they are comprised of locally-derived sands moved from adjacent interdunes (the ‘wind-rift’ model). Sediment fingerprinting studies, with origins in fluvial science, have been shown to offer the possibility to trace the provenance of aeolian sands, and thus elucidate transport pathways.

Two models (a Monte Carlo framework and a Generalized Likelihood Uncertainty Estimate framework) are used here to provide quantitative estimates of the sediment sources that have supplied a linear dune in the central Simpson Desert of central Australia. Four possible sources are identified that may have supplied the dune; two adjacent interdunes, one upwind low ridge of sand, and a merging upwind dune. Two sites near the dune’s crest are used as the target and provided twenty surface samples for analysis. Following geochemical assay, stepwise discriminant function analysis identified optimum elemental sediment fingerprints for a variety of possible sediment pathway configurations.

Results suggest that the sands of the dune are sourced predominantly from upwind dunes and sand sources, and that likely contributions from neighbouring dune swales are typically <20%. As such, wind-rift mechanisms of linear dune formation are not supported by these data. More complex sediment pathway configurations (i.e., other than a binary approach: interdune vs. along-dune), whilst confirming the initial findings, had reduced discriminatory power. Further separation of source pathways (e.g., identifying the relative roles of different upwind sources) was not possible with any confidence.

The findings suggest recent sediment accretion of a linear dune dominated by along-dune sand flux, and thus support an extensional component for the development of such dunes. Whilst it is noted that at a point-by-point basis this might not exclude accretion by vertical growth, as some have
observed, there is no clear support for a substantive contribution to the dune sands from adjacent interdunes. Moreover, the use of contemporary sediment fingerprinting methods to question hypotheses of aeolian geomorphology suggests that such methods have great potential for addressing other terrestrial geomorphological questions where identifying sediment pathways can provide vital insight.
Testing models of linear dune formation by provenance analysis with composite sediment fingerprints

1. Introduction

Linear (longitudinal) dunes are probably the most abundant desert dune morphology, and yet the mechanisms of formation and development of these dunes remains unclear. Multiple hypotheses, probably working in conjunction, and perhaps at different temporal and spatial scales, have been proposed for the formation of linear dunes. An equally diverse range of methods have been used to investigate the problem, including field-based monitoring of dunes (Craddock et al., 2015), time series of remotely sensed images (Lucas et al., 2015), geophysical surveys to reveal internal sedimentary structures using radar (Bristow et al., 2000, Bristow et al., 2007a, Bristow et al., 2007b, Hollands et al., 2006) and gravity surveys (Yang et al., 2011), chronostratigraphic surveys (Telfer, 2011), numerical modelling (Werner, 1995) and sediment provenance studies (Pell et al., 1999, Pell et al., 2000, Pell et al., 2001).

A crucial, and as yet unresolved, aspect of the formation of linear dunes lies in the provenance of the sands of which the dunes are formed. Amongst a diverse range of hypotheses for the formation of these features, two models emerge that can be seen as end-members of a long-standing (Melton, 1940, Mabbutt and Sullivan, 1968) debate regarding the degree to which linear dunes are extensional depositional features (Lucas et al., 2015, Telfer, 2011), perhaps serving as long-distance transport corridors for wind-blown sand, or whether they primarily accumulate by sand derived from adjacent interdunes (the so-called ‘wind rift’ model) (Wopfner and Twidale, 2001, Zhou et al., 2012, Hollands et al., 2006).

Composite sediment ‘fingerprinting’ methods, originally developed for identifying the origin of fluvial sediments (Collins et al., 1997, Walling et al., 1993), and since developing in sophistication with Monte Carlo and/or Bayesian methodologies (Motha et al., 2003, Fox and Papanicolaou, 2008), have demonstrated the ability of the methods to identify the sources of aeolian sediment. Although
the term ‘fingerprinting’ covers a diverse range of properties and methods, ranging from geochemical analyses to radionuclides and magnetic properties, today most composite sediment fingerprinting methods attempt to identify the optimal properties for discerning the relative contributions of different sources of sediment to a target location, and use these to derive quantitative estimates of contributions with robust estimates of uncertainty.

Gholami et al. (2017) demonstrated the potential of quantitative fingerprinting of aeolian dune sands in elucidating aeolian transport pathways and revealing sediment sources, and Behrooz et al. (2019) identified the provenance and pathways of aeolian dust affecting a region in eastern Iran. Gholami et al. (2019a) revealed that both long (10-10^2 km) and short (1-10 km) transport had contributed to the sands of a small erg, and highlighted the potentially complex nature of aeolian transport pathways.

Here, quantitative composite fingerprinting methods are used to test hypotheses regarding the source of sand in a linear dune in the central Simpson Desert, in central Australia. We use a sediment source fingerprinting method within two different modelling frameworks including Generalized Likelihood Uncertainty Estimate (GLUE) and Monte Carlo (MC) simulations to provide quantitative estimates of the source of dune sands.

1.1 Aims

This study aims to identify local-scale source contributions to linear dunes to improve understanding of their formative mechanisms. In order to do this, we address the following objectives:

1) Quantify contributions and uncertainties for different possible source contributions for aeolian linear sand samples in the Simpson Desert, central Australia, with two different fingerprinting approaches (GLUE and MC).

2) Assess the performance of both MC and GLUE models by goodness of fit (GOF) in the different source -sink configurations to identify the most likely sediment transport pathways.
1.2 Models of linear dune formation

The debate about the formative mechanisms of linear dunes is exemplified in research in the Australian dunefields, where debates have sometimes been most starkly expressed, but draw from evidence worldwide; observational, experimental, modelled, and based upon field and laboratory analyses. Several simultaneous debates emerged. Some suggested that linear dunes did not move laterally (Bourne et al., 2019, Tsoar et al., 2004, Fujioka et al., 2009), but other evidence was more equivocal (Nanson et al., 1992, Rubin et al., 2008, Rubin and Hunter, 1985), and some contradictory (Hesp et al., 1989), until stratigraphic evidence from geophysical surveys proved convincingly that linear dunes can indeed move laterally (Bristow et al., 2000, Bristow et al., 2005, Bristow et al., 2007a). Others sought to reconcile the degree to which linear dunes grew by extension (Tsoar et al., 2004), or by vertical accretion of locally-derived material (Pell et al., 1999, Pell et al., 2000, Zhou et al., 2012). It is worth noting that, on a point-by-point basis, all accumulation is by necessity ‘vertical’, and only on a landform scale does the term ‘vertical accretion’ really have any meaning. An extension of the latter argument, taken to its most extreme, views linear dunes as erosional rather than depositional features, an idea which has been vigorously contested (Zhou et al., 2013, Rubin and Rubin, 2013). Whilst evidence for very long-distance (inter-basin, or at least \( \approx 10^3 \) km) along-dune transport is lacking on grounds of geochemical provenance (Pell et al., 1997, Pell et al., 1999, Pell et al., 2000), and chronostratigraphic evidence over similar scales lacks support for a purely extensional mode of linear dune formation (Hollands et al., 2006), there is decisive evidence of smaller scale (<10 km) elongation from geophysical (Bristow et al., 2007b), chronostratigraphic (Telfer, 2011, Miller et al., 2018) and observational evidence (Lucas et al., 2015) that linear dunes do develop, at least in part, by extension. Taken to its extreme, the extensional argument has been applied to streaming of sand over the entire north African deserts, including across mountain ranges,
for $10^2$-$10^3$ km (Wilson, 1971, Mainguet and Callot, 1978). It is, perhaps, telling, that some papers within this debate were characterized by distinctly didactic or binary titles; “Longitudinal dunes can move sideways” (Hesp et al., 1989) or “Australian desert dunes; wind rift or depositional origin?” (Wopfner and Twidale, 2001).

The concept that linear dunes may be better considered at the dunefield scale, rather than as individual bedforms, was perhaps best highlighted by Werner’s classic simulations (1995), which demonstrated that characteristic landscapes similar to those observed in the field could emerge when forced with only large-scale forcing parameters, and that individual dune types could be considered as attractors within the phase-space of a complex system. This work, followed by numerous other modelling studies – though infrequently on linear dunes per se – suggested that numerous processes may occur concurrently, and that lateral stability vs. sideways movement, or vertical accretion vs. extension were not mutually exclusive conditions at the dunefield scale. Moreover, new evidence emerged that long-standing theories regarding linear dune orientation may not fully account for the range of alignments observed in the field, and that sediment supply also plays a role in controlling dune orientation (Courrech du Pont et al., 2014). Field evidence also revealed that even adjacent dunes may behave very differently in their accumulation record (Telfer and Thomas, 2007, Telfer et al., 2017). This paper seeks to contribute to this discussion by applying methodologies only recently applied to aeolian settings to address a specific question: at a local scale, are dunes supplied with sediment more by downwind dune sources under a net time-averaged wind regime, or adjacent interdunes fed by individual components of the wind regime?

2. Materials and Methods

2.1 Experimental set-up

To isolate the possible contributions of several different geomorphological settings, we identified a dune where (a) clear adjacent interdunes are present on both sides, (b) the upwind termination of the dune is clearly visible, where the dune ends in a low, ill-defined slipface-less sand ridge and (c)
where a downwind-joining junction also merges laterally into the target dune. This is shown schematically in Fig. 1. Samples were collected from ten locations at each site, from the top 1-5 cm of the sands.

This structure facilitates the testing of different hypotheses, as different combinations of source area definitions can be considered either together, or separately. Thus it is possible to simply consider all potential upwind source samples as a single region (i.e., A+B), and all adjacent interdunes as a possible source (i.e., C+D); or to isolate individual sources (for instance, consider A and B as distinct).

### 2.2 Field location

The Simpson Desert lies in the arid centre of the Australian continent (Fig. 2a), and the dunefield is composed almost exclusively of linear dunes, occupying an area of around 180,000 km$^2$. Part of the continent-scale whorl of linear dunes formed under anticyclonic influence, the dunes of the Simpson are oriented approximately NNW-SSE (Fig. 2b and 2c), and experience a net southerly wind regime (Hesse, 2010). The misalignment of many Australian dunefields with the modern wind regime has long been noted (Hesse, 2011), and whilst some young (Holocene) dunes of the northwestern areas of the Simpson align with current net sand-transporting winds (Hollands et al., 2006, Nanson et al., 1995), Pleistocene dunes in the southern Simpson do indeed appear out of alignment (Nanson et al., 1992). The dunefield is of considerable antiquity, with luminescence dating suggesting dunefield initiation prior to ~590 ka (Fujioka et al., 2009). Ages for the emplacement of individual dunes
suggest that some dunes have been in their current location for at least \( \sim 100 \) ka (Nanson et al., 1992, Nanson et al., 1995), and possibly substantially more (Fujioka et al., 2009).

Figure 2. The location of the dune studied, in the central Simpson Desert. (a) The location of the Simpson dunefield, in the arid centre of Australia. (b) Sampling location set amongst hundreds of SSE-NNW trending dunes. (c) More detailed inspection reveals the presence of both dune terminations and some junctions and bifurcations within the patterning. (d) Local view of the study site, with main dune crestlines highlighted with dashed lines, target dune samples (blues), possible upwind dune crest sands (yellows) and possible adjacent interdune source sands (reds).

Samples were taken from the top 1-5 cm of sand, and a .kmz file of the exact locations of samples is provided along with the online version of this article.

2.2 Analytical Methods

2.2.1 Geochemical and Sedimentological Analysis

Geochemical assays were performed at the ISO9001-accredited Analytical Research Facility at the University of Plymouth. Preparation involved fusion with lithium metaborate/tetraborate mixture, and samples were fused at 950°C for 20 min in graphite crucibles. The fused mixture was dissolved in 40 mL of 10% nitric acid and then diluted to 100 mL. A further ten-fold dilution with 10% nitric acid was required prior to analysis. Analysis of the samples was undertaken using a Thermo Scientific iCAP 7400 ICP-OES instrument and an X Series 2 ICP-MS instrument (both Thermo Scientific, UK). A total suite of 30 elements was analyzed (V, Cr, Mn, Co, Ni, Cu, Mo, Sb, Ba, Ce, Pr, Nd, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb and Lu by ICP-MS, and Na, Mg, Ca, Al, Si, Fe, K and Ti by ICP-OES).

Calibration standards were prepared by dilution of stock standards, either 10,000 or 100 mg/L and were matrix matched to the samples with the appropriate amount of flux. The performance of each
instrument was checked against the manufacturers’ specifications prior to use. A certified reference
material, BCR 667, and procedural blanks were prepared and analyzed in the same way as the
samples.

Particle size data was provided by laser granulometry using a Malvern Mastersizer 2000 with a
Hydro-G wet sample unit. Five subsamples of each sample were each analyzed five times, and mean
values taken. Ultrasonic dispersion @90% power was employed for 90 s prior to measurement, and
derivation of grain size fractions used Malvern’s general analysis model (software v5.6), with
enhanced sensitivity and assuming irregular particle shape, a refractive index of 1.56 and light
absorption of 0.01 to 0.001.

2.3 Sediment fingerprinting

In this study, once an optimum fingerprint was identified for each permutation of source/target
sample, we used two different methods to quantify source contributions; a Monte Carlo framework
(Gholami et al., 2019b), and a Generalized Likelihood Uncertainty Estimate (GLUE; Beven and Binley,
1992, Behrooz et al., 2019) model. The use of fundamentally different procedures allows assessment
of the dependence of the results on the choice of methodology, as several studies have highlighted
potential dependence of model outputs on the choice of model employed (Palazón et al., 2015,
Laceby and Olley, 2015, Haddadchi et al., 2013, Haddadchi et al., 2014).

2.3.1 Selection of the optimum composite fingerprints

A two-stage statistical process including range test and stepwise discriminant function analysis (DFA)
was applied for selecting optimum composite fingerprints (Habibi et al., 2019). In the range test
(stage 1) (Collins et al., 2010), the maximum and minimum fingerprint values in the source and
sediment samples were used for identifying outliers. Tracers failing the range test were removed
from further analysis. In stage 2, a stepwise DFA based on the minimization of Wilk’s Lambda was
used to select the optimum composite fingerprints (Gholami et al., 2017, Pulley and Collins, 2018).
Bi-plots, as a further test of the conservative behavior of the tracers included in the optimum composite fingerprints, were used to assess similarities in the relationships between tracers in the sediment and source samples (Habibi et al., 2019).

2.3.2 Quantifying source contributions of aeolian sediment using a mixing model within a Monte Carlo simulation framework

A mixing model (Collins et al., 1997) within a Monte Carlo simulation framework (Gholami et al., 2019b) was applied to quantify contributions of the potential sources in three different permutations (A+B and C+D; A, B and C+D; A, B, C and D) to twenty aeolian sediment samples (X1-X10 and Y1-Y10). The probability density functions (pdfs) (Collins et al., 2013) were constructed based on the means and standard deviations of the optimum composite fingerprints for the sediment and source samples, and these were repeatedly sampled during the Monte Carlo simulations (Hughes et al., 2009). Using Latin Hypercube Sampling (LHS), 50,000 random samples were drawn from the pdfs to permit Eq. (1) to be solved 50,000 times. The contributions of the two potential sources were calculated by the model with 95% confidence limits. The mixing model is defined as:

\[ f(X_j) = \sum_{i=1}^{n} \left( \frac{(C_i - \sum_{j=1}^{m} P_{ij} \cdot X_{ij})}{C_i} \right)^2 \]  

(1)

where \( n \) is the number of fingerprint properties (here varying from 2 to 3), \( m \) is the number of sediment sources (that is, between 2 and 4 depending on experimental set-up), \( C_i \) is the mean concentration of fingerprint property (i) in the sediment sample, \( P_{ij} \) is the relative contribution of source (j) to the sediment sample, and \( X_{ij} \) is the mean concentration of fingerprint property (i) in source (j). The mixing model must satisfy two boundary constraints: each source contribution must be between 0 and 1, and all the contributions must sum to 1.

2.3.3 Quantifying source contributions of aeolian sediment using the Generalized Likelihood Uncertainty Estimate (GLUE) model
The GLUE methodology followed Behrooz et al.’s (2019) implementation of the original methodology proposed by Beven and Binley (1992) and used the same permutations of target and source. This utilizes five steps, and is described in full in Behrooz et al. (2019), but to summarize:

1) Latin Hypercube Sampling (LHS) (Collins et al., 2013) is used to sample the parameter sets for 200,000 iterations, based upon a uniform distribution for all parameters, due to lack of a priori knowledge. It is assumed all source contributions are non-negative, and sum to unity.

2) The Nash–Sutcliffe coefficient (ENS) is used as the likelihood function, and is defined thus:

\begin{equation}
ENS = 1 - \frac{\sum(o_{obs} - o_{sim})}{\sum(o_{obs} - o_{obs})} = 1 - \frac{\sigma^2_i}{\sigma^2_{obs}}
\end{equation}

where $o_{obs}$ is the mean value of the observed tracer concentration, $o_{sim}$ is the simulated tracer concentration, $o_{obs}$ is the observed tracer concentration, $\sigma^2_i$ is the error variance for the $i$th model (i.e., the combination of the model and the $i$th parameter set) and $\sigma^2_{obs}$ is the variance of the observations.

3) The sampled parameter sets from step 1 are fed into the mixing model (Eq. (2)), and the likelihood function is calculated for each parameter set as:

\begin{equation}
C_{Sediment} = C_{Sources} \times P
\end{equation}

where $P$ is an $m$-dimensional column vector of sources contribution (sampled parameter sets), $C_{Sediment}$ is an $n$-dimensional column vector of element concentration in sediment sample and $C_{Sources}$ is an $n \times m$-dimensional matrix representing mean tracer concentration in sources (each row represents mean tracer concentration in each source).
4) Each parameter set is defined as either behavioural or non-behavioural types, depending on whether their likelihood function exceeds a threshold value (Zhou et al., 2016). Non-behavioural parameter sets were discarded.

5) For each parameter set defined as behavioural, likelihood weights are rescaled such that they sum to one, and a cumulative distribution derived for each parameter, to enable the derivation of uncertainties.

2.3.4 Assessing performance of the MC and GLUE models

A Goodness of Fit (GOF) test (Manjoro et al., 2016; Gholami et al., 2019b) was applied to evaluate performance of the two models - MC and GLUE. Although not without critics (Palazón et al., 2015), the method is widely used to give an indication of the validity of model findings (e.g., Habibi et al., 2019, Zhou et al., 2016), and here we use it relatively to assess differences of the proposed source configurations. Goodness of Fit, using the terms of Eq. (1), is thus defined:

$$ GOF = (1 - \sqrt[n]{\left(\frac{\sum_{i=1}^{n} \left(\frac{c_i - \left(\sum_{j=1}^{n} p_j x_{ij}\right)}{c_i}\right)^2}{n}\right)}) $$

3. Results

In Section 3.1, the basic geochemical and particle size data for the samples are presented. Section 3.2 discusses the development of the statistical fingerprinting methods from the geochemical data, and lastly, Section 3.3 presents the outcomes of different combination of source-target configurations and modelling frameworks.

3.1 Geochemical and particle size results

3.1.1 Geochemical assays
The results of the ICP analyses are presented in Table 1. The major species are, unsurprisingly, indicative of quartz-dominated sands (indeed the Si values seem low, with even 38% Si corresponding to an equivalent pure quartz concentration of 80%) with a more minor K-dominated feldspar component. This is broadly in line with the few other quantitative studies of sand mineral composition from central Australia, with Fitzsimmons et al. (2009) reporting 80-95% quartz and 1-15% feldspar for linear dunes of the Strzelecki to the southeast.

<table>
<thead>
<tr>
<th></th>
<th>Na (ppm)</th>
<th>Mg (ppm)</th>
<th>Ca (ppm)</th>
<th>Al (%)</th>
<th>Si (%)</th>
<th>Fe (%)</th>
<th>K (%)</th>
</tr>
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<tr>
<td>Min</td>
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<td>229</td>
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<tr>
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<td>1.45</td>
<td>37.83</td>
<td>0.8</td>
<td>0.90</td>
</tr>
<tr>
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<td>339</td>
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<tr>
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**Range test**

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| Range test  | P   | P   | P   | F   | F   | F   | F   |

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| Range test  | F   | F   | F   | F   | F   |

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<td>74</td>
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<td>675</td>
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<td>183</td>
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Table 1: Minimum, mean and maximum concentrations of the geochemical tracers in all of the source and target sediment samples. p and f indicate passing and failing the range test, respectively; see Section 3.2.1.

3.1.2 Physical sediment characteristics

Figure 3. Particle size distributions for all samples. Sand source samples (a) A and (b) B are dominated by very fine – medium sands, with a marked positive tail towards coarse sands, and whilst the interdune source samples (c) C and (d) D are also dominated by very fine – fine sands, here there is a negative tail in the distribution, with up to 20% silt in some samples. The target dunes (e) X and (f) Y are the best sorted, with little other than very fine – medium sand.

All samples (Fig. 3) are characterized by a dominance of fine sands (31.5 – 64.6%; mean = 48.7%) and very fine sands (11.5 – 50.7%; mean = 30.7%). In total, sands comprise 78.7 – 100% of the sediments (mean = 96.0%), and silts comprise 0 – 20.4% (mean = 3.9%). The interdune samples (C and D; Figs. 3c and 11d), however, are typified by an increased silt component (averaging 10.2%, and up to 20.4% in one sample) compared to the source and target dune sands where silts average just 0.8% and the maximum observed value is 3.6%. A slight positive tail exists for all candidate source samples (A-D), with a minor component of coarser sands; this is in line with well-reported trends in linear dunes/interdunes (e.g., Lancaster, 1982, Folk, 1971).

3.2 Discrimination of sediment sources by range test and stepwise DFA

3.2.1 Range test
Prior to applying a statistical procedure for selecting final fingerprints, a range test (Collins et al., 2010; Gellis and Noe, 2013) was used to identify outliers and, therefore, significantly non-conservative tracers for exclusion from further analysis. Here, the maximum and minimum tracer concentrations in the source and sediment samples were used for identifying outliers (Table 1). Tracers failing the range test (i.e., tracer concentrations measured for the target sediment samples that fell outside the corresponding ranges of the source sample tracer concentrations) were removed from further analysis (Gholami et al., 2019a, Gholami et al., 2019b, Nosrati et al., 2018).

Five tracer elements were identified as significant for the three models of sediment pathway, but only one (Na) is consistent throughout. Antimony (Sb) and potassium (K) are identified as the other most significant tracers for the two-source scenario, molybdenum (Mo) as the additional tracer in the three-source model, and barium (Ba) in the four-source configuration. The likely sources of these elements are considered in Section 4.1, though for now it is worth noting that whilst some mobility of soluble Na salts cannot be ruled out, Sb, with a near-equal predictive power, is very insoluble in the natural environment. It is likely significant that Na and Ba together have lower predictive power in the case of the four-source scenario in the later interpretation of results, as indicated by the markedly lower sum of the Wilk’s Lambda; the implications of this are considered in Section 4.1. Fig. 4 shows scatterplots of the three- and four-source permutations of the stepwise DFA; the two-source model yielded a single predictive discriminant function.
<table>
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<tr>
<td><strong>With two potential sources (A+B and C+D)</strong></td>
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<tr>
<td>1</td>
<td>Na</td>
<td>0.269</td>
<td>&lt;0.001</td>
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<tr>
<td>2</td>
<td>Sb</td>
<td>0.230</td>
<td>&lt;0.001</td>
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<td>3</td>
<td>K</td>
<td>0.204</td>
<td>&lt;0.001</td>
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<tr>
<td><strong>With three potential sources (A, B and C+D)</strong></td>
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<td></td>
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<tr>
<td>1</td>
<td>Na</td>
<td>0.262</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>2</td>
<td>Mo</td>
<td>0.186</td>
<td>&lt;0.001</td>
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<tr>
<td><strong>With four potential sources (A, B, C and D)</strong></td>
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<tr>
<td>1</td>
<td>Na</td>
<td>0.13</td>
<td>&lt;0.001</td>
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<tr>
<td>2</td>
<td>Ba</td>
<td>0.068</td>
<td>&lt;0.001</td>
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Table 2: Results of DFA for selecting optimum composite fingerprints with two (A+B and C+D), three (A, B and C+D) and four (A, B, C and D) potential sources.

Figure 4: Scatterplots were constructed from first and second functions in the stepwise DFA, (a) with three potential sources (A, B and C+D); and (b) with four potential sources (A, B, C and D). With two potential sources (A+B and C+D), scatterplots are not applicable because there is a single
discrimination function. These functions correctly classified 97.4, 84.6 and 92.3% of source samples for two, three and four potential sources, respectively.

3.2.2 Conservative behaviour of optimum composite fingerprints in the sediment and source samples

Results from the bi-plot test are presented in Fig. 5. Plots wherein the source and sediment samples do not fall in the same general space suggest non-conservative behaviour of the tracers in question.

Figure 5: Bi-plots for all pairings of the geochemical tracers in the final composite signature, measured on the source and target sediment samples: (a), (b) and (c) with two potential sources (A+B and C+D), (d) with three potential sources (A, B and C+D) and (e) with four potential sources (A, B, C and D).

3.3 Source contributions from different models and various sediment pathway configurations

Three different source-target configurations are considered here, each with the two models proposed; Monte Carlo modelling and the GLUE framework.

3.3.1 Two-source configuration: upwind and adjacent sources (A+B; C+D)
Figure 6: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A+B and C+D indicate two potential sources for aeolian sediment samples.

The results of the two-source configuration from both models are encouragingly consistent (Figs. 6 and 7); both imply a system dominated by dune sands sourced from upwind locations (both the upwind dune snout (A), and the merging dune (B)). By either assessment, 16 of the 20 samples are clearly dominated (>70%) by sediments with affiliation to these sources, with X6 (most markedly), Y2, Y6 and Y7 as notable exceptions. Both modelling approaches are consistent in the identification of which samples share greater affinity with the two possible sources. GLUE estimates are typically characterized by their smaller uncertainties.

3.3.2 Three-source configuration: dune snout, merging dune and adjacent sources (A; B; C+D)

Figure 7: GLUE results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A+B and C+D indicate two potential sources for aeolian sediment samples.

Figure 8: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B and C+D indicate three potential sources for aeolian sediment samples.
Figure 9: GLUE results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B and C+D indicate three potential sources for aeolian sediment samples.

The three-source configuration (Figs. 8 and 9) offers much support for the two-source scenario, but also offers further information. With both Monte Carlo and GLUE methodologies, source B – the merging dune – is seen to dominate the likely source contributions. Extreme uncertainties – especially for the Monte Carlo method - are undoubtedly wider, but interquartile ranges (indicated by the blue box on the box-and-whisker plots of Figs. 7 and 8) are generally supportive of a dominant source contribution coming specifically from the merging dune (source B), beyond that contributed from the immediate upwind sand source (source A). Sample X6, especially, remains a clear outlier to the general trend, with greater similarity to the interdune samples.

3.3.4 Four-source configuration: dune snout, merging dune and eastern and western interdune

Figure 10: Monte Carlo simulation results for sand dune source contributions with 95% confidence limits (with percentiles 2.5, 25, 50, 75 and 97.5). A, B, C and D indicate four potential sources for aeolian sediment samples.

Results from the four-case scenario are more complex, and characterized, especially in the case of Monte Carlo modelling (Fig. 10), by much greater uncertainties. Broad agreement remains that the contribution of the upwind sources (that is, A and B) dominates that from the interdunes (that is, C and D), but interquartile variance in the estimates typically exceeds 50% and, in some cases, approaches 100% for the upwind sources. GLUE estimates (Fig. 11) also suggest greater importance
of the upwind sources, and has tighter constraints on uncertainty, but it is noticeable that variance is
greater under this scenario than others approached with the GLUE methodology (Figs. 7 and 9).
Despite the greater uncertainties, the relative contribution of the upwind sources (the immediately-
upwind low sand pile, and merging dune) is apparently somewhat reversed under this approach,
with a greater role indicated for the immediate upwind source. Both modelling approaches suggest a
slightly higher input from the western interdune, compared to the eastern side, with the notable
exception of sample X6, with a median contribution of around 50% total from the eastern interdune
and just 20-30% from the west.

4. Discussion

The performance of the models is considered first, before considering the implications of the most
robust findings for models of linear dune formation.

4.1 Sediment fingerprinting model performance

The elements identified as the most significant tracers vary from abundant mineral-forming alkali
metals (Na and K), to much scarcer alkaline earth metals (Ba), transitional metals (Mo) and
metalloids (Sb); all are relatively enriched in the source sediments relative to the target dune sands.
The alkali metals are likely associated with weathering products from feldspars and micas, and Ba
may substitute for K in the lattice of these minerals (Kasper-Zubillaga et al., 2007). Indeed, K/Ba ratio
(along with K/Rb) in aeolian K-feldspar sands was one of the indices identified by Muhs (2017) as the
most promising for identifying the provenance of North American dune sands. Whilst the possibility
of a soluble sodium component in the sands cannot be entirely discounted, most of the other tracers identified are insoluble in this environment, and Muhs also note the relative chemical resistance of K-feldspars (orthoclase and microcline), and likely variance in K and Ba as being attributable to source geology, and not weathering. The dominant heavy minerals in the study region belong to Pell et al.’s (2000) ‘northern Simpson’ population, in which haematite, epidote and muscovite are abundant, and garnet, tourmaline, monazite and zircon significant. Molybdenum is most often associated with Cu ores, an observation consistent with Pell et al.’s (2000) attribution of the Mount Isa block, which contains substantial Cu deposits (Gregory et al., 2008), as the ‘proto-source’ for the sands of the Simpson. Antimony is also known from the Mount Isa block, associated with Pb mineralization. In short, the tracers identified seem likely to reflect both primary mineralization and long-distance transport of heavy minerals from proto-sources, and subsequent elemental differences in sands and silts as a result of weathering.

Fig. 12 presents the results of the evaluation performance of the Monte Carlo simulation (MC) and GLUE model by GOF for the different configurations of sources (two-, three- and four-sources). Both MC and GLUE models have the highest performance associated with the simplest (two-source) configuration, with GOF values for the majority of sand samples of >80%. In the three-source model, the GOF values for majority of the samples were 50-80%, and yet poorer performance for the four-source model is indicated by GOF values typically <50%. Overall, based on the GOF values (for majority of samples >80%) and scatterplot constructed stepwise DFA (97.4% source samples were classified correctly), the two-sources grouping (A+B and C+D) is the best grouping for discriminating sources of sand dunes in the Simpson Desert.
Figure 12. The Goodness of Fit (GOF) values for the MC and GLUE models for 20 sand dunes samples 
(a) X1-X10, and (b) Y1-Y10. In the majority of cases, the two-source model is seen to provide the 
strongest predictive power, followed by the three-source scenario and lastly the four-source 
configuration.

4.2 Implications for linear dune formation

4.2.1 Interpreting the provenance analyses

The results of the six provenancing assays are shown spatially in Fig. 13.

Figure 13. Spatial representation of the median estimate of source contributions under different 
assumed sediment pathway configurations and using two different methodologies for the 
fingerprinting. The simplest situation simply compares upwind and adjacent sources using (a) Monte 
Carlo and (b) GLUE frameworks. (c) and (d) differentiate between the immediate upwind low sands 
(A) and a flanking dune that merges with the target (B). (e) and (f) treat all four possible sources 
individually. Pie charts are shaded according to the colours of the source labels in panels (a), (c) and 
(e). Under all permutations, sands from upwind sources dominate; more detailed breakdown of the 
sources is less unequivocal.

Results from the provenance analyses, using either methodology, and, broadly, under any of the 
source configurations considered, suggest a dominant source component for the dune studied from 
immediately up-wind sources; the upwind ill-defined sand ridge, and the merging dune to the 
southwest. These results are more consistent with the concept of along-dune sediment transport
than wind-riift models of dune formation, whereby the sands of the dune are derived from adjacent interdunes. Some caveats must ride with this interpretation, under any of the suggested sediment configurations, though. First, this interpretation necessarily assumes that the sands – and typically the interdunes are ~90% sand-sized (Fig. 3) - found in the interdune today are the same as those found in the interdune at the time of dune formation. Whilst no ages are available for this dune, similar dunes from the Simpson are characterized by basal (i.e., emplacement) ages of $10^4$-$10^5$ yr (Fujioka et al., 2009, Hollands et al., 2006, Nanson et al., 1992), and thus the formative timescales of such landforms are long. Are the potential sources of dune sand today (i.e., interdunes vs. dunes) the same as they were at the time of dune emplacement? This is, and must always be, a hypothetical question; it is not possible to directly assess this. It should be noted that the sediment samples taken – both source and target – are essentially surface samples, and we cannot sensu stricto conclude that the same pathways would have been followed at the time of dune emplacement at this location. The assays here address the question of recent sand transport most directly, and it is not advisable to extrapolate necessarily to the timescale of tens of thousands of years.

Second, the question of similarity of the source and target samples must be addressed. It was hypothesized that the most likely causes for the choice of tracers found to be the most suitable by the stepwise DFA (that is, Na, K and Sb for the two-source model) are most likely driven by weathering of non-quartz minerals such as feldspars (which may well be found in greater quantities in the finer-grained silts of the interdunes) and in resistant, heavy minerals found as sand-sized grains. Given the differences observed in grain sizes, might the observed results be driven not by aeolian sand transport, but by in-situ weathering of the interdunes? Some evidence that this is not the case can be drawn from the outlying sample (X6) in the target group, which, of the twenty target samples analysed, was the only one showing much clearer affinity with the interdune samples that the upwind sources. If it were the case that the differences observed between the possible sources are attributed largely to a size-fraction dependent cause, then it might be expected that this is evident in the physical properties of sample X6 – it should be more similar in texture to the
interdunes, with an enhanced fine-grained component. However (Fig. 14), this is not evident from the physical characteristics of this sample; from this, it seems most likely that the provenancing methodology is indeed identifying sediment transport-driven differences.

Figure 14. Grain size properties for sample X6, alongside those of other samples from the target site X. Although the provenance analysis identified X6 as being an outlying sample, and more likely derived from the adjacent interdunes, it is physically indistinguishable from the well-sorted sands of the other samples.

4.2.2. Differing source configurations

The dominance of upwind sources is clear across all methods, and all source configurations tested (Fig. 13). Further interpreting the three- and four-source configurations, however, is harder, and much more equivocal, likely due in part to the weaker performance of both models under these configurations (Table 2 and Fig 12). Both MC and GLUE models, under the three-source configuration, do suggest some additional information. The contribution from the merging dune for both target sites is markedly greater than that of the immediate-upwind low sand ridge for both target sites (X and Y), and both models are in agreement that this effect is more marked for the northerly target site, Y (Fig. 13). This observation could be seen as consistent with the idea of linear dunes as preferential transport pathways in the landscape. In the case of the four-source model, however, this result is no longer visible, and both upwind sources are attributed approximately equal importance as contributions. Similarly, there is no clear differentiation between eastern and western interdunes as the dominant source of the lesser lateral component of transport. Thus,
whilst the different configurations tested are unanimous in identifying a dominant role for the upwind sources, further granularity in identifying sources is not possible from these findings.

4.2.3. Results in context

We interpret the results of this study as being consistent with a model favouring along-dune sediment flux, and less supportive of ‘wind-rift’ models whereby dune sands are derived from adjacent interdunes, and accretion is primarily vertical. How, then, can these findings be reconciled with the findings of others (e.g., Craddock et al., 2015, Hollands et al., 2006) who have supported the wind-rift/vertical accretion model? It is worth considering the very different methodologies that have been employed to address the questions surrounding linear dune extension/wind-rift formation. Craddock et al. (2015), for instance, used decadal-scale (8-yr) field observation of erosion pins, and differential GPS surveying. Others have used chronostratigraphies (e.g., Hollands et al., 2006, Telfer, 2011) or stratigraphies derived from geophysical surveying (e.g., Bristow et al., 2007b).

Previous provenance studies have used geochemical and geochronological methods to assess the role of long-distance sediment transport (e.g., Pell et al., 1997, Pell et al., 2000). Inherent in these different methodologies are a vast range of timescales (from $10^0$ yr for field study – $10^9$ yr in the case of zircon U-Pb provenance analyses), and spatial scales (from $10^2$ m scale accretion in the case of field survey, to $10^3$ - $10^4$ m scale for some stratigraphic studies). The challenges in reconciling such data are self-evident, and part of a wider narrative within the aeolian community that has sometimes questioned the instructiveness of reductionist approaches (Livingstone et al., 2007). A useful exercise may, thus, be to look for similarities, not differences, in the findings of this study and the most recent study with apparently contradictory findings in this region; that of Craddock et al. (2015).

First, both studies seek to address the changes that have affected linear dunes of the Simpson Desert in the recent past – in the case of Craddock et al. (2015), over an eight-year period of observation, and here by focusing on surficial sediment. Although it is not possible to directly assess
the timeframe of observation here, late Holocene ages are recorded at depths of ~1 m in the Tirari and northern Strzelecki deserts (Fitzsimmons et al., 2007, Telfer et al., 2017), as well as the western Simpson (Nanson et al., 1995). For samples collected within the top 5 cm of the dune, it seems reasonable to infer that timescales of >100 yr are likely for the sands in this study. Both studies observe spatial scales on the order of $10^3$-$10^3$ m, but, perhaps significantly, the dune chosen to for study by Craddock et al. (2015) is located at a downwind termination, whereas this study focuses on an upwind dune termination. Craddock et al. (2015) observed ~10 cm – 1 m of net accumulation on most stakes, with some showing periodic exhumation towards the lower end of this range, but did not see evidence of dune extension during this time in the form of progradation of the dune snout; this was interpreted as dune growth by vertical accretion, which, over the timescale under consideration, is clearly the case. Craddock et al. (2015) note that their findings are not necessarily at odds with the millennial-scale chronostratigraphies of Telfer (2011), which were interpreted as showing evidence both for elongation and dune mobility without concurrent lengthening; conclusions echoing those of Bristow et al.'s (2007b) geophysical surveys, which suggested that both lengthening and vertical landform growth were possible at different times/places. Miller et al. (2018), working on a linear dune whose origin is clearly tied to the adjacent Wolfe Creek meteor impact crater by the deflection that the crater has imparted on the dune planform, were able to estimate a minimum extension rate of ~3 km over ~120 ka, or of the order of 35 m ka$^{-1}$; it is unsurprising that studies working at observational timescales of ~10 yr may not observe dune extension. The interdune areas surveyed by Craddock et al. (2015) experienced both net accumulation and deflation of a few centimetres, with no clear spatial patterning. As such, there is no specific evidence here for the source of the sand that, over their decadal-scale survey, contributed to vertical landform growth; a condition that seems necessary for the wholesale adoption of the wind-rift model. Whilst the work of Pell and colleagues on numerous Australian dunefields provides convincing evidence for a lack of continental-scale aeolian sand transport fluxes (Pell et al., 1999,
Pell et al., 2000, Pell et al., 2001), there is again no mutual exclusivity with the findings of these studies, and those suggested here. Pell et al. (1999, 2000, 2001) were considering the ultimate ‘proto-source’ of the heavy mineral assemblages of dunes, and as such, constrained by U-Pb zircon dating, considering timescales of $10^8$-$10^9$ yr. Because of evidence (Fujioka et al., 2009) that the Simpson dunes likely have an early Pleistocene initiation age, such conclusions, whilst relevant to the degree to which continental-scale wind transport has occurred, do not necessarily support the dune sands as being locally-derived over scales of $10^0$ – $10^1$ km, as has sometimes been inferred (Hollands et al., 2006). Here, we demonstrate evidence that the sands near the upwind snout of a linear dune are predominantly derived, not from the adjacent interdunes as required by a pure wind-rift model, but by downwind sediment transport, either from upwind interdune sediment sources, or by sediment flux along a merging dune. Given local spatial differences in dune accumulation histories over even the most local of scales (Telfer et al., 2017), we note that this does not preclude net vertical accumulation of dunes occurring at certain places and times, or even that such sediment might not periodically come from interdune sources.

In summary, sufficient evidence now exists from diverse sources that linear dunes can, at different times and places, grow by extension and predominantly vertical growth at landform-scale; that they can migrate laterally, and yet often do remain in the same place for $10^4$-$10^5$ yr; and that whilst we cannot rule out predominantly lateral accretion of sediment at times, that they act as downwind corridors of sediment flux, resulting in dunes that, at times, clearly grow by extension. Whilst such statements may seem paradoxical, there is no reason that they cannot all be true, given sufficient time and spatial timeframes, which both seem generously available for the formation of linear dunefields.

5. Conclusions

We demonstrate here that sediment fingerprinting studies have the potential to elucidate transport pathways at a scale relevant to understanding landform formation. Two different sediment
fingerprinting modeling frameworks (a Monte Carlo approach, and the GLUE methodology) provide consistent estimates that the upwind sources, including a low sand ridge and a merging dune, are the most significant contributions for the sands of a linear dune in the central Simpson Desert, compared to the adjacent interdunes. Both frameworks performed with greater success when considering simpler configurations of possible sources, and metrics of model performance (Goodness of Fit) suggest a high degree of confidence in the findings. The data imply greater importance for along-dune sediment flux than deflation from the surrounding dune swales, and thus do not provide supporting evidence for a pure ‘wind-rift’ model of dune formation. We note that this does not preclude the possibility of primarily vertical accretion of linear dunes, especially at a point-by-point basis, at certain points and times on dunes. It does, however, provide a new line of support for along-dune sand transport, which ultimately implies an extensional component to linear dune development. Attempts to further dissect possible pathways by increasing the number of possible pathways under investigation came only at the expense of reduced predictive power of both models, and ultimately it was not possible to further isolate sources to any greater degree of granularity with any reasonable degree of confidence.

As such, the findings suggest the potential for modern sediment provenance studies to directly address aeolian geomorphological questions of landform development. This result applies beyond the question of linear dune formation, and may apply to other bedforms and aeolian deposits such as loess. Although not addressed here, the scope for the combination of such studies with geochronological methods offer potentially valuable new means of adding long-term temporal controls over studies of aeolian sediment pathways. Whilst this study deliberately targeted a ‘typical’ linear dune in the central Simpson, it is also possible that careful locational choice (for instance, in dunefields where sediment sources are characterized by more marked variability in local geology) may have even more power in determining aeolian transport pathways.
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References


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Targets X/Y: main dune crest sands

Source C/D: adjacent interdune sands

Source A: Upwind slipface-less low sands

Source B: Upwind merging dune

Approximate net wind vector

Approximate inferred subsidiary wind vectors

Approx. scale: 1 km
Figure 3 (Color)
Figure 4 (Color)
Figure 5 (Color)
Figure 7 (Color)

% contribution

Source A+B

Source C+D

Sediment sample
Figure 8 (Color)

% contribution

Source A

Source B

Source C+D

Sediment sample
Figure 9 (Color)

Source A

Source B

Source C+D

Sediment sample
Figure 11 (Color)

Source A

Source B

Source C

Source D

Sediment sample
Figure 12 (Color)

(a) and (b) show the goodness of fit for different samples and sources. The bars represent the percentage of fit for each sample (X1 to X10 or Y1 to Y10) under different source conditions (2-sources, 3-sources, 4-sources). The legend indicates the method used (MC or GLUE) and the number of sources (2, 3, or 4).
Targets X/Y: main dune crest sands

Source C/D: adjacent interdune sands

Source A: Upwind slipface-less low sands

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Approximate net wind vector

Approximate inferred subsidiary wind vectors

Approx. scale: 1 km
Interactive Map file (.kml or .kmz)

Click here to download Interactive Map file (.kml or .kmz): Simpson GPS.kmz
Declaration of interests

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

☐ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: