

2017

Flexural behaviour of BFRP rebar reinforced concrete beams

Rudzinskis, E.

Rudzinskis, E. (2017) '

<http://hdl.handle.net/10026.1/14163>

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1. Appendices

10.01 Basalt Rebar Tensile Test



Photo 1 – BFRP Rebar Sample Ends Sheared Off During Tensile Strength Test.



Photo 2 – BFRP Rebar Pulled Out from Aluminium Encasement.



Photo 3 - Extensometer BFRP Rebar Inside The Testing Machine



Photo 4 – BFRP Spiral Sanded Off at Each End. Test Failed by one end crushed.

Damaged “teeth” on the left-hand side.



Photo 5 – Damaged Upper Tensile Strength Testing Machine Clamp.

10.02 Concrete Cubes Class C40/50 Mix

Concrete mix design was based on BS 8500-1-2005+A1 and “*Design of Normal Concrete Mixes*” design manual (refer to list of references).

5 Flow chart of procedures

11

Table 1 Concrete mix design form

		Job title Dissertation					
Stage	Item	Reference or calculation	Values				
1	1.1 Characteristic strength	Specified	Cube: 50 N/mm ² at 28 days				
	1.2 Standard deviation	Fig 3	0 N/mm ² or no data				
	1.3 Margin	C1 or Specified	(k = 1.64) × = N/mm ²				
	1.4 Target mean strength	C2	0 + 50 = 50 N/mm ²				
	1.5 Cement strength class	Specified	42.5, 52.5				
	1.6 Aggregate type: coarse Aggregate type: fine		Crushed/uncrushed Crushed/uncrushed				
	1.7 Free-water/cement ratio	Table 2, Fig 4 Use the lower value				
	1.8 Maximum free-water/cement ratio	Specified	0.45				
2	2.1 Slump or Vebe time	Specified	Slump S2, 80 mm or Vebe time s				
	2.2 Maximum aggregate size	Specified	20 mm				
	2.3 Free-water content	Table 3	225 kg/m ³				
3	3.1 Cement content	C3	225 + 0.45 = 500 kg/m ³				
	3.2 Maximum cement content	Specified kg/m ³				
	3.3 Minimum cement content	Specified kg/m ³				
			use 3.1 if ≤ 3.2 use 3.3 if > 3.1				
	3.4 Modified free-water/cement ratio		500 kg/m ³				
4	4.1 Relative density of aggregate (SSD)		2.7 known assumed				
	4.2 Concrete density	Fig 5	2375 kg/m ³				
	4.3 Total aggregate content	C4	2375 - 500 - 225 = 1650 kg/m ³				
5	5.1 Grading of fine aggregate	Percentage passing 600 µm sieve	53 %				
	5.2 Proportion of fine aggregate	Fig 6	38 %				
	5.3 Fine aggregate content	C5	0.38 × 1650 = 627 kg/m ³				
	5.4 Coarse aggregate content		1650 - 627 = 1023 kg/m ³				
Quantities		Cement (kg)	Water (kg or litres)	Fine aggregate (kg)	Coarse aggregate (kg)		
					10 mm	20 mm	40 mm
per m ³ (to nearest 5 kg)		500	225	627	341	682	
per trial mix of m ³							

Items in *italics* are optional limiting values that may be specified (see Section 7).

Concrete strength is expressed in the units N/mm². 1 N/mm² = 1 MN/m² = 1 MPa. (N = newton; Pa = pascal.)

The internationally known term 'relative density' used here is synonymous with 'specific gravity' and is the ratio of the mass of a given volume of substance to the mass of an equal volume of water.

SSD = based on the saturated surface-dry condition.

10.03 Class C28/35 Concrete Design Mix

Concrete mix design was based on BS 8500-1-2005+A1 and “*Design of Normal Concrete Mixes*” design manual (refer to list of references).

Table 1 Concrete mix design form

		Job title ...Dissertation.....					
Stage	Item	Reference or calculation	Values				
1	1.1 Characteristic strength	Specified	Cube: 35 N/mm ² at 28 days				
			Proportion defective 0 %				
	1.2 Standard deviation	Fig 3	0 N/mm ² or no data				
	1.3 Margin	C1 or Specified	(k =) × = N/mm ²				
	1.4 Target mean strength	C2	0 + 35 = 35 N/mm ²				
	1.5 Cement strength class	Specified	42.5/52.5				
	1.6 Aggregate type: coarse Aggregate type: fine		Crushed/uncrushed Crushed/uncrushed				
	1.7 Free-water/cement ratio	Table 2, Fig 4	0.68				
1.8 Maximum free-water/cement ratio	Specified	Use the lower value					
2	2.1 Slump or Vebe time	Specified	Slump S2, 80 mm or Vebe time s				
	2.2 Maximum aggregate size	Specified	20 mm				
	2.3 Free-water content	Table 3	225 kg/m ³				
3	3.1 Cement content	C3	225 ÷ 0.68 = 330 kg/m ³				
	3.2 Maximum cement content	Specified	kg/m ³				
	3.3 Minimum cement content	Specified	kg/m ³				
			use 3.1 if ≤ 3.2 use 3.3 if > 3.1				
	3.4 Modified free-water/cement ratio		330 kg/m ³				
4	4.1 Relative density of aggregate (SSD)		2.7 known/assumed				
	4.2 Concrete density	Fig 5	2375 kg/m ³				
	4.3 Total aggregate content	C4	2375 - 330 - 225 = 1820 kg/m ³				
5	5.1 Grading of fine aggregate	Percentage passing 600 µm sieve	53 %				
	5.2 Proportion of fine aggregate	Fig 6	42 %				
	5.3 Fine aggregate content	C5	0.42 × 1820 = 764 kg/m ³				
	5.4 Coarse aggregate content		1800 - 764 = 1036 kg/m ³				
Quantities		Cement (kg)	Water (kg or litres)	Fine aggregate (kg)	Coarse aggregate (kg)		
					10 mm	20 mm	40 mm
per m ³ (to nearest 5 kg)		330	225	765	350	705	
per trial mix of 0.065 m ³		21.45	14.625	49.725	22.75	45.825	

Items in *italics* are optional limiting values that may be specified (see Section 7).
Concrete strength is expressed in the units N/mm². 1 N/mm² = 1 MN/m² = 1 MPa. (N = newton; Pa = pascal.)
The internationally known term 'relative density' used here is synonymous with 'specific gravity' and is the ratio of the mass of a given volume of substance to the mass of an equal volume of water.
SSD = based on the saturated surface-dry condition.

Per 4 beams = 0.18 m³

63.0	40.50	14.5	60.3	119.7
------	-------	------	------	-------

4x (0.2x0.15x1.5) = 4x(Depth x Breadth x Length) B D
















Photo 6—Aggregate Quantities for Concrete Mix.



Photo 7 – Plasticiser “MasterPolyheed”

Control of Substances Hazardous to Health (COSHH) Assessment

Faculty/Department: Science and Engineering		School/Section: School of Engineering / Civil and Coastal Engineering	
Assessment No.		Assessor: Tony Tapp	
Description of procedure or experiment (<i>Include how long and how often this is carried out and the quantity of substance used</i>).	BASF MasterPolyheed 410, a mid range plasticizer admixture based on polycarboxylate ether, used in concrete mixes to increase workability or to lower the water/cement ratio while maintaining workability. Added to a mix at a rate of 0.5 to 2% by weight of cement by incorporating into the final 40% of the mixing water. Product is supplied in 1 litre plastic screw-top container.		
Identify the persons at risk:	Staff <input checked="" type="checkbox"/>	Contractors <input type="checkbox"/>	Public/students <input checked="" type="checkbox"/>
Name the substance involved in the process, the supplier (<i>if known</i>) and the information source.	BASF MasterPolyheed 410, supplied as a light brown coloured alkali liquid which is soluble in water. Supplier: BASF plc, PO Box 4, Earl Road, Cheadle Hulme, Cheadle, Cheshire, SK8 6QG; 0161 485 6222; product-safety-north@basf.com ; Emergency: 0049 180 2273 112		
Classification (<i>state the category of danger, tick all that apply</i>)			
 <input type="checkbox"/> Very Toxic	 <input checked="" type="checkbox"/> Irritant	 <input type="checkbox"/> Carcinogenic	 <input type="checkbox"/> Gas under pressure
 <input type="checkbox"/> Toxic	 <input type="checkbox"/> Sensitiser	 <input type="checkbox"/> Highly flammable	
 <input type="checkbox"/> Corrosive	 <input type="checkbox"/> Explosive	 <input type="checkbox"/> Flammable	
 <input type="checkbox"/> Harmful	 <input type="checkbox"/> Oxidising	 <input type="checkbox"/> Environment	
Hazard Type (<i>tick all that apply</i>)			
<input type="checkbox"/> Gas	<input type="checkbox"/> Vapour	<input checked="" type="checkbox"/> Mist	<input type="checkbox"/> Fume
<input type="checkbox"/> Dust	<input checked="" type="checkbox"/> Liquid	<input type="checkbox"/> Solid	<input type="checkbox"/> Other (Details)
Route of Exposure (<i>tick all that apply</i>)			
<input checked="" type="checkbox"/> Inhalation	<input checked="" type="checkbox"/> Skin	<input checked="" type="checkbox"/> Eyes	<input checked="" type="checkbox"/> Ingestion
<input type="checkbox"/> Other (Details)			
Workplace Exposure Limits (WELs) <i>please indicate n/a where not applicable</i>			
Long-term exposure level (8hrTWA): No limits given.		Short-term exposure level (15 mins): No limits given.	
State the Risks to Health from Identified Hazards (<i>include Risk Phrases</i>)			
R36/38 - Irritating to eyes and skin; S37/39 - Wear suitable gloves and eye/face protection.			

Control Measures: (for example extraction, ventilation, training, supervision). Include special measures for vulnerable groups, such as disabled people and pregnant workers. Take account of those substances that are produced from activities undertaken by another employer's employees. (include Safety Phrases)









Wear PPE. Avoid aerosol generation.

Can a less hazardous substance be used ? Yes ☐ No ☒

If YES why is it not being used ?:

Is health surveillance or monitoring required ? Yes ☐ No ☒

Personal Protective Equipment (state type and standard)

 <input type="checkbox"/> Dust mask		 <input checked="" type="checkbox"/> Visor	To avoid splashes.
 <input type="checkbox"/> Respirator		 <input checked="" type="checkbox"/> Goggles	EN166 class 2FT or better.
 <input checked="" type="checkbox"/> Gloves	Impermeable / chemical resistant; EN374	 <input type="checkbox"/> Overalls	
 <input type="checkbox"/> Footwear		 <input type="checkbox"/> Other	

First Aid Measures

In all cases seek medical attention if symptoms persist. **Inhalation:** Remove casualty to fresh air. **Skin contact:** Wipe off immediately; wash with soap and plenty of warm water. Seek medical attention if irritation develops. **Eye contact:** Flush with water for at least 15 minutes. Seek immediate medical attention. **Ingestion:** Rinse mouth, then drink plenty of water; seek medical attention.

Spillage/Uncontrolled Release Procedures


Do not breathe vapours. Wear PPE. Avoid discharge into watercourses or drains. Contain spill and absorb spill with an inert absorbent or cloth; place collected product into suitable container for disposal.

Storage

Store at room temperature in tightly closed original container.

Disposal of Substances & Contaminated Items

<input type="checkbox"/> Hazardous Waste	<input checked="" type="checkbox"/> Skip	<input type="checkbox"/> Run to Drain	<input type="checkbox"/> Return to Supplier	<input type="checkbox"/> (Details) Other
---	---	--	--	---

Name of Assessor: Tony Tapp	Signed: 	Date: 22/12/2016
Name of Safety Manager/ HOS/ HOD:	Signed:	Date:
Review Date:	Signed:	Date:
Review Date:	Signed:	Date:

10.04

Bending schedule

Bar schedule ref:

 Rev letter


Date prepared: 29/11/2016 Date revised:

Prepared by: E.R. Checked by: D.E

[illegible]

BFRP Rebar COSHH Assessment Form

Material Safety Data Sheet	Vulkan- Europe B.V.
Basalt Continuous Filament Fibres	Continuous Basalt Fibre Distributor
Date of print : 21-11-2016	

<p>1) Identity and Distributor information.</p> <p>Identity of the Distributor.</p>	<p>Basalt fibre components : yarns , rovings , chopped strands , fabrics , non-woven mats , nets . With epoxy : rebars of different diameters , wall ties and composite mesh.</p>  <p>Raesbergenstraat 47 2804TJ Gouda The Netherlands. Tel: +31 182 535520 Mob: +31 6 54 907 214 E-mail : j.dewit@vulkan-europe.com Web site : www.vulkan-europe.com</p>
<p>4. Emergency and First Aid Procedures.</p> <p>Inhalation :</p> <p>Skin Contact:</p> <p>Eye contact :</p> <p>Ingestion :</p>	<p>No specific treatment is necessary as this material is not likely to be inhaled, unless the material is in dust form : see infra 8.</p> <p>Wash with soap and running water .</p> <p>Immediately flush with plenty of water . Get medical attention if problem develops.</p> <p>Ingestion of this material is unlikely. If it does occur , get medical attention .</p>

<p>6. Accidental Material Release or Spillage.</p> <p>Personal protective equipment :</p> <p>Environmental protection :</p> <p>Cleaning procedures :</p>	<p>See infra 8.</p> <p>Prevent spread of basalt fibre dust and avoid dust-generating conditions .</p> <p>Vacuum clean dust. If sweeping is necessary , use a dust suppressant .</p>																		
<p>8. Exposure Limits and Personal Protective Equipment .</p> <p>Fibrous basalt (Fibrous basalt dust) , CAS No 65997-17-3 .</p> <p>Basalt fibre continuous filament :</p> <p>Size (μm)</p> <p>Personal protective clothing and equipment.</p> <p>Respiratory protection :</p> <p>Protective gloves :</p> <p>Eye protection :</p> <p>Body protection :</p>	<table> <tr> <th>OSHA PEL</th><th>ACGIH TLV</th></tr> <tr> <td>(8 h TWA)</td><td>(8 h TWA)</td></tr> <tr> <td>5 mg/m³</td><td>5 mg/m³</td></tr> <tr> <td>(respirable dust)</td><td>1 fibre /cm³</td></tr> <tr> <td>15 mg/m³</td><td></td></tr> <tr> <td>(total dust)</td><td></td></tr> <tr> <td>1 fibre /cm³</td><td></td></tr> <tr> <td>(suggested)</td><td></td></tr> <tr> <td>N/A</td><td>N/A</td></tr> </table> <p>When , through mechanical processing , basalt dust is produced and when the dust levels exceed the recommended levels , use an approved respirator and local exhaust for processing machines .</p> <p>Impervious gloves are recommended.</p> <p>Impervious glasses are recommended.</p> <p>Protect skin as much as possible by clothing.</p>	OSHA PEL	ACGIH TLV	(8 h TWA)	(8 h TWA)	5 mg/m ³	5 mg/m ³	(respirable dust)	1 fibre /cm ³	15 mg/m ³		(total dust)		1 fibre /cm ³		(suggested)		N/A	N/A
OSHA PEL	ACGIH TLV																		
(8 h TWA)	(8 h TWA)																		
5 mg/m ³	5 mg/m ³																		
(respirable dust)	1 fibre /cm ³																		
15 mg/m ³																			
(total dust)																			
1 fibre /cm ³																			
(suggested)																			
N/A	N/A																		
<p>11. Toxicology.</p>	<p>The basalt continuous filament has a diameter > 5 μm and does not split longitudinally. Only when , through a mechanical process, the filaments are broken into dust particles , is the OSHA standard for nuisance dust of</p>																		

	application . (if the respirable fraction of 5 mg/m ³ is reached)
12. Ecology.	N/A. Basalt has its origin in nature.
16. Other Information .	<p>All data in the MSDS are based on the current state of knowledge , however they do not certify product properties and they do not justify legal liability.</p> <p>Vulkan- Europe bv. as the distributor cannot control the use of the end-product, the consumer has to determine under which circumstances the product can be used safely, This Material Safety Data Sheet is exclusively intended for professional use.</p>



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Web site : www.vulkan-europe.com



Photo 8 – BFRP and Steel Reinforcement Setup in Beams B2 and B4.



Photo 9 - BFRP and Steel Reinforcement Setup in Beams B1, B2 and B4

10.07 **Concrete Cube Curing**

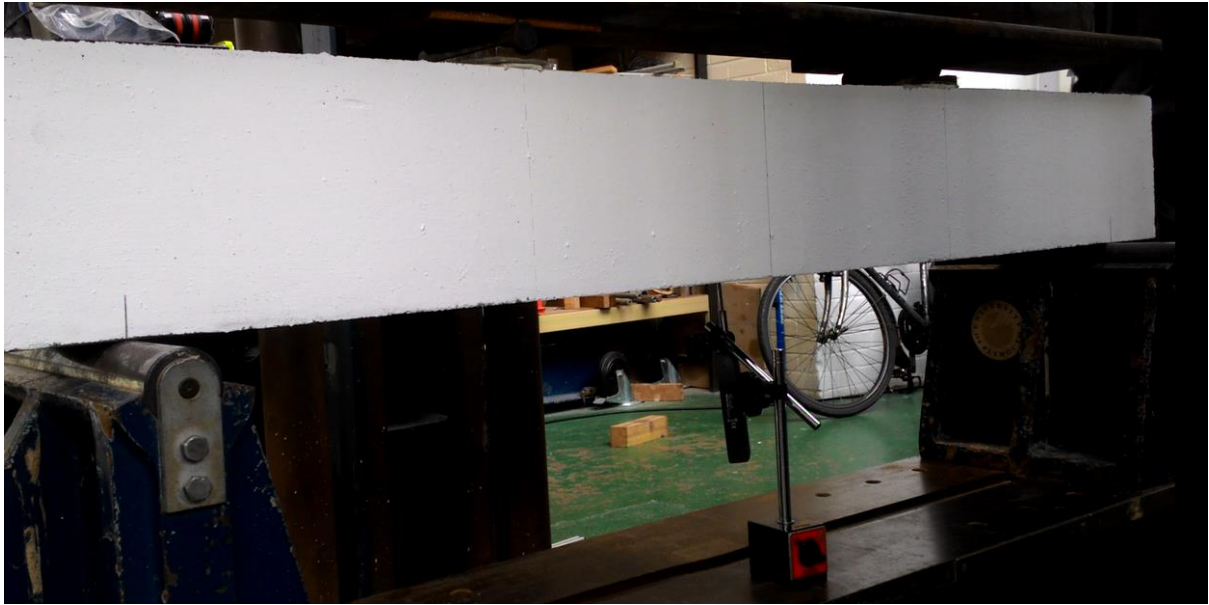


Photo 10 – Concrete (C28/35) Concrete Cube Curing Inside the Water Chamber.

10.08 **Location of external displacement gauge.**



Photo 11 – External Vertical Displacement Gauge Location 1.

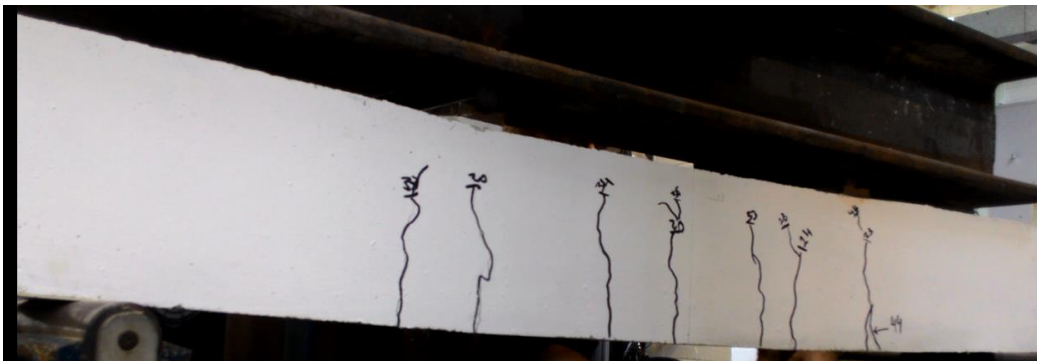
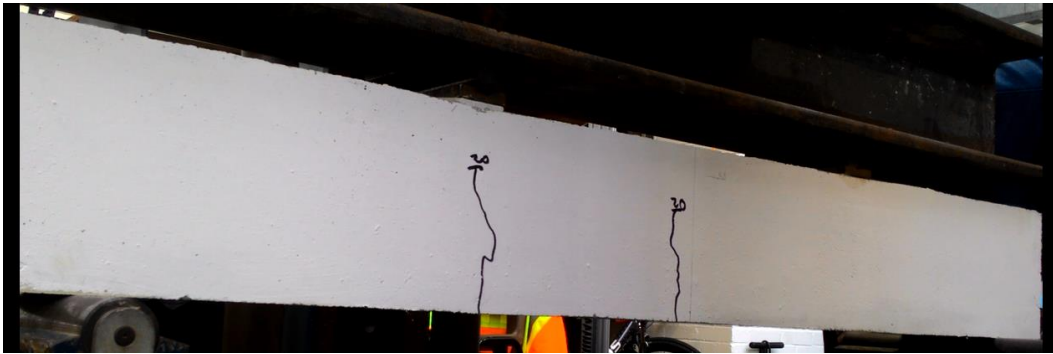


10.09 Crack Propagation

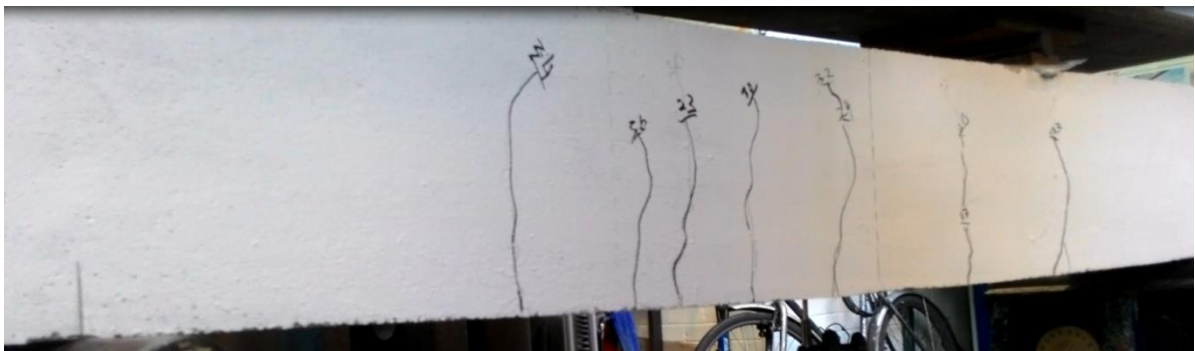
10.09.1 *Beam B1 (Control Beam)*

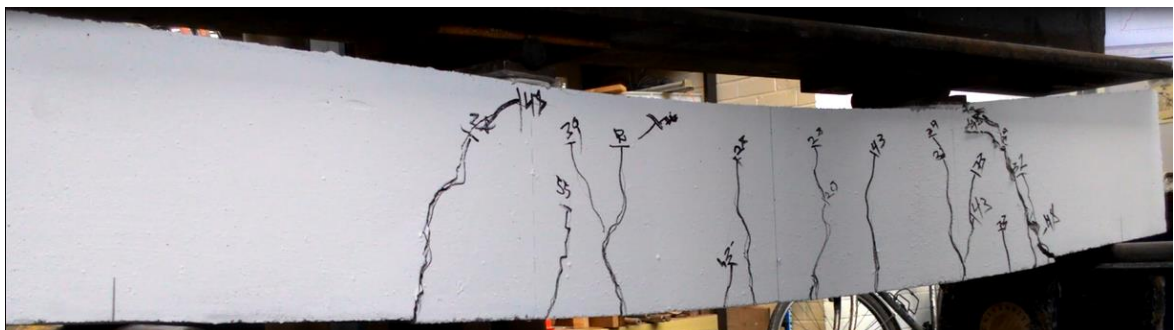
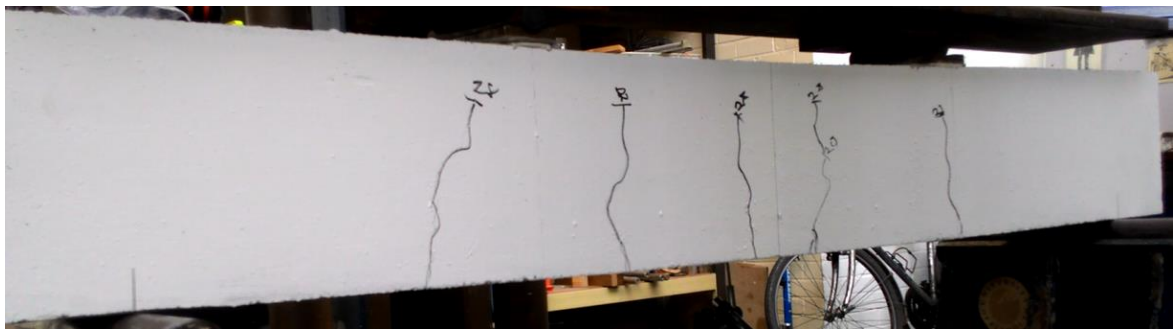


10.09.2 *Beam B2*



10.09.3 *Beam B3*





Statistical Factor=	1
---------------------	---

Fck=	28
------	----

Section Width (b)=	150
--------------------	-----

lambda	0.8
--------	-----

X < 0.45d

0.45d=	73.35
--------	-------

BM Capacity = T*(d-0.8*X/2)

BM Capacity =	7.93	(kNm)
---------------	------	-------

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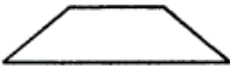
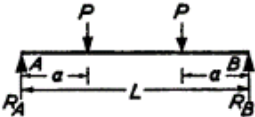
a(m)=	0.35	
-------	------	--

E=	210000000
----	-----------

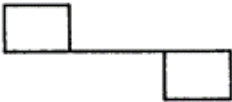
I=	0.00005625
----	------------

δ Uncracked(Max)=	0.25	(mm)
-------------------	------	------

MB max=Pa		
P in (kN)=	22.65	(kN)
P _{Total} in (kN)=	45.30	(kN)



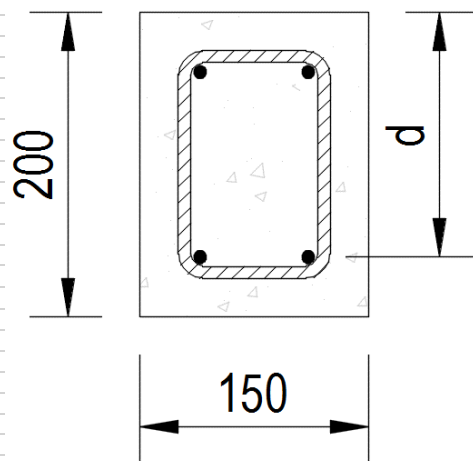
$$M_{max.} = Pa$$



$$R_A = R_B = P$$

$$\delta_{max.} = \frac{PL^3}{6EI} \left[\frac{3a}{4L} - \left(\frac{a}{L} \right)^3 \right]$$

10.11

BFRP Ultimate Load Calculations

$$d = h - c_{nom} - \phi_{link} - \phi_{bar}/2$$

$$d = 200 - 25 - 8 - (8/2) = 163 \text{ mm}$$

L=1.5	(m)
h= 200	(mm)
C _{nom} =25	(mm)
Ø= 8	(mm)

$$T = \text{Area of Steel Reinforcement} \times \text{Allowable Stress} = 101 \text{ (kN)}$$

Area of Reinforcement=	101
Allowable Stress=	1000
Materials Factor=	1

FOR EQUILIBRIUM COMPRESION MUST BE EQUAL TENSION

101 (kN)

$$C = 0.8 * X * (\text{materials factor} * F_{ck} / \text{materials factor}) \rightarrow X = (C * 10^3) / (f_{ck} * b)$$

X= 30.05952 (mm)

Statistical Factor=	1
F _{ck} =	28
Section Width (b)=	150
lambda?	0.8

0.8

$X < 0.45d$

$0.45d = 73.35$

BM Capacity = $T \cdot (d - 0.8 \cdot X / 2)$		
---	--	--

BM Capacity =	15.25	(kNm)
----------------------	--------------	--------------

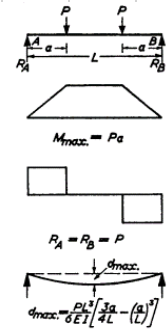
BM=Pa		
P in (kN)=	43.57	(kN)
P_{Total} in (kN)=	87.13	(kN)

a(m)=	0.35	
--------------	-------------	--

E=	50000000
-----------	-----------------

I=	0.00005625
-----------	-------------------

δ_{max}=	2.8	(mm)
-----------------------------------	------------	-------------



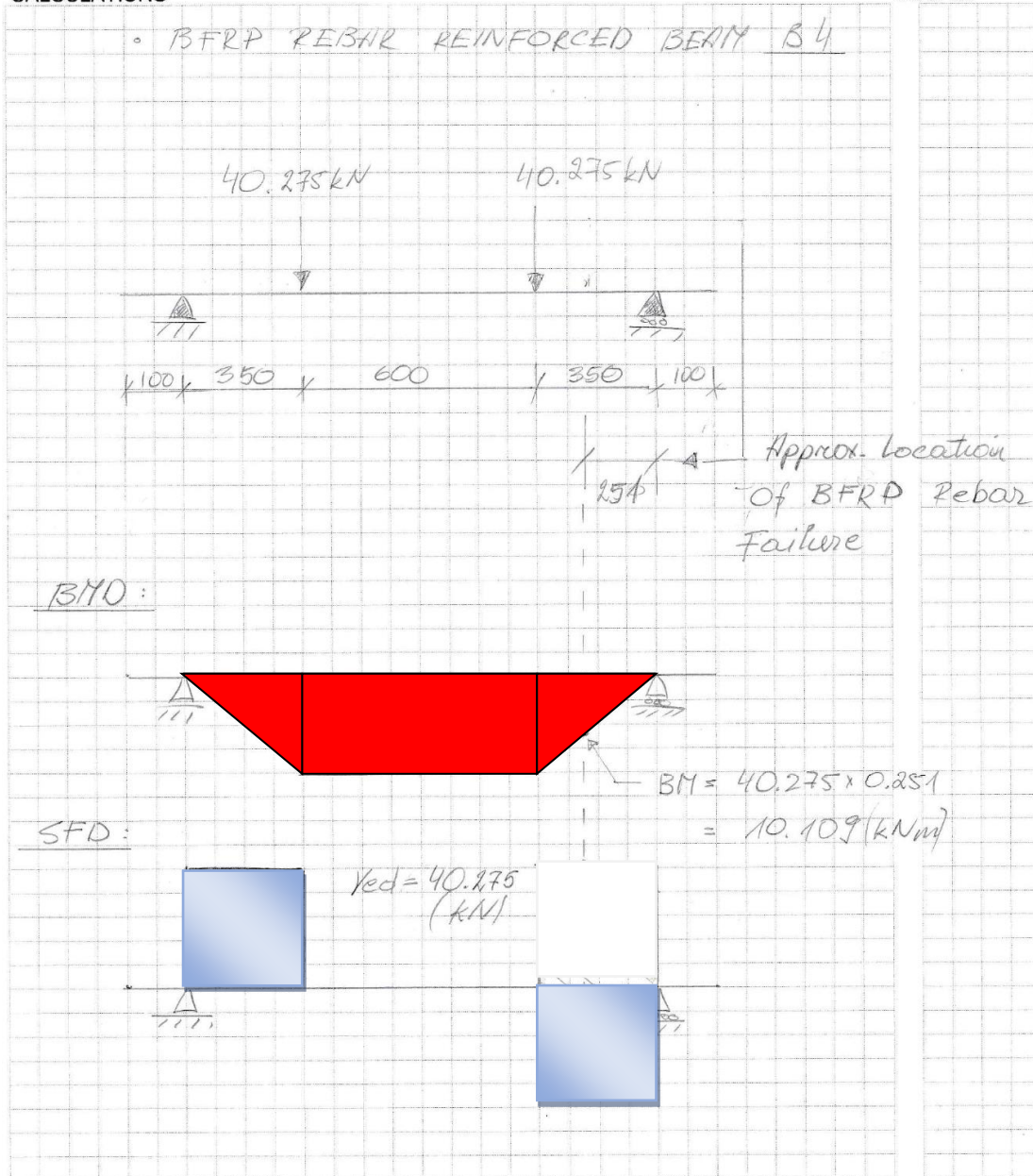
PROJECT Disseztation
 ELEMENT BFRP BEAM B4
 SHEET NO 1
 DESIGNED BY E.R.
 DATE 05/04/2017

MARINE
SCIENCE
& ENGINEERING
WITH
PLYMOUTH
UNIVERSITY

School of Marine Science & Engineering
 University of Plymouth
 Reynolds Building
 Drake Circus
 Plymouth
 PL4 8AA

CALCULATIONS

OUTPUT



PROJECT Disseztation
 ELEMENT BFRP BEAM B4
 SHEET NO 2
 DESIGNED BY E.K
 DATE 05/04/2017

**MARINE
SCIENCE
& ENGINEERING
WITH
PLYMOUTH
UNIVERSITY**

School of Marine Science & Engineering
 University of Plymouth
 Reynolds Building
 Drake Circus
 Plymouth
 PL4 8AA

CALCULATIONS

OUTPUT

BENDING CHECK

$$K = \frac{M}{bd^2 f_{ck}}$$

$$= \frac{10.109 \times 10^6}{150 \times 163^2 \times 28}$$

$$c28/35 = 28 \text{ N/mm}^2$$

$$= 0.0906$$

$$\xi = \frac{d}{2} \left[1 + \sqrt{1 - 3.53 K'} \right] \leq 0.95 d$$

$$K \leq K'$$

$$K' = 0.168$$

$$\xi = \frac{163}{2} \left[1 + \sqrt{1 - 3.53(0.0906)} \right] \leq 0.95(163)$$

$$= 148.72 \leq 154.85$$

✓

$$A_s = \frac{M}{f_{yd} \xi}$$

$$f_{yd} = \frac{f_{yk}}{\gamma_m} = \frac{1000}{1}$$

$\gamma_m = 1.0$ - since materials factor is not established.

PROJECT Dissertation
ELEMENT BFRP Beam B4
SHEET NO 3
DESIGNED BY ER
DATE 05/04/2017

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University of Plymouth
Reynolds Building
Drake Circus
Plymouth
PL4 8AA

CALCULATIONS

OUTPUT

$$\begin{aligned} \bullet f_{yk} &= 1000 \\ \bullet f_{yd} &= 1000/1 \\ &= 1000 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \bullet A_s &= \frac{10.109 \times 10^6}{1000 \times 148.72} \\ &= 68 \text{ mm}^2 < A_{s \text{ prov (Basalt)}} = 101 \text{ mm}^2 \end{aligned}$$

Calculation above signifies that
at point of failure BFRP had
more than enough capacity to
withstand the tension.

Thus this suggest that Beam failure did
not occur in bending.

shear check is required...

PROJECT Dissertation
 ELEMENT BFRP BEAM B4
 SHEET NO 4
 DESIGNED BY E.R.
 DATE 05/04/2017

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CALCULATIONS

OUTPUT

SHEAR CHECK

$$V_{ed} = \frac{V_{ed}}{b_w \cdot Z}$$

$$V_{ed} = 410.275 \text{ kN}$$

$$= \frac{410.275 \cdot 10^3}{150 \cdot 148.72}$$

$$= 1.81 \text{ N/mm}^2$$

$$A_{sw} = \frac{V_{ed} \cdot b_w \cdot S}{f_{ywd} \cdot \cot \theta}$$

$$= \frac{1.81 \times 120 \times 150}{435 \times 2.5}$$

$$= 30 \text{ mm}^2$$

$$\cdot 3 \text{ H'8 links provide: } 151 \text{ mm}^2 > 30 \text{ mm}^2$$

This signifies that at the point of failure shear links had more than enough capacity to withstand shear force applied.

10.13

Un-cracked Section Deflection Calculations

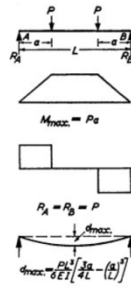
P_{Total} in (kN)= 8 (kN)

Length (m)= 1.3

a(m)= 0.35

E= 30000000

I= 0.00005625

 δ_{max} = Variable (mm)

Beam B1				
Experimental Load Applied (kN)	Actual Deflection Recorded by External Gauge (mm)	Predicted Deflection (mm)	Difference (mm)	%
4	0.11	0.10	0.01	4.6
8	0.18	0.18	0.01	4.9
12	0.25	0.26	0.01	5.3
16	0.36	0.34	0.02	4.9
20	0.48	0.42	0.06	12.2

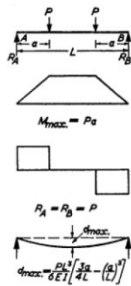
P_{Total} in (kN)= 8 (kN)

Length (m)= 1.3

a(m)= 0.35

E= 30000000

I= 0.00005625

 δ_{max} = Variable (mm)

Beam B2				
Experimental Load Applied (kN)	Actual Deflection Recorded by External Gauge (mm)	Predicted Deflection (mm)	Difference (mm)	%
4	0.1	0.10	0.00	4.9
8	0.18	0.18	0.00	2.2
12	0.27	0.26	0.01	2.5
16	0.41	0.34	0.07	16.5
20	1.28	0.42	0.86	67.1

P_{Total} in (kN)= 8 (kN)

Length (m)= 1.3

a(m)= 0.35

E= 30000000

I= 0.00005625

 δ_{max} = Variable (mm)

Beam B3				
Experimental Load Applied (kN)	Actual Deflection Recorded by External Gauge (mm)	Predicted Deflection (mm)	Difference (mm)	%
4	0.1	0.10	0.00	4.9
8	0.18	0.18	0.00	2.2
12	0.26	0.26	0.00	1.2
16	0.36	0.34	0.02	4.9
20	0.5	0.42	0.08	15.7

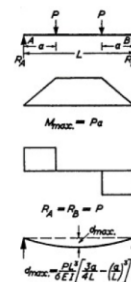
P_{Total} in (kN)= 8 (kN)

Length (m)= 1.3

a(m)= 0.35

E= 30000000

I= 0.00005625

 δ_{max} = Variable (mm)

Beam B4				
Experimental Load Applied (kN)	Actual Deflection Recorded by External Gauge (mm)	Predicted Deflection (mm)	Difference (mm)	%
4	0.1	0.10	0.00	4.9
8	0.175	0.18	0.01	5.2
12	0.26	0.26	0.00	1.2
16	0.36	0.34	0.02	4.9
20	0.5	0.42	0.08	15.7

10.14 Cracked Section Deflection Calculations

neutral axis position

$$x = 30.1$$

bii second moment of area of the cracked section

$$I_{cr} = bx^3/3 + aeAs(d-x)^2$$

$$b = 150 \text{ mm}$$

$$ae = 5.81$$

$$As = 101$$

$$d = 163$$

$$E = 50 \text{ N/mm}^2$$

$$E_{c,eff} = 8.61 \text{ kN/mm}^2$$

$$I_{cr} = 11723848.4 \text{ mm}^4$$

biii Curvature Cracked Section

$$(1/r)_{cr} = M/E_{c,eff} I_{cr}$$

$$M = 15.25 \text{ kNm}$$

$$E_{c,eff} = 8.61 \text{ kN/mm}^2$$

$$(1/r)_{cr} = 1.51E-04 \text{ /mm}$$

c The Average of cracked and uncracked curvature

ci $M_{cr} = f_{ctm} * (b_w h^2 / 6)$

$$f_{ctm} = 2.8 \text{ N/mm}^2 \quad \text{or} \quad \text{Mpa}$$

$$b_w = 150 \text{ mm}$$

$$h^2 = 40000 \text{ mm}^2$$

$$M_{cr} = 2.8 \text{ kNm}$$

cii $\epsilon = 1 - \beta (M_{cr}/M)^2$

$$\beta = 1 \quad (\text{assumed for a single short-term load}). \text{ Also for sustained loads or cyclic loading is } 0.5$$

$$\epsilon = 0.966$$

ciii $1/r = \epsilon (1/r)_{cr} + (1 - \epsilon) (1/r)_{uc}$

$$(1/r)_{uc} = M/E_{c,eff} * I_{uc}$$

$$I_{uc} = bd^3/12 \quad b = 150 \quad d = 200$$

$$I_{uc} = 100000000 \text{ mm}^4$$

$$(1/r)_{uc} = 1.77103E-05 \text{ /mm}$$

$$1/r = 1.47E-04$$

The deflection of the beam can be calculated from the total curvature using elastic bending theory which for small deflections is based on the expression:

$$M = \frac{EI d^2 y}{dx^2}$$

$$\frac{EI dy}{dx} = Mx + A$$

A – constant of integration

$$A + x = \frac{L dy}{2 dx} = 0$$

$$\therefore A = \frac{-ML}{2}$$

$$-EIy = \frac{Mx^2}{2} + Ax + B$$

B – constant of integration

$$-EIy = \frac{Mx^2}{2} - \frac{MLx}{2} + B$$

when $x = 0$ and $y = 0$

$$B = 0$$

$$y = \frac{M}{EI} \left(\frac{x^2}{2} - \frac{Lx}{2} \right)$$

Maximum Deflection Occurs at Midspan When $x = \frac{L}{2}$

$$y = -\frac{M}{EI} \left(\frac{L^2}{8} \right)$$

substitute $-\frac{M}{EI}$ with $\frac{1}{r}$ (refer to ciii)

$$y = \frac{1}{r} \left(\frac{L^2}{8} \right)$$

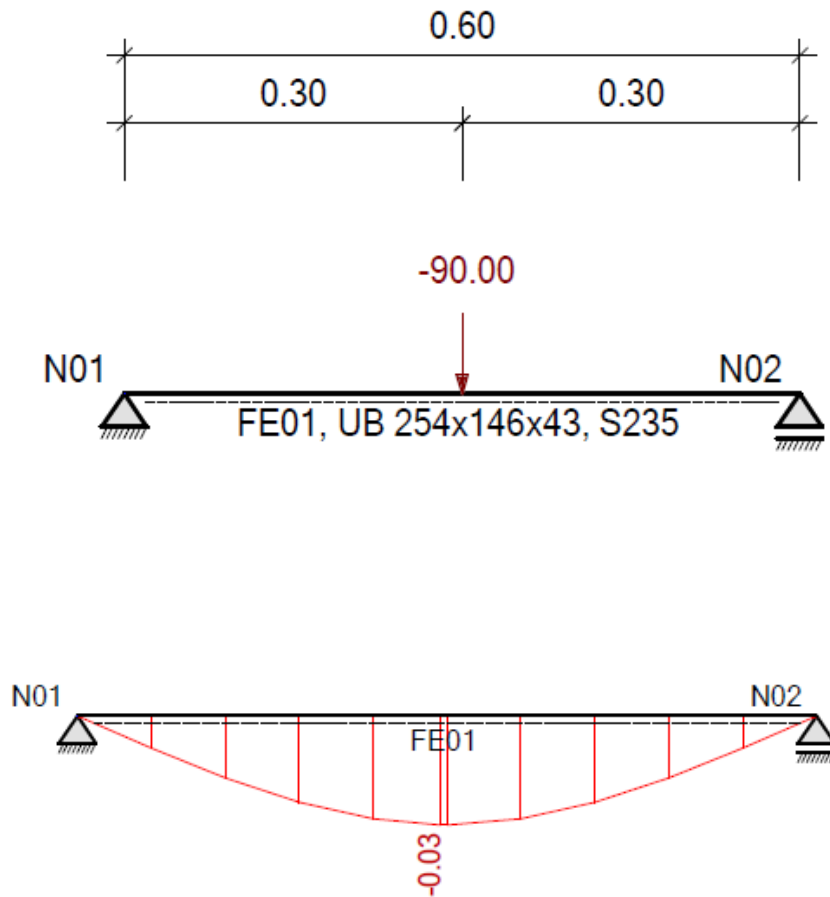
$$y = 1.47 * 10^{-4} \left(\frac{1300^2}{8} \right)$$

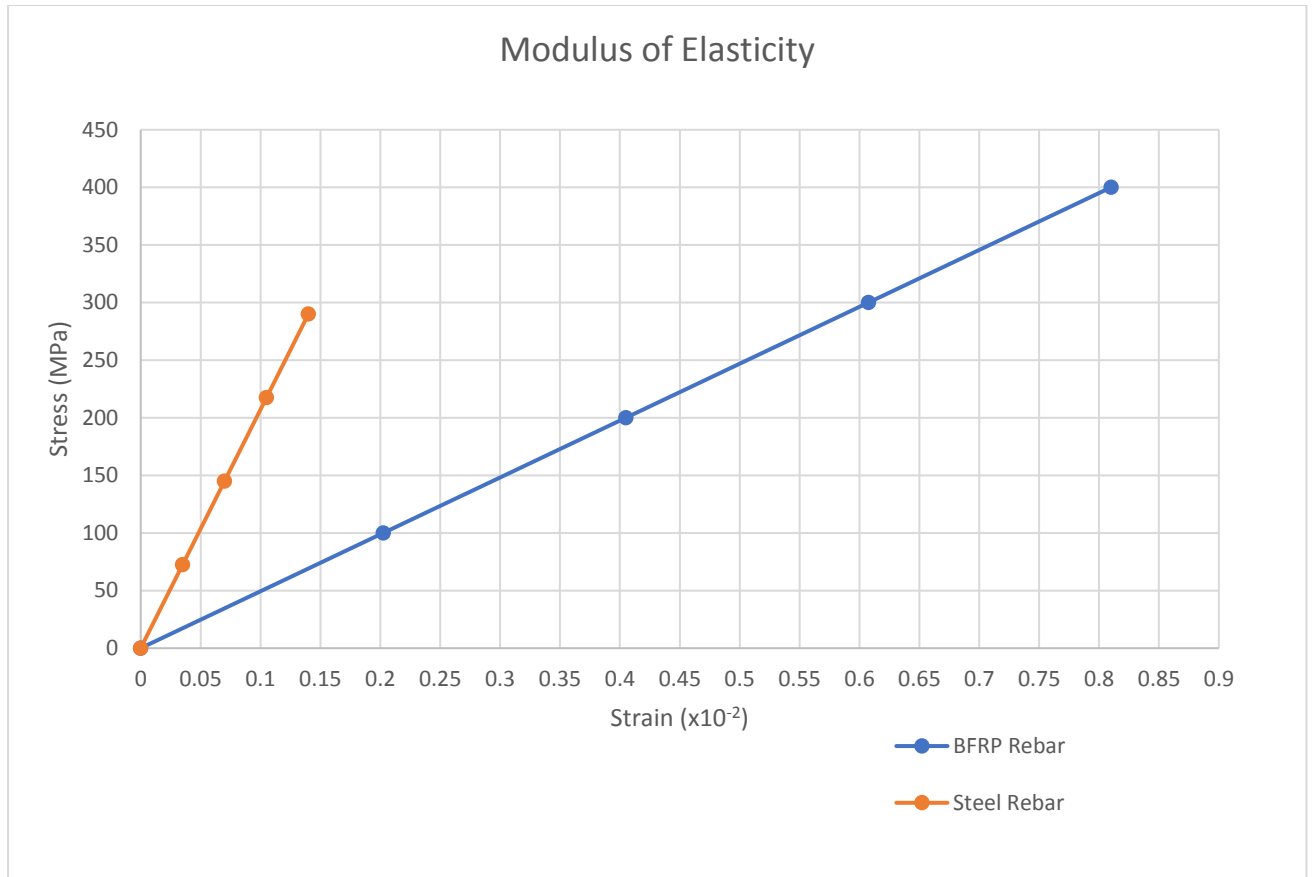
$$y = 31.0 \text{ mm}$$

10.15 Transverse Steel Beam Deflection

Analysis undertaken using Two-Frame Structural Analysis software.

(Deflection Units in mm; External Load in kN)





Graph 1 – Experimental Steel and BFRP Rebar Modulus of Elasticity.

Basalt Rebar Modulus of Elasticity:

$$E = \frac{\text{Stress}}{\text{Strain}} = \frac{400}{.00081} = 49383 \text{ MPa} = \mathbf{49.4 \text{ kN/mm}^2}$$

Steel Rebar Steel Modulus of Elasticity:

$$E = \frac{\text{Stress}}{\text{Strain}} = \frac{290}{.00014} = 207143 \text{ MPa} = \mathbf{207.1 \text{ kN/mm}^2}$$

