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Polvara, R

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Article

Vision-based Autonomous Landing of a Quadrotor on the Perturbed Deck of an Unmanned Surface Vehicle

Riccardo Polvara ^{1*}  0000-0001-8318-7269, Sanjay Sharma ¹, Jian Wan ¹, Andrew Manning ¹ and Robert Sutton ¹

¹ Autonomous Marine Systems Research Group, School of Engineering, University of Plymouth, UK; name.surname@plymouth.ac.uk

* Correspondence: riccardo.polvara@plymouth.ac.uk; Tel.: +44-07492-050558

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Abstract: Autonomous landing on the deck of an unmanned surface vehicle (USV) is still a major challenge for unmanned aerial vehicles (UAVs). In this paper, a fiducial marker is located on the platform so as to facilitate the task since it is possible to retrieve its six-degrees of freedom relative-pose in an easy way. To compensate interruption in the marker's observations, an extended Kalman filter (EKF) estimates the current USV's position with reference to the last known position. Validation experiments have been performed in a simulated environment under various marine conditions. The results confirmed the EKF provides estimates accurate enough to direct the UAV in proximity of the autonomous vessel such that the marker becomes visible again. Using only the odometry and the inertial measurements for the estimation, this method is found to be applicable even under adverse weather conditions in the absence of global positioning system.

Keywords: Unmanned Aerial Vehicle; Position Control; Computer Vision; Image Processing

0. Introduction

In the last few years, significant interest has grown towards Unmanned Aerial vehicles (UAVs), as described in [1]. The applications involving UAVs range from scientific exploration and data collection [2–4], to commercial services, military reconnaissance and law enforcement [5,6], search and rescue [7,8], patrolling [9] and even entertainment [10].

Among different UAVs topologies, helicopter flight capabilities such as hovering or vertical take-off and landing (VTOL) represent a valuable advantage over fixed-wing aircraft. The ability of autonomously landing is very important for unmanned aerial vehicles, and landing on the deck of a un-/manned ship is still an open research area. Landing an UAV on an unmanned surface vehicle (USV) is a complex multi-agent problem [11] and solutions to this can be used for numerous applications such as disaster monitoring [12], coastal surveillance [13,14] and wildlife monitoring [15,16]. In addition, a flying vehicle can also represent an additional sensor data source when planning a safe collision-free path for USVs [17].

Flying an UAV in the marine environment encounters rough and unpredictable operating conditions due to the influence of wind or wave in the manoeuvre compared to land. Apart from above, there are various other challenges associated with the operation of UAVs. For example, the inaccuracy of low-cost GPS units mounted on most UAV and the influence of the electrical noise generated by the motors and on-board computers on magnetometers. In addition to this, the estimation of the USV's movements is a difficult task due to natural disturbances (e.g. winds, sea currents etc.). This poses difficulty for an UAV to land on a moving marine vehicle with a low quality pose information. To overcome these issues, the camera mounted on the UAV and commonly used during surveillance mission [18], can also be used to increase the accuracy of the relative-pose estimates between the

34 aerial vehicle and the landing platform [19]. The adoption of fiducial markers on the vessel's deck
35 is proposed as solution to further improve the estimate results. To increase the robustness of the
36 approach, a state estimation filter is adopted for predicting the 6 degrees-of-freedom (DOF) pose of the
37 landing deck which is not perceived by the UAV's cameras. This work can be considered as the natural
38 consequence of [20], in which the developed algorithm has been tested against a mobile ground robot,
39 without any pitch and roll movements of the landing platform.

40 In terms of the paper organisation, Section 1 presents the method existing in literature about
41 autonomous landing for UAVs, while Section 2 introduces the quad-copter model, the image processing
42 library used for the deck identification, the UAV controller and the pose estimation filter. In Section
43 3 three experiments, each with a different kind of perturbation acting on the landing platform, are
44 presented and discussed. Finally, conclusions and future works are shown in Section 4.

45 1. State of the Art

46 Autonomous landing is until now one of the most dangerous challenges for UAV. Inertial
47 Navigation Systems (INS) and Global Navigation Satellite System (GNSS) are the traditional sensors
48 of the navigation system. On the other hand, INS accumulates error while integrating position and
49 velocity of the vehicle and the GNSS sometimes fails when satellites are occluded by buildings. At this
50 stage, vision-based landing became attractive because it is passive and does not require any special
51 equipment other than a camera (generally already mounted on the vehicle) and a processing unit.
52 The problem of accurately landing using vision-based control has been well studied. For a detailed
53 survey about autonomously landing, please refer to [21–23]. Here, only a small amount of works are
54 presented.

55 In [24] and [25] an IR-LED helipad is adopted for robust tracking and landing, while a more
56 traditional T-shaped and H-shaped helipad are used respectively in [26–29]. The landing site is
57 searched for an area whose pixels have a contrast value below a given threshold in [30]. In [31] a Light
58 Imaging, Detection, And Ranging (LIDAR) sensor is combined with a camera and the approach has
59 been tested with a full-scale helicopter. Bio-inspired by the honeybees that use optic flow to guide
60 landing, [32] follow the approach for fixed-wing UAV. The same has been done in [33,34] showing
61 that by maintaining constant optic flow during the manoeuvre, the vehicle can be easily controlled.
62 Hovering and landing control of a UAV on a large textured moving platform enabled by measuring
63 optical flow is achieved in [35]. In [36], a vision algorithm based on multiple view geometry detects a
64 known target and computes the relative position and orientation. The controller is able to control only
65 the x and y positions to hover on the platform. In a similar work [37], the authors were also able to
66 regulate the UAV's orientation to a set point hover. In [38] an omnidirectional camera has been used to
67 extend the field of view of the observations.

68 Four light sources have been located on a ground robot and homography is used to perform
69 autonomous take-off, tracking, and landing on a UGV [39]. In order to land on a ground robot,
70 [40] introduces a switching control approach based on optical flow to react when the landing pad is
71 out of the UAV's camera field of view. In [41], the authors propose the use of an IR camera to track a
72 ship from long distances using its shape, when the ship-deck and rotocraft are close in. Similarly, [42]
73 address the problem of landing on a ship moving only on a 2D plane without its motion known in
74 advance.

75 The work presented in this paper must be collocated among vision-based methods. Differently
76 from most of them, given the platform used it relies on a pair of low resolution fixed RGB cameras,
77 without requiring the vehicle to be provided with other sensors. Furthermore, instead of estimating
78 the current pose of the UAV, in order to land on a moving platform we employ an extended Kalman
79 filter for predicting the current position of the vessel on whose deck the landing pad is located. The
80 estimate is forwarded in input to our control algorithm that update the last observed USV's pose and
81 send a new command to the UAV. In this way, even if the landing pad is not within the camera's
82 field of view any more, the UAV can start a recovery manoeuvre that, differently from other works, is

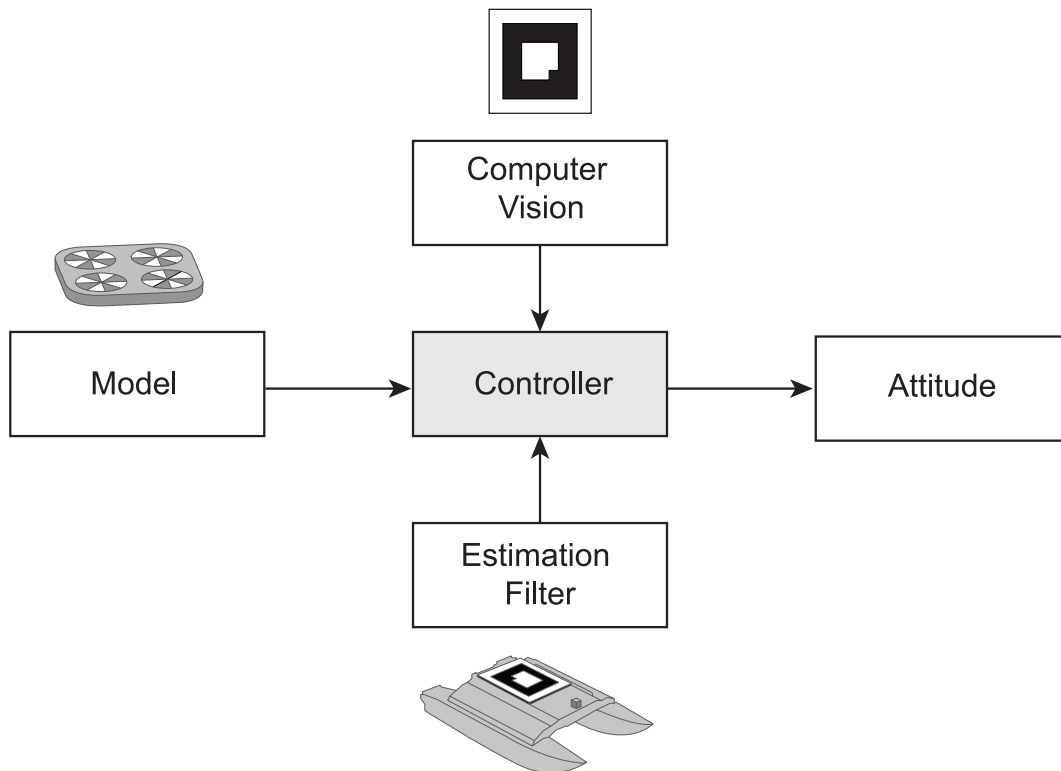


Figure 1. Different components are integrated for achieving autonomous landing on the deck of an unmanned surface vehicle.

83 taking the drone in proximity of its final destination. In this way it can compensate interruptions in
 84 the tracking due to changes in attitude of the USV's deck on which the pad is located.

85 2. Methods

86 In this section all the components used for accomplishing the autonomous landing on an USV
 87 are introduced. Initially, the aerial vehicle, together with its mathematical formulation, is described.
 88 Successively, the *ar_pose* computer vision library is presented. In the end, the controller and the pose
 89 estimation filter are discussed. A graphical representation of these components is depicted in Fig. 1
 90 and a video showing the overall working principle is available online ¹.

91 2.1. Quad-copter model

92 The quad-copter in this study is an affordable (\$250 USD in 2017) AR Drone 2.0 built by the
 93 French company Parrot and it comprises multiple sensors such as two cameras, a processing unit,
 94 gyroscope, accelerometers, magnetometer, altimeter and pressure sensor. It is equipped with an
 95 external hull for indoor navigation and it is mainly piloted using smart-phones and tablets through the
 96 application released by the producer over a WiFi network. Despite the availability of an official software
 97 development kit (SDK), the Robot Operating System (ROS) [43] framework is used to communicate
 98 with it, using in particular the *ardrone-autonomy* package developed by the Autonomy Laboratory
 99 of Simon Fraser University, and the *tum-ardrone* package [44–46] developed within the TUM
 100 Computer Vision Group in Munich. These package run within ROS Indigo on a GNU/Linux Ubuntu
 101 14.04 LTS machine. The specification of the UAV are as follow:

¹ Video showing the working principle of the algorithm: <https://youtu.be/J1ib9PIsr-8>

- 102 • Dimensions: 53 cm x 52 cm (hull included);
- 103 • Weight: 420 g;
- 104 • Inertial Measurements Units (IMU) including gyroscope, accelerometer, magnetometer, altimeter
- 105 and pressure sensor;
- 106 • Front-camera with a High-definition (HD) resolution (1280x720), a field of view (FOV) of $73.5^\circ \times$
- 107 58.5° and video streamed at 30 frame per second (fps);
- 108 • Bottom-camera with a Quatered Video graphics Array (QVGA) resolution (320x240), a FOV of
- 109 $47.5^\circ \times 36.5^\circ$ and video streamed at 60 fps;
- 110 • Central processing unit running an embedded version of Linux operating system;

111 The downward-looking camera is mainly used to estimate the horizontal velocity and the accuracy
 112 of the estimation highly depends on the ground texture and the quad-copter's altitude. Only one of
 113 the two video streams can be streamed at the same time. Sensors data are generated at 200Hz. The
 114 on-board controller (closed-source) is used to act on the roll Φ and pitch Θ , the yaw Ψ and the altitude
 115 of the platform z . Control commands $u = (\Phi, \Theta, \Psi, z) \in [-1,1]$ are sent to the quad-copter at a frequency
 116 of 100Hz.

While defining the UAV dynamics model, the vehicle must be considered as a rigid body with 6-DOF able to generate the necessary forces and moments for moving [47]. The equations of motion are expressed in the body-fixed reference frame \mathcal{B} [48]:

$$\begin{cases} m\dot{V} + \Omega \times mV = F \\ J\dot{\Omega} + \Omega \times J\Omega = \Gamma^b \end{cases} \quad (1)$$

117 where $V = [u, v, w]^T$ and $\Omega = [p, q, r]^T$ represent, respectively, the linear and angular velocities of the
 118 UAV in \mathcal{B} . F is the translational force combining gravity, thrust and other components, while $J \in \mathbb{R}^{3 \times 3}$
 119 is the inertial matrix subject to F and torque vector Γ^b .

The orientation of the UAV in air is given by a rotation matrix R from \mathcal{B} to the inertial reference frame \mathcal{I} :

$$\begin{aligned} R &= R_\psi R_\theta R_\phi \\ &= \begin{pmatrix} c\theta c\psi & s\phi s\theta c\psi - c\phi s\psi & c\phi s\theta c\psi + s\phi s\psi \\ c\theta s\psi & s\phi s\theta s\psi + c\phi c\psi & c\phi s\theta s\psi - s\phi c\psi \\ -s\theta & s\phi c\theta & c\phi c\theta \end{pmatrix} \end{aligned} \quad (2)$$

120 where $\eta = [\phi, \theta, \psi]^T$ is the Euler angles vector and $s.$ and $c.$ are abbreviations for $\sin(\cdot)$ and $\cos(\cdot)$.

Given the transformation from the body frame \mathcal{B} to the inertial frame \mathcal{I} , the gravitational force and the translational dynamics in \mathcal{I} are obtained in the following way:

$$\begin{cases} \dot{\xi} = v \\ m\dot{v} = RF^b - mge_3^i \end{cases} \quad (3)$$

121 where g is the gravitational acceleration and F^b is the resulting force in \mathcal{B} , $\xi = [x, y, z]^T$ and $v = [\dot{x}, \dot{y}, \dot{z}]^T$
 122 are the UAV's position and velocity in \mathcal{I} .

123 2.2. Augmented Reality

124 The UAV's body frame follows right-handed z-up convention such that the positive x-axis is
 125 oriented along the UAV's forward direction of travel. Both camera frames are fixed with respect to
 126 the UAV's body one, but translated and rotated in such a way that the positive z-axis points out of
 127 the camera lens, the x-axis points to the right from the image centre and the y-axis points down. The
 128 USV's frame also follows the same convention and is positioned at the centre of the landing platform.

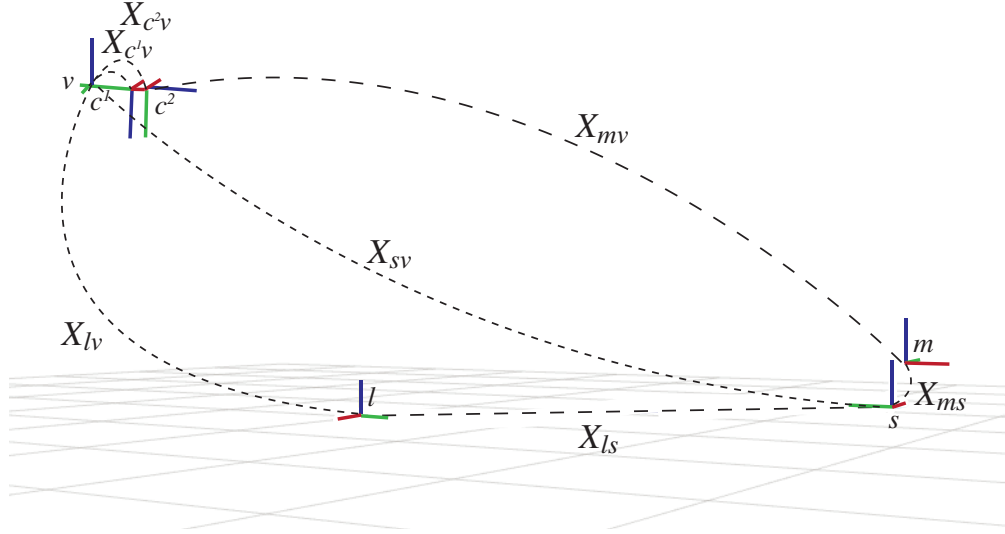


Figure 2. Coordinate frames for the landing systems. X_{lv} represents the UAV's pose with reference to the local frame and, in the same way, X_{ls} for the USV. X_{c^1v} and X_{c^2v} are the transformation between the down-looking camera and frontal cameras, respectively, and the vehicle's body frame. X_{mv} and X_{ms} are the pose from the visual marker to the UAV and to the USV, respectively. Finally, X_{sv} is the pose from the USV to the UAV.

129 Finally, it has been defined a local frame fixed with respect to the world and initialized by the system
 130 at an arbitrary location. In Fig. 2 the coordinate systems previously described are depicted.

The pose of frame j with respect to frame i is now defined as the 6-DOF vector:

$$x_{i,j} = [{}^i t_{i,j}^T, \Theta_{i,j}^T]^T = [x_{i,j}, y_{i,j}, z_{i,j}, \phi_{i,j}, \theta_{i,j}, \psi_{i,j}]^T \quad (4)$$

131 composed of the translation vector from frame i to frame j and the the Euler angles ϕ, θ, ψ .

Then, the homogeneous coordinate transformation from frame j to frame i can be written as:

$${}^i H_j = \begin{bmatrix} {}^i R_j & {}^i t_{i,j}^T \\ 0 & 1 \end{bmatrix} \quad (5)$$

where ${}^i R_j$ is the orthonormal rotation matrix that rotates frame j into frame i and is defined as:

$${}^i R_j = \text{rotxyz}(\Theta_{ij}) = \text{rotz}(\psi_{ij})^T \text{roty}(\theta_{ij})^T \text{rotx}(\phi_{ij})^T \quad (6)$$

132 Fig. 3 offers a graphical representation of the problem studied: retrieving the homogeneous
 133 matrix H offers the possibility to calculate the UAV's pose with reference to the USV expressed as
 134 translation and rotation along and around three axis respectively.

135 In this work, augmented reality (AR) visual markers are adopted for identifying the landing
 136 platform. As described in [49], "in a AR virtual objects super-imposed upon or composited with the
 137 real world. Therefore, AR supplements reality".

138 The *ar_pose* ROS package [50], a wrapper for the *ARToolkit* library widely used in human computer
 139 interaction (HCI) [51,52], is used for achieving this task. The *ar_pose* markers are high-contrast 2D
 140 tags designed to be robust to low image resolution, occlusions, rotations and lighting variation. For
 141 this reason it is considered suitable for a possible application in a marine scenario, where the landing
 142 platform can be subject to adverse conditions that can affect its direct observation.

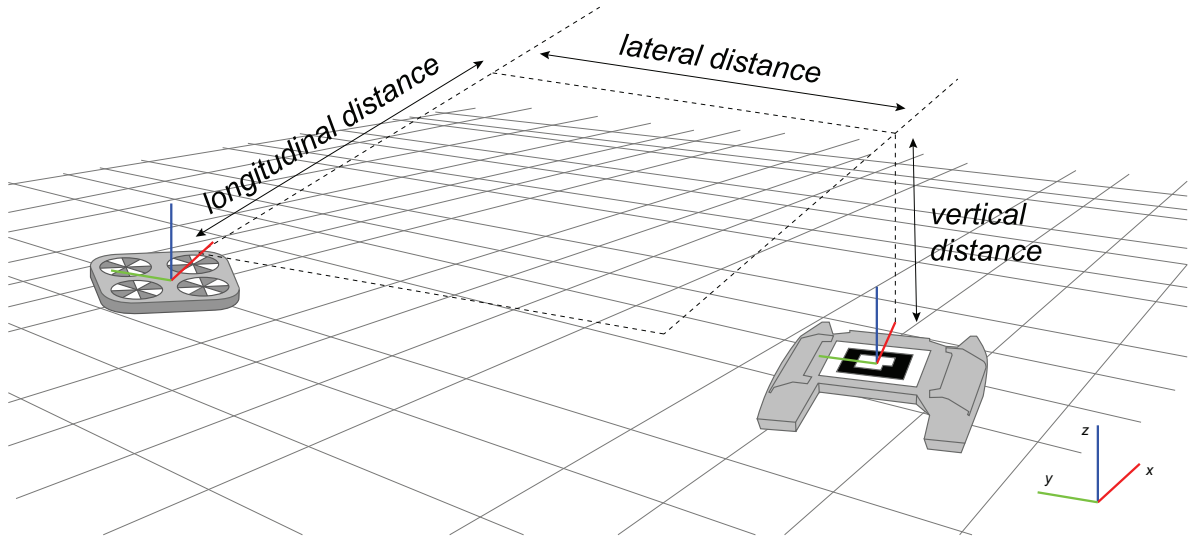


Figure 3. The image processing algorithm estimates the distances between the UAV and the visual marker.

In order to use this library, the camera calibration file, the marker's dimension and the proper topic's name must be defined inside a configuration file. The package subscribes to one of the two cameras. Pixels in the current frame are clustered based on similar gradient and candidate markers are identified. The Direct Linear Transform (DLT) algorithm [53] maps the tag's coordinate frame to the camera's one, and the candidate marker is searched for within a database containing pre-trained markers. The points in the marker's frame and camera's frame are respectively denoted as ${}^M P$ and ${}^C P$. So, the transformation from one frame to the other is defined as follow:

$${}^M P = {}^M H {}^C P = {}^M H^{-1} {}^C P = {}^C H {}^M P \quad (7)$$

143 where ${}^M H$ and ${}^C H$ represent the transforms from the marker to the camera frame and vice versa,
 144 respectively.

145 Using the camera's calibration file and the actual size of the marker of interest, the 6-DOF
 146 relative-pose of the marker's frame with respect to the UAV camera is estimated at a frequency of 1 Hz.
 147 For the current and the last marker's observation, the time stamp and the transformation are recorded.
 148 These informations are then used to detect if the marker has been lost and to actuate a compensatory
 149 behaviour.

150 2.3. Controller

151 In order to control the drone in a less complex way, the PID controller offered by the `tum_ardrone`
 152 package has been replaced with a (critically) damped spring one.

153 In the original work of [46], for each of the four degrees of freedom (roll $\bar{\Phi}$, pitch $\bar{\Theta}$, the yaw $\bar{\Psi}$ and
 154 the altitude \bar{z}), a separate PID controller is employed. Each of them is used to steer the quad-copter
 155 toward a desired goal position $p = (\hat{x}, \hat{y}, \hat{z}, \hat{\psi}) \in \mathbb{R}^4$ in a global coordinate system. The generated
 156 controls are then transformed into a robotic-centric coordinate frame and sent to the UAV at 100Hz.

157 In this paper, in order to simplify the process of tuning the controller's parameters, a damped
 158 spring controller has been adopted. In the implementation, only two parameters, K_{direct} and K_{rp} ,
 159 were used to modify the spring strength of the directly controlled dimensions (*yaw* and *z*) and the
 160 leaning ones (*x* and *y*). An additional one, *xy_damping_factor*, is responsible to approximate a damped
 161 spring and to account external disturbances such as air resistance and wind.

Table 1. The controller parameters used in the simulation performed.

Parameter	Value	Parameter	Value
K_direct	5.0	K_rp	0.3
droneMass [kg]	0.525	max_yaw [rad/s]	1.0
xy_damping_factor st19	0.65	max_gaz_rise [m/s]	1.0
max_gaz_drop [m/s]	-0.1	max_rp	1.0

The controller inputs are variations in the angles of roll, pitch, yaw, and altitude, respectively denoted as $u_{\Phi}, u_{\Theta}, u_{\Psi}$ and u_z , defined as follows:

$$u_{\Phi} = -K_{rp}(\hat{x} - x) + c_{rp}(\dot{\hat{x}} - \dot{x}) \quad (8)$$

$$u_{\Theta} = -K_{rp}(\hat{y} - y) + c_{rp}(\dot{\hat{y}} - \dot{y}) \quad (9)$$

$$u_{\Psi} = -K_{direct}(\hat{\psi} - \psi) + c_{direct}(\dot{\hat{\psi}} - \dot{\psi}) \quad (10)$$

$$u_z = -K_{direct}(\hat{z} - z) + c_{direct}(\dot{\hat{z}} - \dot{z}) \quad (11)$$

where c_{rp} and c_{direct} are the damping coefficients calculated in the following way:

$$c_{rp} = xy_damping_factor \cdot 2\sqrt{K_{rp} \cdot droneMass} \quad (12)$$

$$c_{direct} = 2\sqrt{K_{direct} \cdot droneMass} \quad (13)$$

162 Therefore, instead of controlling nine independent parameters (three for the yaw, three for the
163 vertical speed and three for roll and pitch paired together) the control problem is reduced to the three
164 described above (namely K_{direct} , K_{rp} and $xy_damping_factor$).

165 The remaining controller parameters are platform dependent variables and they are kept always
166 constant during all the trials. Ignoring $droneMass$ which does not require an additional description
167 more than its name, max_yaw , max_gaz_rise and max_gaz_drop limit the rotation and linear speed on
168 the yaw and z-axis, respectively. In the end, max_rp limits the maximum leaning command sent.

169 The controller's parameters are the same across all the experiments performed and they are shown
170 in Table 1. The K_{rp} parameter, responsible to control the roll and pitch behaviour, is kept small in
171 order to guarantee smooth movements along the leaning dimensions. In the same way, max_gaz_drop
172 has been reduced to a value of 0.1 for decreasing the descending velocity. On the other hand, the
173 max_yaw parameter, used to control the yaw speed, has been set to its maximum value because the
174 drone must align with the base in the minimum amount of time possible. The others have been left to
175 their default values.

176 2.4. Pose estimation

To increase the robustness and efficiency of the approach, an extended Kalman filter (EKF) has been adopted here for estimating the pose of the landing platform [54]. In fact, it may happen the UAV lose the track of the fiducial marker while approaching and descending on it. In order to redirect the flying vehicle in the right direction, the EKF estimates the USV current pose that is then processed and forwarded to the controller. For estimation purposes, the odometry and inertial data are fused together to increase the accuracy [55,56]. The state vector is defined as $\mathbf{x} = [x, y, z, \phi, \theta, \psi, \dot{x}, \dot{y}, \dot{z}, \dot{\phi}, \dot{\theta}, \dot{\psi}]$, with x, y, z and $\dot{x}, \dot{y}, \dot{z}$ representing respectively the global positions and velocity, and ϕ, θ, ψ and $\dot{\phi}, \dot{\theta}, \dot{\psi}$ the

attitude of the vessel. Considering the sensor readings, the estimation process satisfies the following equations:

$$\hat{\mathbf{x}}_{k|k-1} = \mathbf{F}_k \hat{\mathbf{x}}_{k-1|k-1} \quad (14)$$

$$\mathbf{P}_{k|k-1} = \mathbf{F}_k \mathbf{P}_{k-1|k-1} \mathbf{F}_k^T + \mathbf{Q}_k \quad (15)$$

$$\mathbf{K}_k = \mathbf{P}_{k|k-1} \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^T + \mathbf{R}_k)^{-1} \quad (16)$$

$$\hat{\mathbf{x}}_{k|k} = \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k (\mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_{k|k-1}) \quad (17)$$

$$\mathbf{P}_{k|k} = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_{k|k-1} \quad (18)$$

177 where k represents a discrete time instant, \mathbf{F}_k is a kinematic constant velocity model, \mathbf{H}_k is the
178 observation model, \mathbf{z}_k is the measurements vector, \mathbf{I} is an identity matrix, \mathbf{Q}_k is the process covariance
179 matrix and \mathbf{R}_k is the measurement covariance matrix.

180 The working principle of the EKF in this case is detailed below:

- 181 • the filter estimates the USV's pose at 50Hz and its encoding is saved in an hash table using the
182 time stamp as key;
- 183 • when the UAV loses the track, the hash table is accessed and the last record inserted (the most
184 recent estimate produced by the filter) together with the one having as key the time stamp of the
185 last recorded observation are retrieved;
- 186 • the deck's current position with reference to the old one is calculated using geometric relationship;
- 187 • the controller command are updated including the new relative position;

188 The procedure described above is iterated until the UAV is redirected above the visual marker and can
189 perceive it through its bottom camera.

190 2.5. Methodology

Algorithm 1 Landing Algorithm

```

1: while not landed do
2:   last_known_pose = NULL
3:   if marker_visible then
4:     last_known_pose ← detect_landing_marker()
5:     if last_known_pose < user_defined_threshold then
6:       controller.send_commands(land)
7:       landed ← true
8:     end if
9:   else
10:    usv_pose ← ekf.estimate_pose()
11:    last_known_pose ← last_known_pose + usv_pose
12:  end if
13:  trajectory ← calculate_trj(last_known_pose)
14:  attitude_cmd ← controller.calculate_cmd(trajectory)
15:  controller.send_commands(attitude_cmd)
16: end while

```

191 The following section explains how the algorithm 1 works. The code is publicly available on our
192 repository².

193 The quad-copter flies using its fixed non-tilting frontal camera, approaching the landing site on
194 the USV's deck identified only by a fiducial marker. This, which scope is to outline the landing area,
195 has to be perceived during all the landing manoeuvre. This is a requirement for precise landing despite
196 the state estimator can compensate interruption in observation. When a visual marker is detected, the
197 image processing library computes the 6-DOF relative-pose between the marker itself and the UAV.
198 The result is used to make the quad-copter approaching the marker with the right orientation. To
199 obtain this result, a damped spring controller reduces the error on the x -, y - and z -axis and on the
200 quad-copter's *yaw*. On attaining close proximity to the marker, the marker leaves the field of view of

² Github repository: https://github.com/pulver22/ardrone_tf_controller

201 the frontal camera. This is due to hardware limitation of fixed non-tilting cameras. To overcome this
202 problem, the video stream from the frontal camera is interrupted and acquired from the one located
203 under the UAV and downward-looking. The quad-copter continues the landing manoeuvre keeping
204 the marker at the centre of the second camera's FOV. Otherwise, a compensatory behaviour is adopted:
205 the EKF estimates the actual position of the USV and the drone is redirected close to it while increasing
206 its altitude. Increasing the altitude allows to enlarge the field of view of the bottom camera, that is quite
207 limited. In this way, it is guaranteed that the marker will be soon perceived and centred by the aerial
208 vehicle. When an experimentally defined distance from the marker is reached, the drone lands safely.
209 This distance depends on the side length of the marker used. In fact, with a smaller marker it would
210 be possible to decrease this value but it would become impossible to perceive the marker at longer
211 distance. We found that a marker side length of approximately 0.30 meters represents a good trade-off
212 for making the marker visible at long and close distance at the same time. As a consequence, we decide
213 to use 0.75 meters as distance for starting the touchdown phase of the descending manoeuvre, during
214 which the power of the motors is progressively reduced until complete shut-down. The use of visual
215 markers allows the estimation of the full 6-DOF pose information of the aerial and surface vehicles. In
216 this way, landing operations in rough sea condition with a significant pitching and rolling deck can
217 still be addressed.

218 3. Results and Discussion

219 All the experiments has been conducted inside a simulated environment built on Gazebo 2.2.X
220 and offering a 3D model of the AR Drone 2.0. To the scope of this work, the existing simulator has been
221 partially rewritten and extended to support multiple different robots at the same time. The Kingfisher
222 USV, produced by Clearpath Robotics, has been used as floating base. It is a small catamaran with
223 a dimension of are 135 x 98 cm, that can be deployed in a autonomous or tele-operated way. It is
224 equipped with a flat plane representing a versatile deck for UAVs of small dimension. On this surface
225 a square visual marker is placed. Previous research demonstrated a linear relationship is existing
226 between the side length of the marker and its observability. Therefore, we opted for a side length of 0.3
227 meters that represents a good compromise, making the marker visible in the range [0.5, 6.5] meters.

228 The algorithm has been tested under multiple conditions, namely three. In the first scenario, the
229 USV is subjected only to a rolling movement while floating in the same position for all the length of
230 the experiment; in the second scenario, the USV is subjected only to a pitching movement; while in
231 the last scenario the USV is subject to both rolling and pitching disturbances at the same time. Fig. 4
232 illustrates the rotation angles around their corresponding axis. In all the simulations, the disturbances
233 are modelled as a signal having a maximum amplitude of 5 degrees and a frequency of 0.2 Hz. Rolling
234 and pitching of a vessel generate upward and downward acceleration forces directed tangentially
235 to the direction of rotation, which cause linear motion knowns as swaying and surging along the
236 transverse or longitudinal axis respectively [57].

237 3.1. Rolling Platform

238 In this subsection, the results of a landing manoeuvre on a rolling floating base are reported. In
239 particular, Fig. 5 illustrates the UAV and the USV's trajectory, respectively in blue and red, in the
240 UAV's reference frame; while Fig. 6 and Fig. 7 show the controller commands and the salient moments
241 of the manoeuvre respectively.

242 The marker has been successfully recognised at a distance of 3.74 meters in front of the UAV, and
243 at 0.09 meter on its left. The displacement on the z -axis, used as reference for the altitude, was of
244 0.84 meter instead. The UAV, with the parameters reported in the previous table 1, has been able to
245 complete the landing in 25 seconds.

246 The quad-copter approaches the landing base trying to keep it at the centre (in a range of ± 10
247 degrees) of its camera's FOV. In the case the marker leaves this interval of tolerance, the UAV would
248 rotate around its z -axis in order to centre it again. The approach continues until the UAV's low

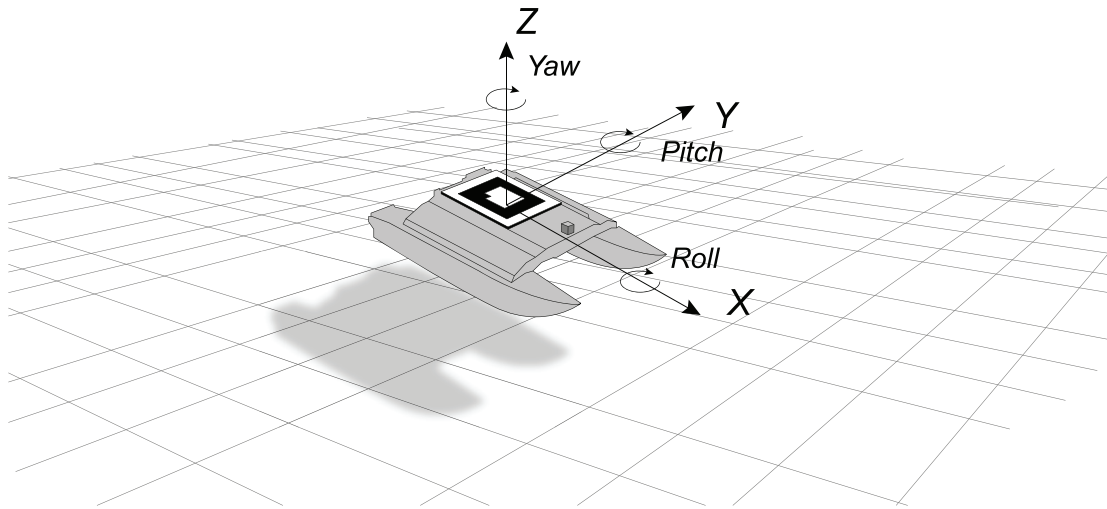


Figure 4. The movements around the vertical, longitudinal and lateral axis of the USV are called yaw, roll and pitch respectively.

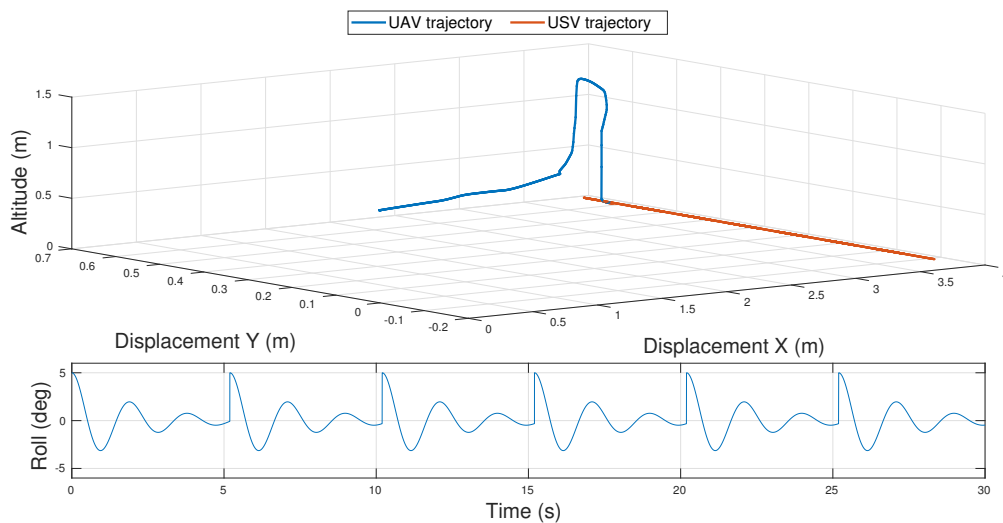


Figure 5. Above: The UAV and USV 3D trajectories, in blue and red respectively, in the UAV's reference frame. Bottom: The roll disturbances the USV is subject to.

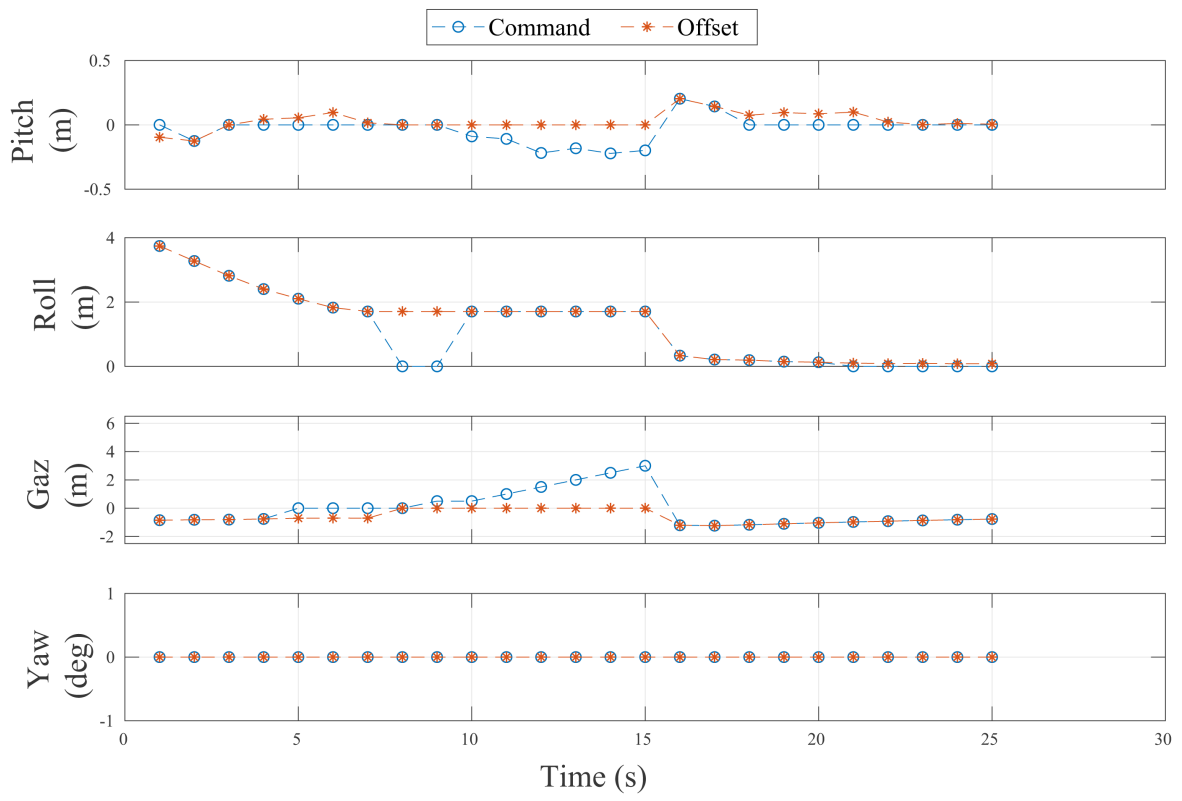


Figure 6. Controller commands and visual offsets in the experiment with a rolling landing platform.

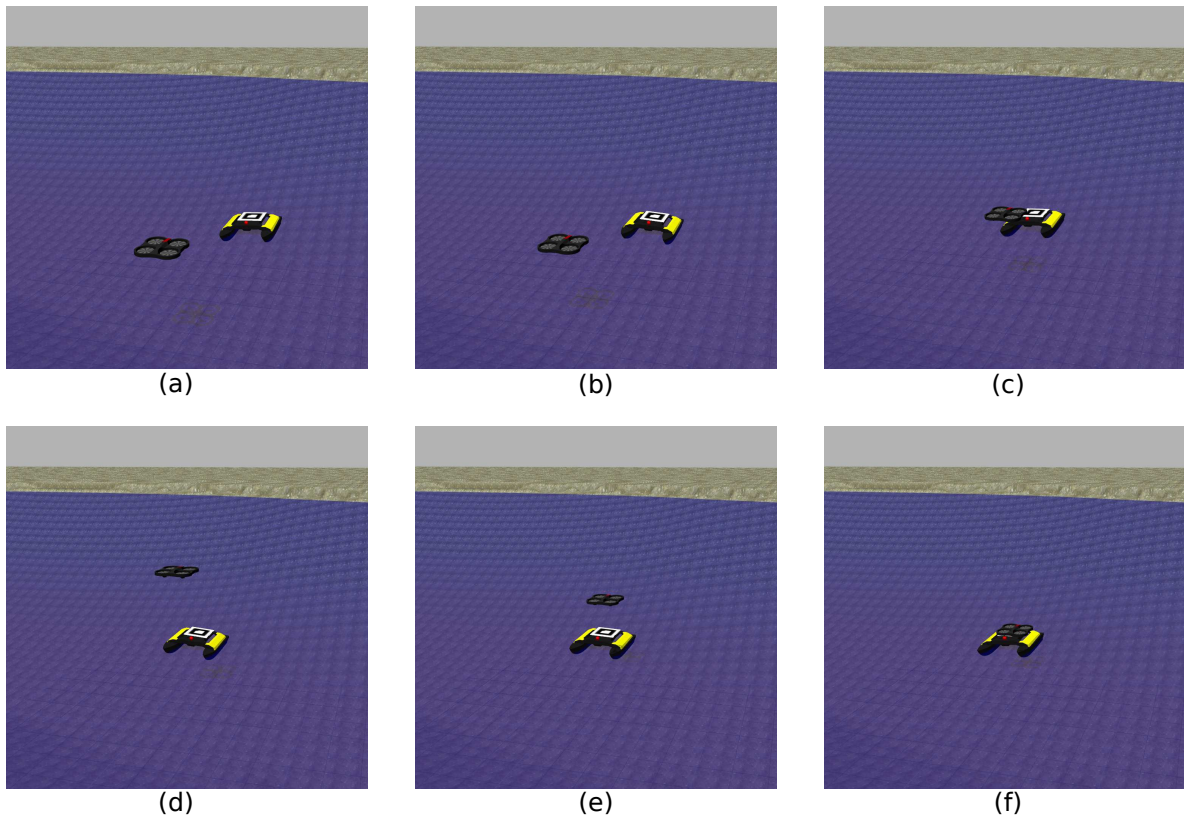


Figure 7. Landing manoeuvre of a VTOL UAV on a USV subject only to rolling disturbances.

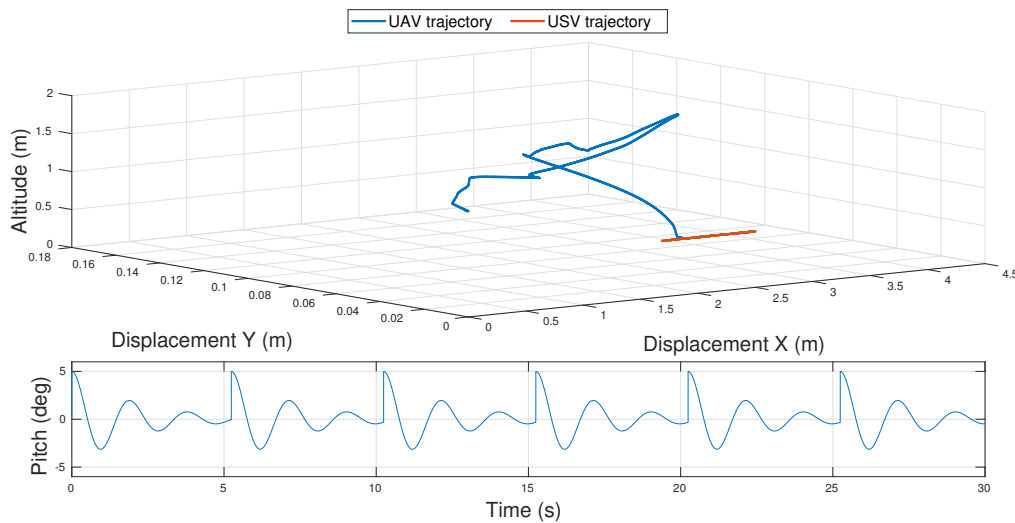


Figure 8. Above: The UAV and USV 3D trajectories, in blue and red respectively, in the UAV's reference frame. Bottom: The pitch disturbances the USV is subject to.

249 altitude prevents the marker to be seen from the frontal camera, as shown in Fig. 7-a ($t = 10$ s). At this
 250 point, the video stream is switched from the frontal camera to the one located at the bottom of the
 251 quad-copter and looking down, and new commands are generated and sent. The UAV is instructed
 252 to move towards the last known position of the landing platform but increasing its altitude in order
 253 to enlarge the area covered by its bottom camera. At $t = 15$ s, as represented in Fig. 7-b, the UAV is
 254 located exactly above the marker and it can now complete the landing phase: it descends while trying
 255 to keep the marker at the centre of its FOV, as shown in Fig. 7-c. Small velocity commands are sent on
 256 the leaning direction (x and y , respectively) in order to approach the final position with high accuracy.
 257 Finally, at $t = 25$ s the UAV reaches the minimum altitude required to shut-down its motors and land
 258 on the platform (Fig. 7-f).

259 The commands generated from the relative-pose between the UAV and the landing platform's
 260 frame are illustrated in Fig. 6. Here, the controller's commands are plotted against the perception
 261 from the camera. As it is possible to see in the figure, for most of the travel the two curves of the
 262 commands and of the observations overlap perfectly. When they do not, the marker is lost and the
 263 UAV actuates the compensatory behaviour: the estimation filter's output, namely the USV's predicted
 264 pose, is combined with the latest vision observation in order to generate new commands for the UAV.
 265 In this way it is possible to explain changing in roll, pitch and altitude in the graph. Since the UAV has
 266 the same yaw of the floating base, namely they have the same orientation along the z -axis, no rotation
 267 commands are issued for this degree of freedom.

268 Few words are reserved for the pitch's data between $t = 18$ s and $t = 22$ s, and the gaz's ones
 269 between $t = 5$ s and $t = 8$ s. In this case, the offsets are below a user-defined threshold and a null
 270 command is sent instead. The use of a threshold has been introduced for speeding up the landing
 271 phase: while testing the controller, it was noticed the UAV spent a lot of time while trying to align
 272 perfectly on the three axis with the centre of the landing plane, sometimes without any success. This
 273 has been identified as a limitation of controllers with fixed values parameters and a new more versatile
 274 solution is already planned as future work.

275 3.2. Pitching Platform

276 In this subsection an experiment with a pitching floating platform is reported. As before, the time
 277 for completing the landing manoeuvre is not considered as key-factor but the attention is on the ability
 278 of the UAV to approach and land on the USV with high precision.

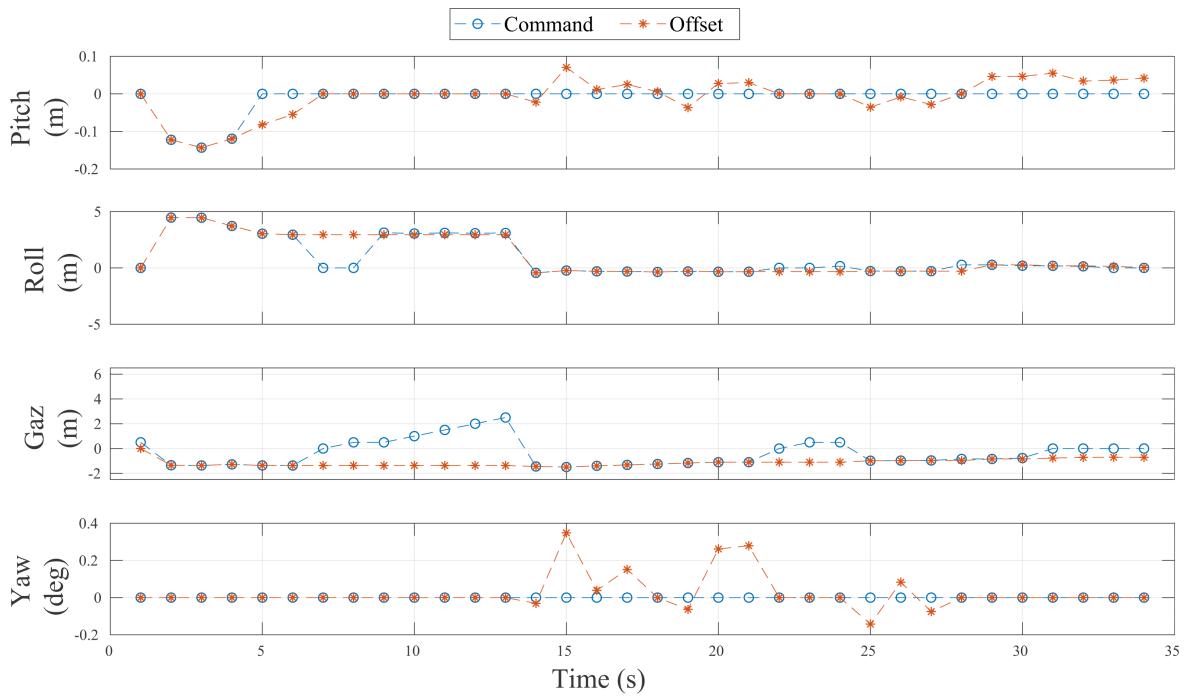


Figure 9. Controller commands and visual offsets in the experiment with a pitching landing platform.

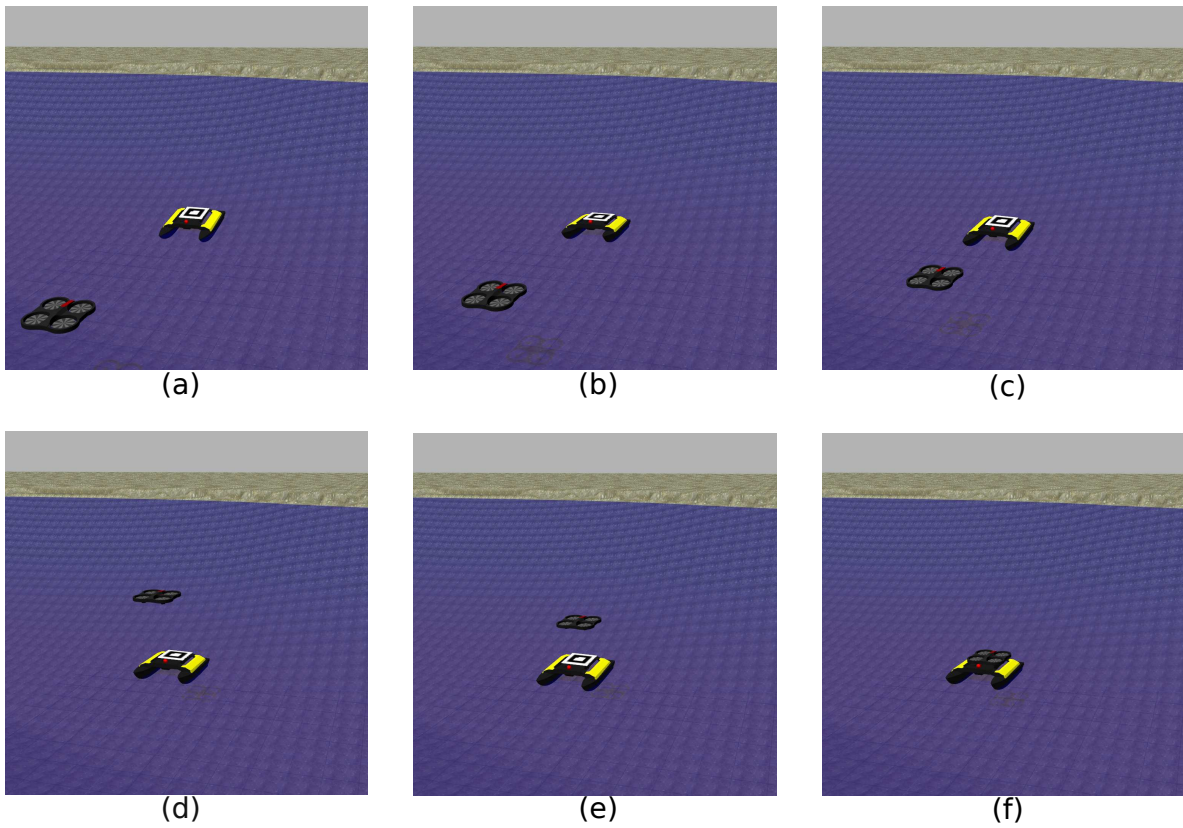


Figure 10. Landing manoeuvre of a VTOL UAV on a USV subject only to pitching disturbances.

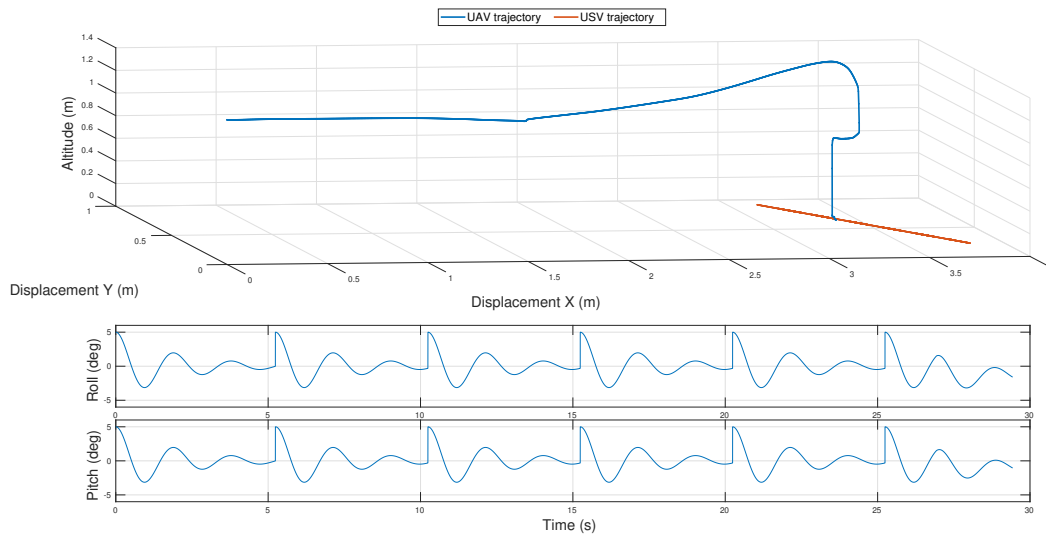


Figure 11. Above: The UAV and USV 3D trajectories, in blue and red respectively, in the UAV's reference frame. Bottom: Both the roll and pitch disturbances the USV is subject to.

279 As in the previous experiments, the two vehicles 3D trajectory are reported in Fig. 8 in the UAV's
 280 reference frame, the controller commands in Fig. 9 and example frames in Fig. 10. The quad-copter,
 281 with the same controller parameters of before, was able to follow and land on the visual marker in
 282 almost 34 seconds after identifying it 4.46 meters ahead and 0.12 meter on its left.

283 As in the case of a rolling base, Fig. 10-a shows the UAV starts moving in order to keep the
 284 visual marker at the centre of its frontal camera's field of view. This is what happens at time $t = 26s$
 285 and shown in Fig. 10-b. At $t = 6s$ the UAV reaches its minimum altitude and it is now impossible
 286 for it to see the visual marker, as illustrated in Fig. 10-c. At this point, the video stream starts to
 287 be acquired from the bottom camera and the USV's estimated position is sent to the controller. At
 288 the same time, instructing the UAV to increase its altitude to augment the total area covered with its
 289 downward-looking camera. Doing this, at $t = 13s$ the UAV is located exactly above the USV. The
 290 landing base is at centre of the camera's FOV, therefore a null velocity command is sent to stop the
 291 USV. Fig. 10-e and 10-f show the UAV can then descend slowly to centre the marker properly and, in
 292 the end, land on it.

293 Further analysis can be done with the results reported in Fig. 9. In the same way of the experiment
 294 with a rolling deck, the curve of the controller's commands and the one related to the offsets overlap
 295 for most of the time. All the considerations made before still hold: while the marker is lost, the EKF
 296 is able to estimate the landing platform's current pose with reference to the instant of time when the
 297 marker has been lost. This relative-pose is added to the last observation in order to produce a new
 298 command.

299 This is what is possible to see in the plot between $t = 21s$ and $t = 25s$. Here, the two curves differ:
 300 while all the offsets remain constant because no new marker observations have been done by the UAV,
 301 the commands (gaz and roll) slightly change. The plot is now discussed in more details. While the yaw
 302 and the pitch commands remain identical to 0 because the UAV is already aligned with the landing
 303 base (within the predefined bounds), the UAV's roll command is changed including at every instant
 304 the new relative-pose (changing on the longitudinal direction) of the USV.

305

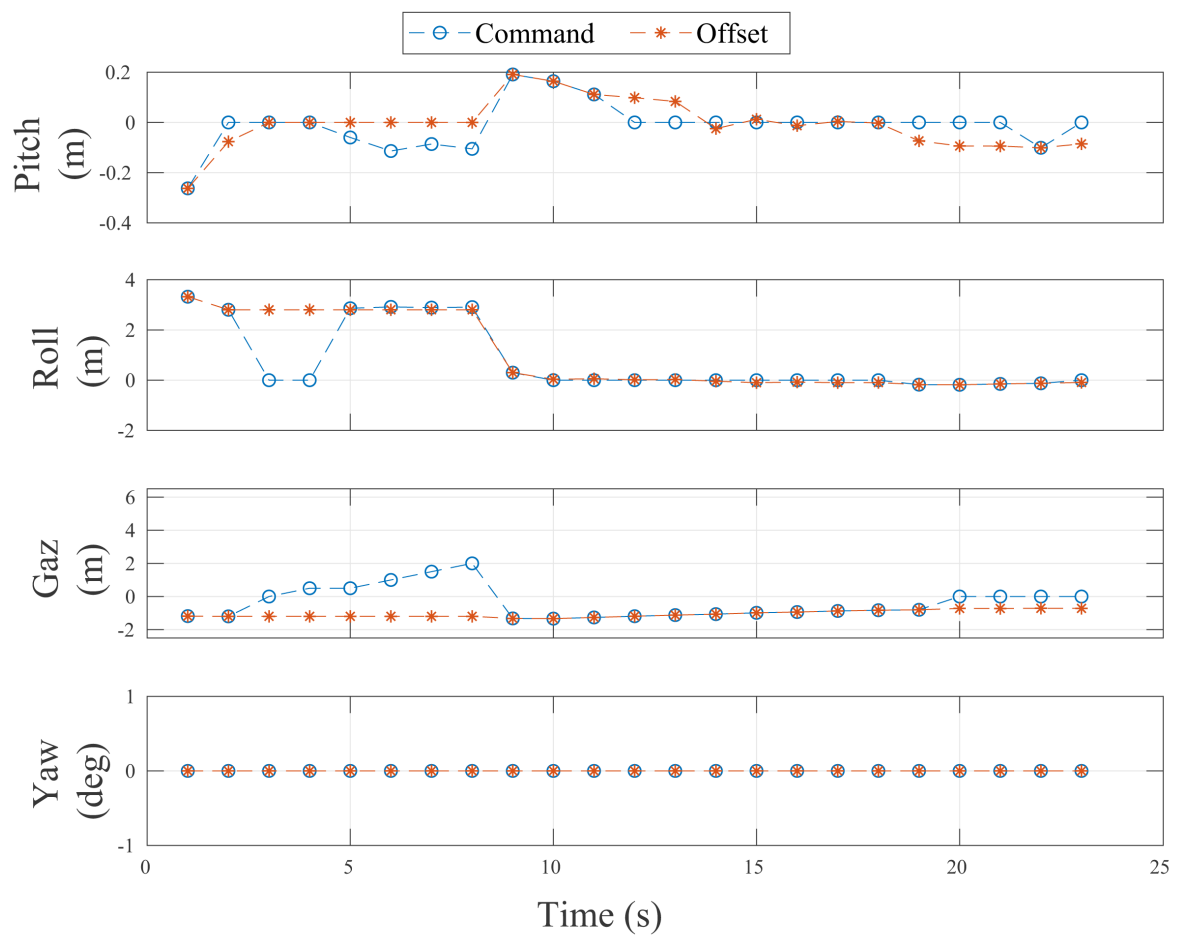


Figure 12. Controller commands and visual offsets in the experiment with a pitching and rolling landing platform, in order to simulate complex marine scenarios.

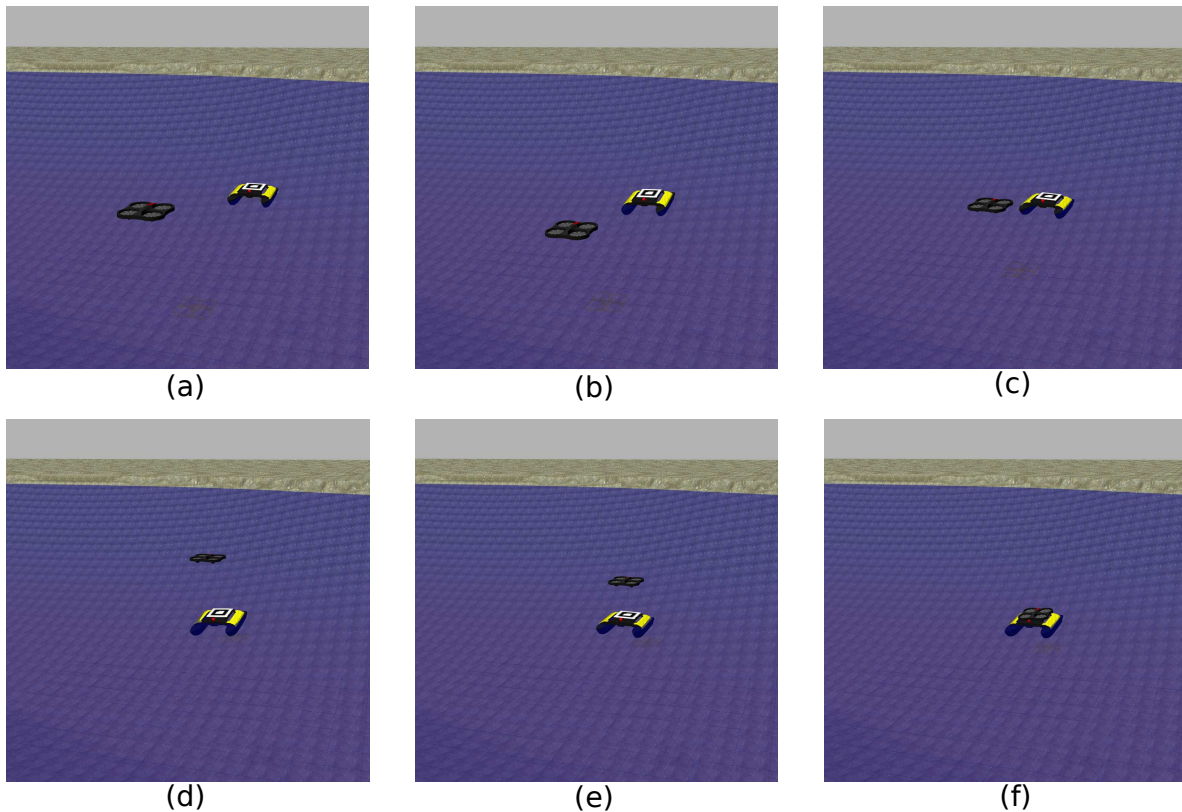


Figure 13. Landing manoeuvre of a VTOL UAV on a USV subject to both rolling and pitching disturbances, in order to simulate complex marine scenarios.

306 3.3. Rolling and Pitching Platform

307 A last simulation has been done with a floating platform that is subject to both rolling and pitching
 308 stresses. The goal of this experiment is to test the developed landing algorithm against simulated
 309 harsh marine conditions.

310 The results are reported in Fig. 11, showing the both vehicles trajectories along a 23 seconds operation.
 311 The UAV successfully accomplish the landing manoeuvre starting from an initial marker's identification
 312 3.71 meters in front of it and 0.30 meters on its left. Fig. 12 shows the comparison between the offsets
 313 obtained through the vision algorithm and the commands sent to the controller. It is possible to see
 314 that, as in the previous experiments, the curve of the offsets and the one related to the commands
 315 mainly overlap. All the analysis made before are still valid, but it is interesting to notice how the
 316 framework proposed is able to react properly also when the landing platform is subject to complex
 317 disturbances. The salient moments of the flight are illustrated in Fig. 13

318 4. Conclusion and Future Directions

319 In this paper, a solution to make an unmanned aerial vehicle to autonomously land on the deck
 320 of a USV is presented. It resides only on the UAV's on-board sensors and on the adoption of visual
 321 marker on the landing platform. In this way, the UAV can estimate the 6-DOF landing area position
 322 through an image processing algorithm. The adoption of a pose estimation filter - in this case an
 323 extended Kalman filter - allows to overcome issues with fixed non-tilting cameras and the image
 324 processing algorithm. Not involving GPS signals in the pose estimation and in the generation of flight
 325 commands, allows the UAV to land also in situations where this signal is not available (indoor scenario
 326 or adverse weather conditions).

327 The validation of the approach has been done in simulation with a quad-rotor and an unmanned
328 surface vehicle as platform on which to land. Three different experiments were performed, each of
329 them with a different type of disturbance acting on the landing base. In all scenarios successful results
330 were obtained.

331 The future research is twofold. From a practical point of view, the proposed approach needs
332 to be tested in a real environment with an unmanned surface vehicle in order to test its robustness
333 against real wind and sea currents. The second aspect is more related to the identified limitation of
334 the algorithm itself. Therefore it is suggested to develop an adaptive controller, possibly based on
335 intelligent solution such as artificial neural networks or fuzzy logic, where the gain of the controller
336 change depending on the distance to the landing base.

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338 experiments. Sanjay Sharma and Jian Wan provided valuable feedback and revisions. Andrew Manning and
339 Robert Sutton contributed in writing and proofreading the manuscript.

340 **Conflicts of Interest:** The authors declare no conflict of interest.

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